COOLING OF THE 6-CENTIMETER AND 2-CENTIMETER DOUBLETS OF INTERSTELLAR H$_2$CO BY COLLISION: AN ACCURATE QUANTUM-MECHANICAL CALCULATION

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ABSTRACT

Cooling of the 6-cm and 2-cm levels of interstellar H$_2$CO by a collisional pump is verified by a series of accurate quantum-mechanical calculations. The $j = 3$ ortho doublet is found to be an integral part of the collisional pumping scheme.

Subject headings: atomic and molecular processes — molecules, interstellar — quantum mechanics

During the past few years, considerable interest has developed around observations of anomalous absorption in interstellar formaldehyde. This absorption is anomalous because it implies an excitation temperature for two rotational states lower than both the background radiation temperature (≈2.7 K) and the expected kinetic temperature (10–20 K). These observations are widespread throughout space and are seen in (1) the $1_1^0 - 1_1$ (6 cm) transition of H$_2$CO (Palmer et al. 1969; Dieter 1973; Minn and Greenberg 1973), (2) the $2_1^1 - 2_1$ (2 cm) transition of H$_2$CO (Evans, Cheung, and Sloanaker 1970; Evans 1973; Evans et al. 1975), and (3) the $1_1^0 - 1_1$ transition of the isotope H$_2^{13}$CO (Evans et al. 1975). To obtain such low excitation temperatures requires a nonthermal cooling mechanism.

A number of pumping models have been proposed that involve transitions to higher rotational states of H$_2$CO and then radiative decay. The pump or force causing the excitations has been variously suggested as being due to collisions (Townes and Cheung 1969) or to radiation at millimeter (Solomon and Thaddeus 1970; Thaddeus 1972a), infrared (Litvak 1970), and ultraviolet (Oka 1970) wavelengths. Evans et al. (1975) have recently given a convincing discussion indicating that the collisional pump is the only model that accounts for all the observations and satisfies necessary criteria.

Since the collisional pump appears to be the key to understanding interstellar cooling of H$_2$CO, several workers have attempted to theoretically verify this model by determining the appropriate rotational cross sections (Townes and Cheung 1969; Thaddeus 1972a, b; Evans 1973; Augustin and Miller 1974; Evans et al. 1975; Evans 1975). These calculations suffer from using either approximate interaction potentials (hard or soft sphere), approximate dynamics (classical or semiclassical calculations), or inappropriate approximations (Born or sudden). In the present study, both the interaction potential and resulting cross sections and rates are determined using accurate quantum-mechanical methods in order to obtain a reliable test of the collisional pumping model.

For these calculations, the most probable scatterer H$_2$ is replaced by He to reduce the scope of the computation. It is anticipated that the main conclusions of this study will not be seriously altered by this choice of scattering particle. To determine the interaction potential for the H$_2$CO–He system, we have solved the electronic Schrödinger equation including electron correlation (Garrison, Lester, and Schafer 1975a, b). The interaction is highly anisotropic and has a 35–40 K attraction arising mainly from dispersion effects. The well depth is believed reliable to ≈20 percent.

For the dynamics, quantum-mechanical cross sections were computed following an extension of the Arthurs and Dalgarno (1960) coupled-channel formalism to the
scattering of an asymmetric rotor by an atom (Garrison, Lester, and Miller 1975c). A total of 16 ortho H$_2$CO states were included in the coupled-channel expansion. Note that from four to eight states are energetically open at the scattering energies considered. Total inelastic cross sections were calculated at a total of 12 energies for 20 K \( \leq E(K) \leq 95 \) K, where \( E \) is the sum of the internal energy of H$_2$CO and the relative kinetic energy. Details of these calculations and results will be published elsewhere (Garrison et al. 1975c).

