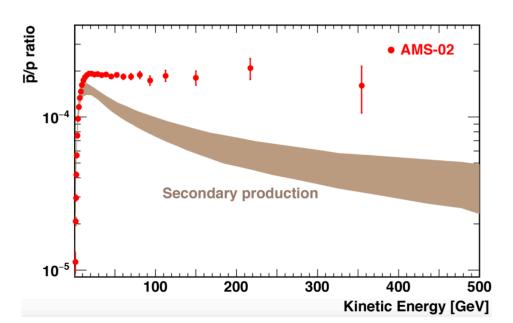
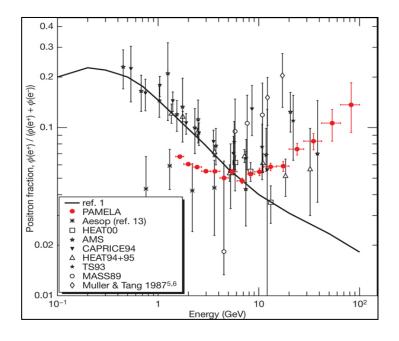
**Issues on CR propagation and local sources** 

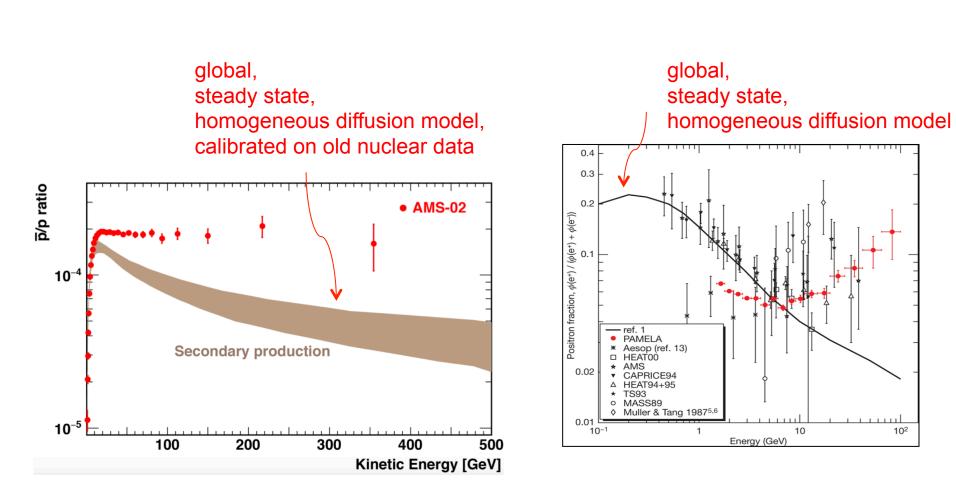
Kfir Blum Weizmann Institute

MACROS 2016 PSU

### Positrons and antiprotons



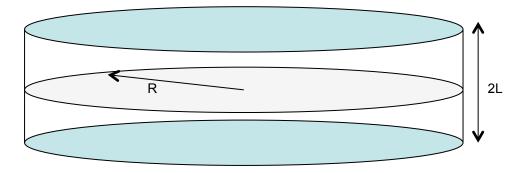


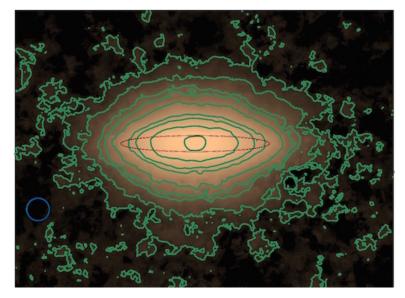


10<sup>2</sup>

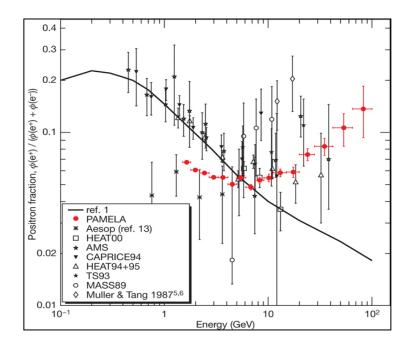
### diffusion model constructed to give a large-scale description