Inelastic cross sections were obtained for the lowest eight ortho levels of H$_2$CO. (For convenience the energy levels are numbered in ascending order of energy [see Fig. 1 of Thaddeus 1972b]; i.e., state 1 is 11, state 2 is 12, state 3 is 21, etc.; thus the low excitation temperatures occur between states 1 and 2 and between states 3 and 4.) Many of the cross sections exhibited resonances at one of two energies, \( E_{res} = 32.7 \) K or 47.7 K. These energies correspond to the \( j = 3 \) and \( j = 4 \) ortho doublets, respectively. Boltzmann averaged rate constants were determined from these cross sections and are given in Table 1 for a kinetic temperature of 15 K. Because the \( j = 4 \) cross sections are not determined at enough energies to form a Boltzmann average, only rate constants for \( j \leq 3 \) are tabulated.

Using the computed rate constants, the equations of statistical equilibrium were solved for the lowest eight energy levels. The background radiation temperature is assumed to be 2.7 K, and the kinetic temperature is varied from 5 to 20 K. Plots of the excitation temperature as a function of He concentration are displayed in Figure 1. Cooling of both the 6 cm (T$_{12}$) and 2 cm (T$_{34}$) doublets is seen to occur for kinetic temperatures between 10 and 20 K, but not for 5 K.

Since resonance contributions to the cross sections can be large at the lowest energies considered, an attempt was made to estimate their importance on the cooling curves. The widths and heights were varied by a factor of 2, with no qualitative change in the cooling curves for He concentrations less than 10$^5$ molecules cm$^{-3}$. The quantitative change in the excitation temperatures, T$_{12}$ and T$_{34}$, was found to be less than 0.2 K.

Having established that the 6 cm and 2 cm doublets of H$_2$CO are cooled by a collisional pump, the question of the relative importance of the various transitions remains to be fully elucidated. By varying the number of states used in the equations of statistical equilibrium, the effect of the different \( j \) doublets on the cooling can be assessed. Neglect of the \( j = 4 \) levels caused less than 0.2 K changes in the effective temperatures for He concentrations at which cooling occurs. Omission of the \( j = 3 \) levels, however, resulted in no cooling. Thus

<table>
<thead>
<tr>
<th>TABLE 1</th>
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<tbody>
<tr>
<td><em><em>Rate Constants</em> at ( T_k = 15 ) K</em>*</td>
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</table>

<table>
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<th>Initial State</th>
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<th>21</th>
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<th>31</th>
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<td>11</td>
<td>5.5</td>
<td>5.0</td>
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<td>0.2</td>
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<tr>
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<td>3.4</td>
<td>1.3</td>
<td>0.8</td>
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<tr>
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<td>2.8</td>
<td>3.9</td>
<td>3.8</td>
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<tr>
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<td>31</td>
<td>1.7</td>
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* In units of 10$^{-11}$ cm$^3$ molecule$^{-1}$ s$^{-1}$.

![Fig. 1. — Excitation temperatures as a function of He density at selected kinetic temperatures](image-url)
the $j = 3$ ortho doublet plays an integral role in the cooling of $\text{H}_2\text{CO}$. At low He concentrations ($\lesssim 10^6$ molecules cm$^{-3}$) radiative contributions are found to dominate collisional dipole allowed transitions so that rate constants $k_{12}$, $k_{13}$, $k_{24}$, $k_{36}$, $k_{46}$, and $k_{56}$ are of minor importance. Ratios of dipole forbidden transitions, e.g., $k_{25}/k_{16}$, are the indicators of cooling. The large ratio of $k_{25}/k_{16} \approx 6$ in Table 1 implies that transitions from the $j = 1$ to the $j = 3$ doublets are the prime determiners of the cooling.

For collisions of the isotopic homologue $\text{H}_2^{13}\text{CO}$ the Born-Oppenheimer interaction potential is the same as before and all differences are contained in the dynamics treatment. They involve small changes in the center of mass of $\text{H}_2\text{CO}$, the reduced mass of the total system, and the energy level spacing. These differences are expected to have little effect on the scattering cross sections. For these reasons it seems likely that the $j = 1$ doublet of $\text{H}_2^{13}\text{CO}$ will also be cooled, in agreement with observations.

By a series of accurate quantum-mechanical calculations, the collisional pump is confirmed as a cooling mechanism for the 6 cm ($j = 1$) and 2 cm ($j = 2$) doublets of ortho $\text{H}_2\text{CO}$. The $j = 3$ levels are found to be an integral part of the pumping scheme.

REFERENCES


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