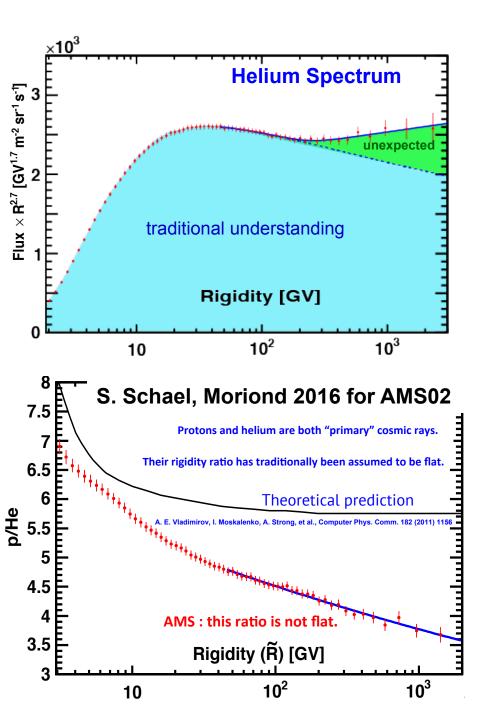
Ginzburg & Ptuskin, Rev.Mod.Phys. 48 (1976) 161-189 Strong, Moskalenko, Ptuskin, Ann.Rev.Nucl.Part.Sci. 57 (2007) 285-327

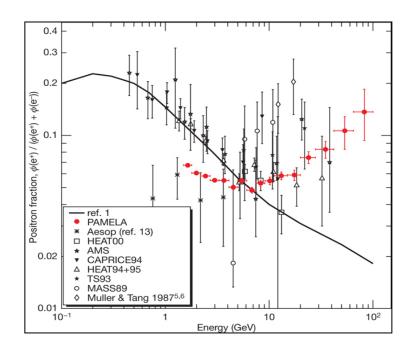


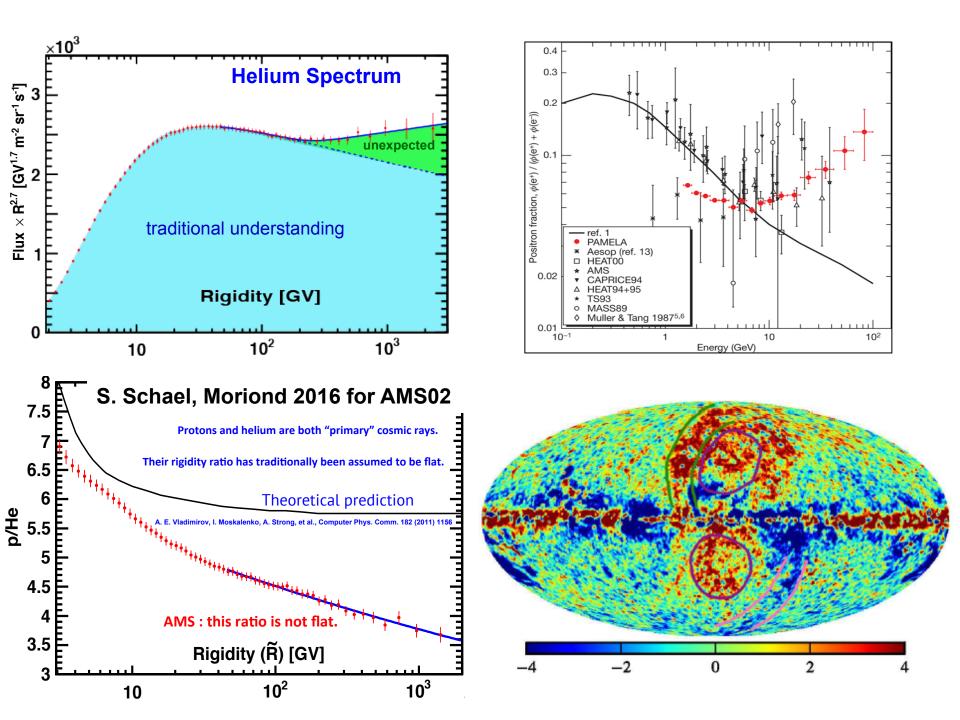


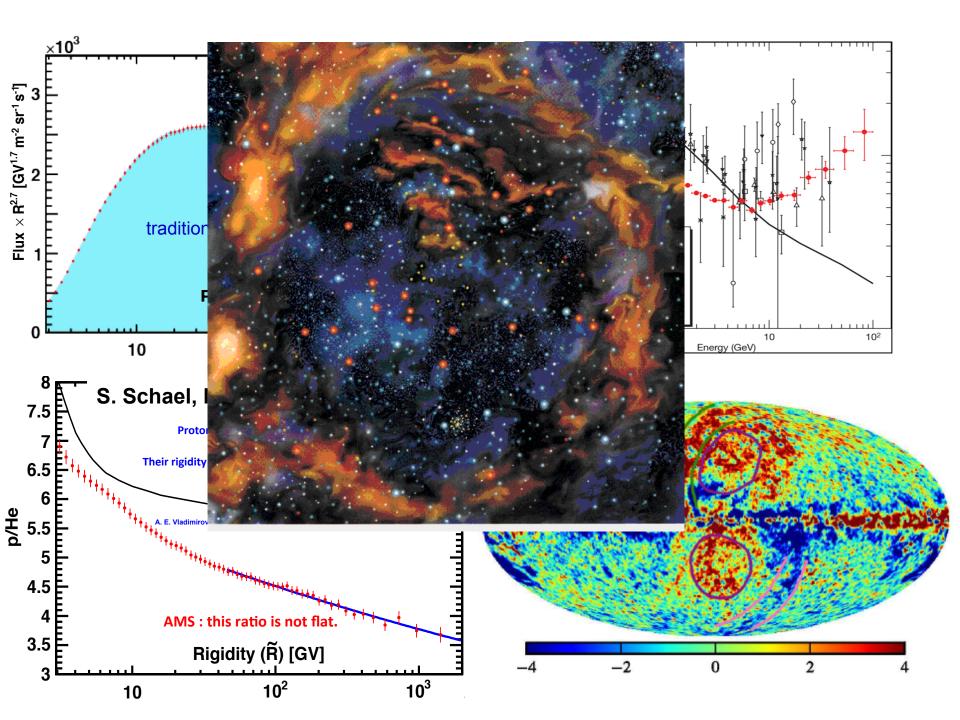
Irwin et al, ApJ 144(2012) [stacking 30 galaxies]







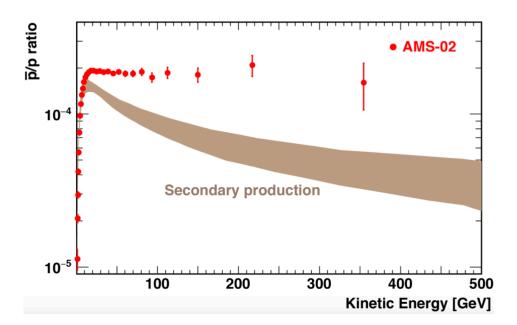


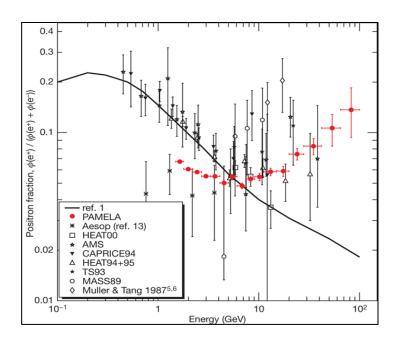


### Positrons and antiprotons

What's consistent w/ old global models and what not? Model building hints in data

- Antiprotons vs. B/C
- e+





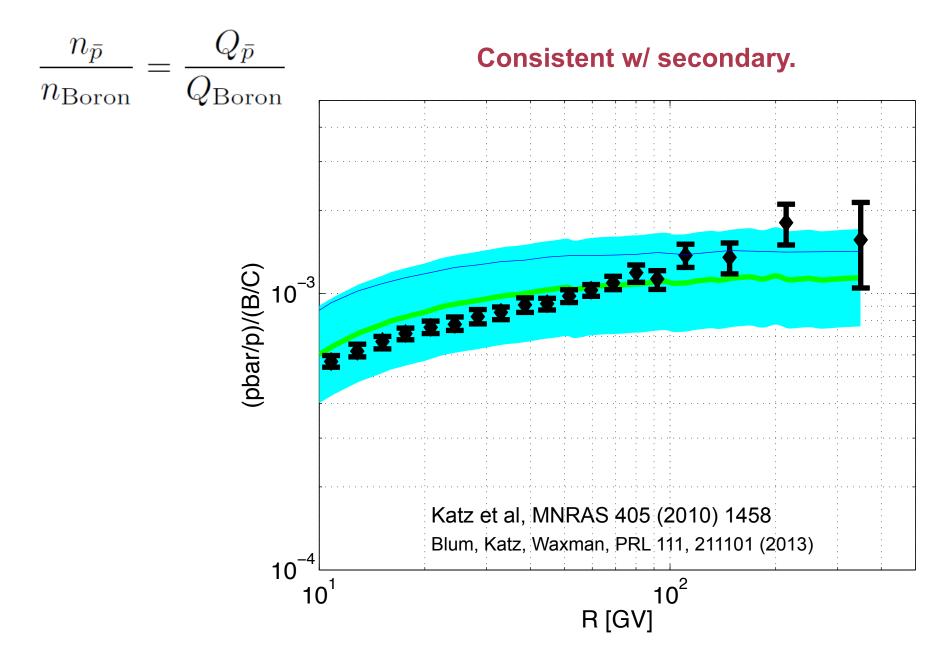
# antiprotons

$$\frac{n_{\bar{p}}}{n_{\rm Boron}} = \frac{Q_{\bar{p}}}{Q_{\rm Boron}}$$

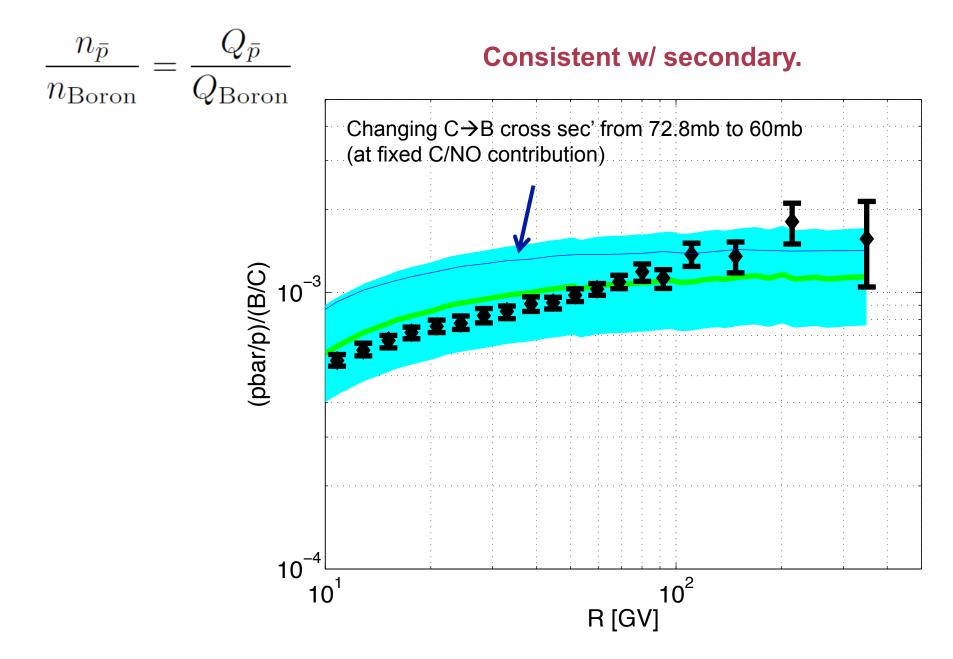
$$\frac{J_{\bar{p}}}{J_p} = 10^{1-\gamma_p} \zeta_{\bar{p},A>1} C_{\bar{p},pp} \frac{\sigma_{pp,\text{inel}}}{m_p} \frac{X_{\text{esc}}}{1+\frac{\sigma_{\bar{p}}}{m_p} X_{\text{esc}}}$$

$$X_{\rm esc} = \frac{\frac{n_B}{n_C}}{\sum_{i=C,N,O,\dots} \left(\frac{\sigma_i \to B}{\bar{m}}\right) \frac{n_i}{n_C} - \left(\frac{\sigma_B}{\bar{m}}\right) \frac{n_B}{n_C}}$$

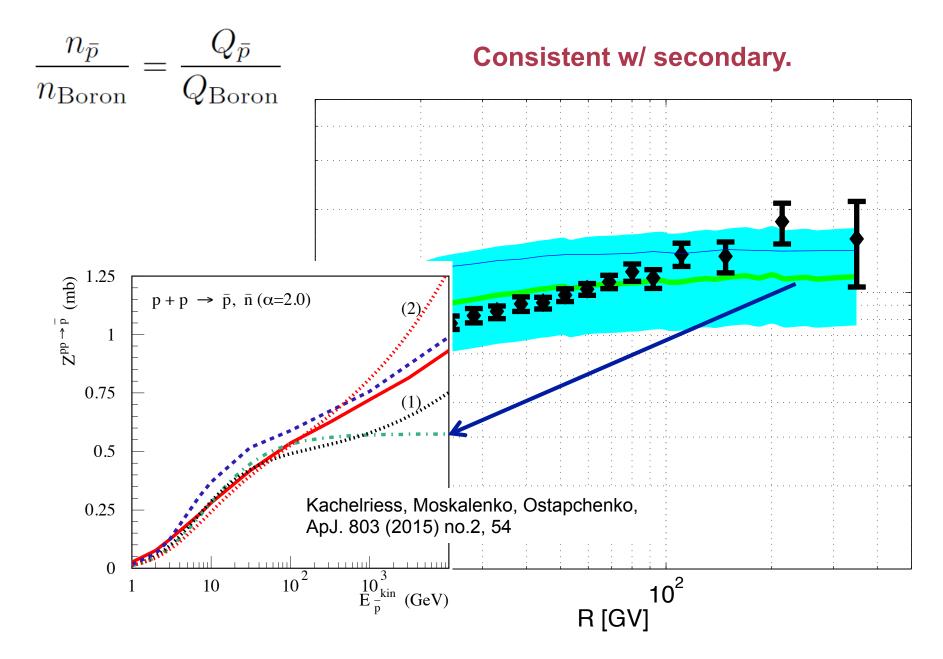
# antiprotons vs. boron (AMS02 2014): results



### antiprotons vs. boron (AMS02 2014)



### antiprotons vs. boron (AMS02 2014)



### Positrons and antiprotons

What's consistent w/ old global models and what not?

- Model building guidelines in data
- Antiprotons vs. B/C consistent w/ secondary, no problem w/ global models
- e+

# positrons

$$\frac{J_{e^+}}{J_p} = f_{e^+} \times 10^{1-\gamma_p} \zeta_{e^+,A>1} C_{e^+,pp} \frac{\sigma_{pp,\text{inel}}}{m_p} X_{\text{esc}}$$

### positrons

$$\frac{J_{e^+}}{J_p} = f_{e^+} \times 10^{1-\gamma_p} \zeta_{e^+,A>1} C_{e^+,pp} \frac{\sigma_{pp,\text{inel}}}{m_p} X_{\text{esc}}$$

# e+ lose energy through IC and synchrotron radiation.

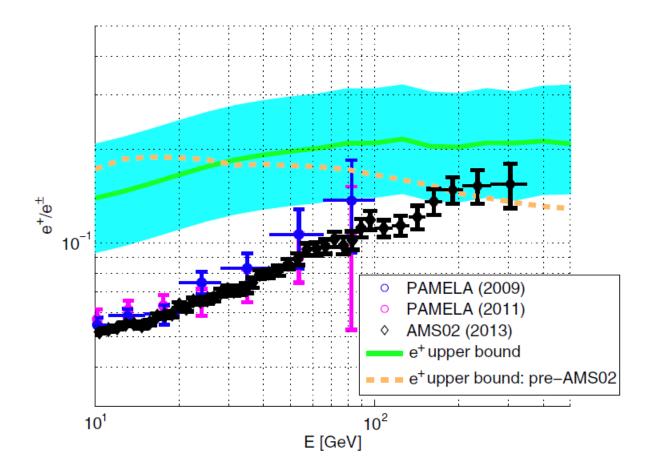
The amount of loss depends on the propagation time  $t_{esc}$  vs. energy loss time  $t_{cool}$ 

### e+ data itself is the first (semi-)direct observational probe of t<sub>esc</sub>.

What we can say:

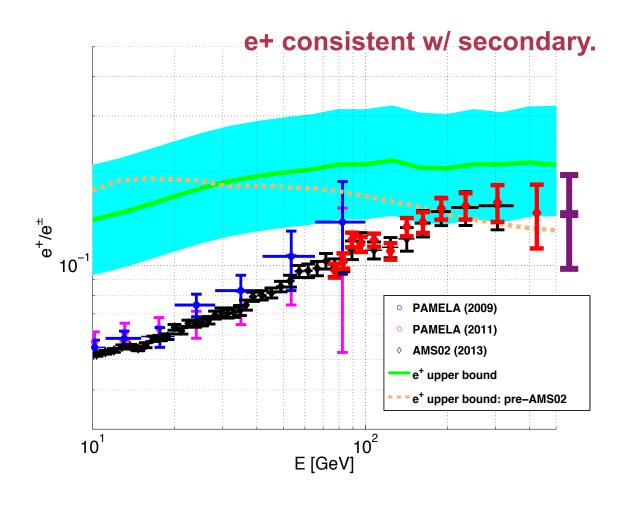
$$f_{e^+} < 1$$

# AMS02 (2013): results

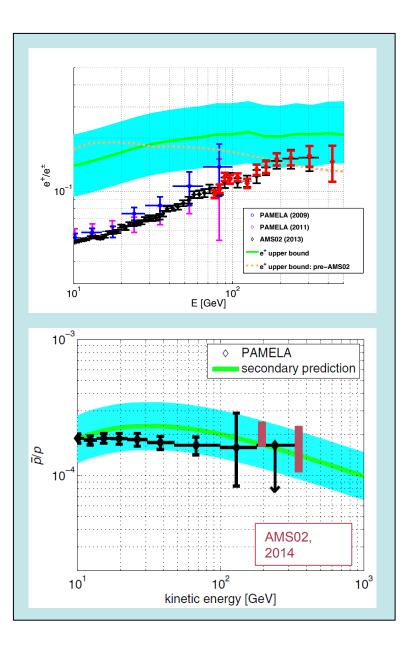


Katz et al, MNRAS 405 (2010) 1458 Blum, Katz, Waxman, PRL 111, 211101 (2013)

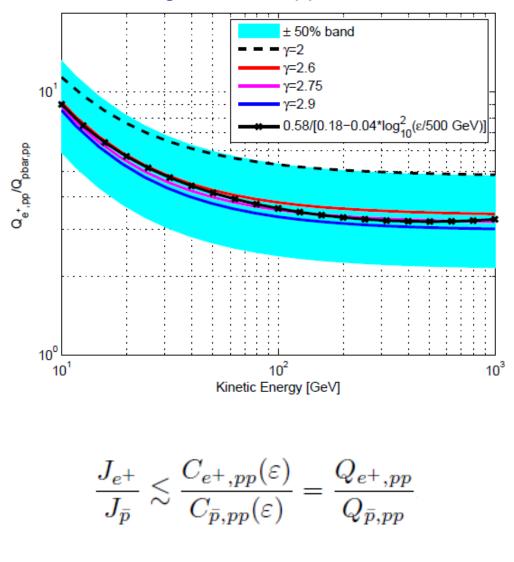
### AMS02 (2014 I+II) (last error bar: rough estimate)



# A clean test: $e^+/\overline{p}$

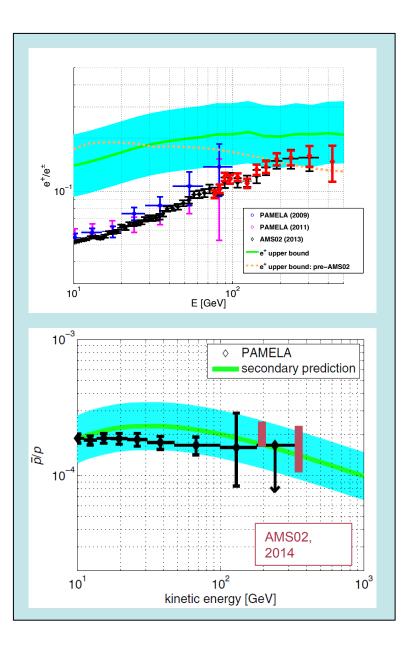


### branching fraction in pp collision:

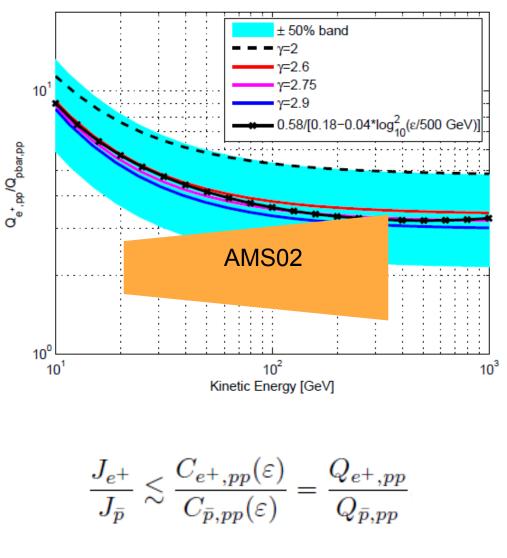


Katz et al, MNRAS 405 (2010) 1458

# A clean test: $e^+/\overline{p}$



### branching fraction in pp collision:



Katz et al, MNRAS 405 (2010) 1458

### Positrons and antiprotons

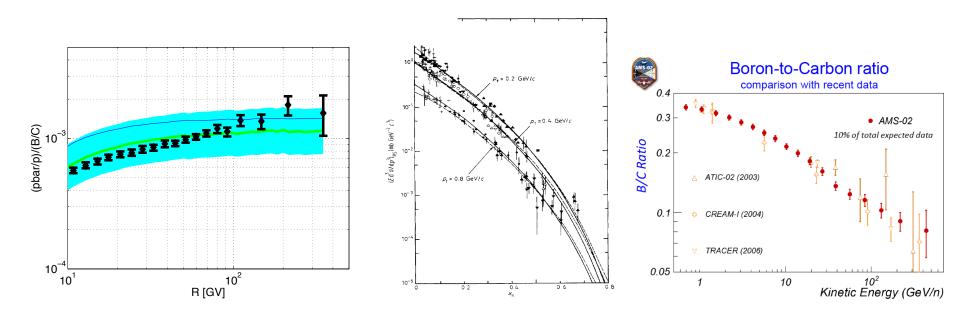
What's consistent w/ old global models and what not?

- Model building guidelines in data
- Antiprotons vs. B/C consistent w/ secondary, no problem w/ global models
- e+ consistent w/ robust calculation for secondary

*inconsistent* w/ common diffusion model

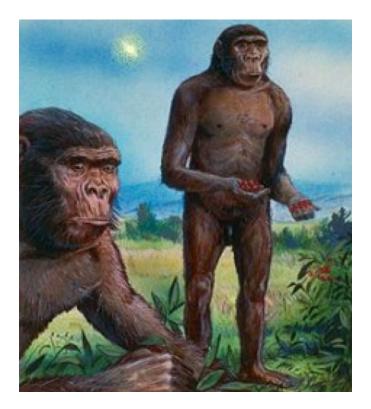
- Local, non steady state sources
- Pulsars

up to now: dry particle physics perspective



- Local, non steady state sources
- Pulsars

now: astrophysics



- Local, non steady state sources
- Pulsars

nearby supernova O(100pc) away and 10<sup>6</sup> years ago

Savchenko, Kachelries, Semikoz, ApJ809 (2015) Kchelries, Neronov, Semikoz, PRL115 (2015) Giacinti, Kachelries, Semikoz, PRD91 (2015) Giacinti, Kachelries, Semikoz, PRD88 (2013)

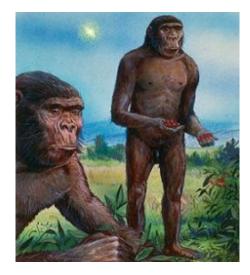
Secondary e+ and pbar from same spectrum p

(should add C, B/C?)

Age of 200GV CR is ~ O(1Myr)

200GV CR live in local ISM density ~ 1mp/cm<sup>3</sup>

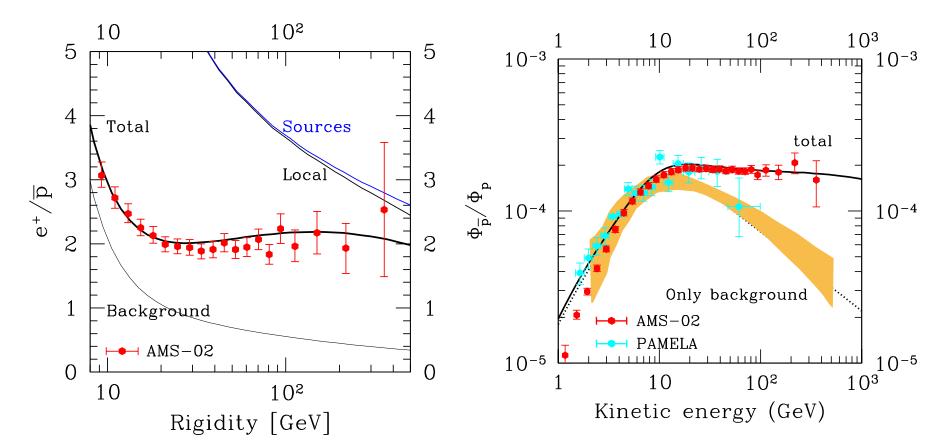
Calibrating global diffusion model from local nuclei would be wrong



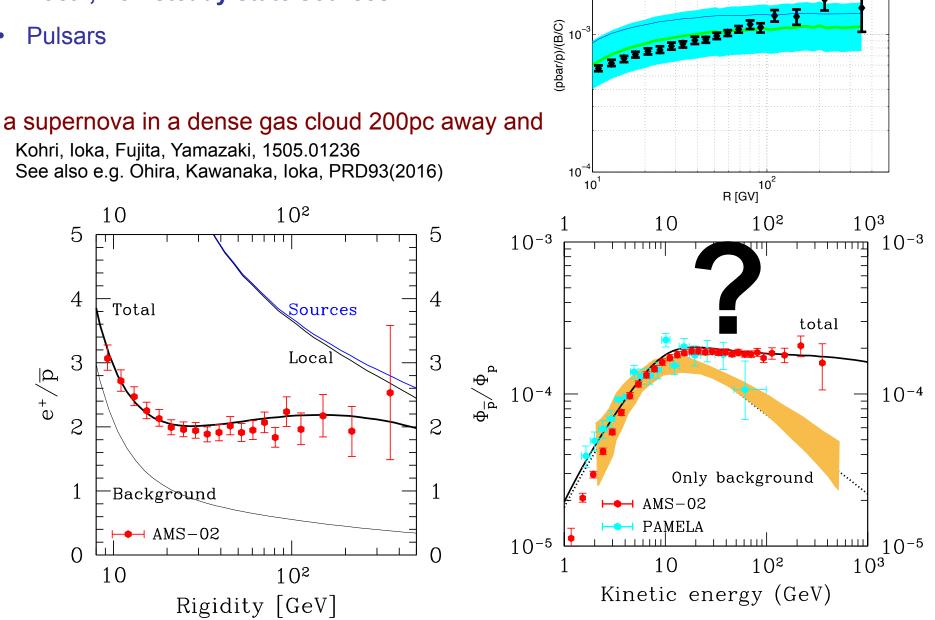
- Local, non steady state sources
- Pulsars

#### a supernova in a dense gas cloud 200pc away and 10<sup>5</sup> years ago

Kohri, Ioka, Fujita, Yamazaki, 1505.01236 See also e.g. Ohira, Kawanaka, Ioka, PRD93(2016)



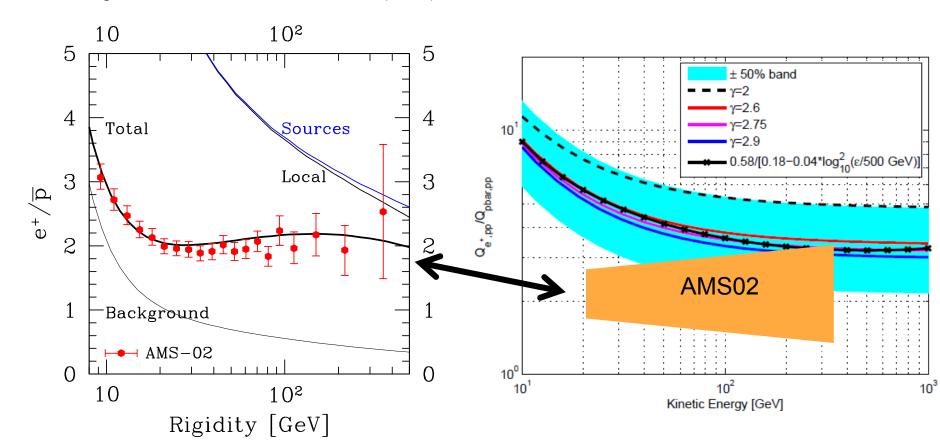
- Local, non steady state sources
- Pulsars



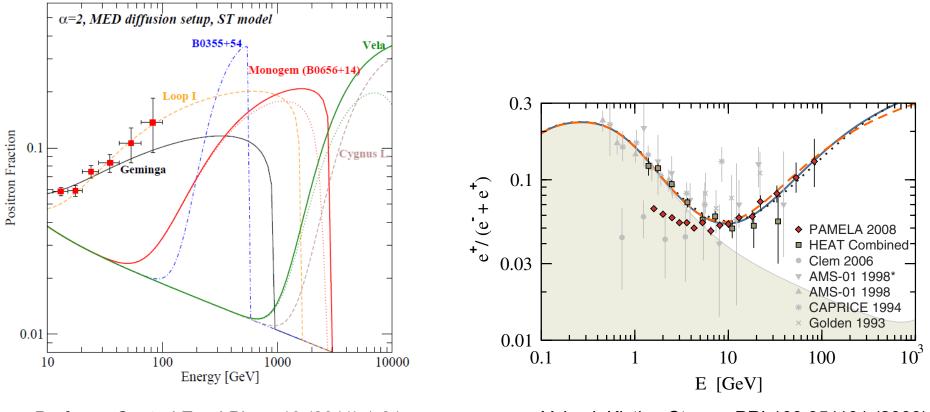
- Local, non steady state sources
- Pulsars

### a supernova in a dense gas cloud 200pc away and 10<sup>5</sup> years ago

Kohri, Ioka, Fujita, Yamazaki, 1505.01236 See also e.g. Ohira, Kawanaka, Ioka, PRD93(2016)



- Local, non steady state sources
- Pulsars



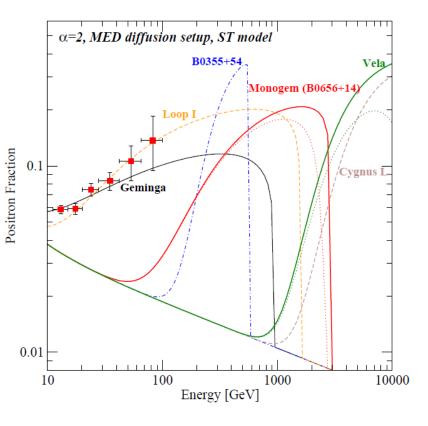
Profumo, Central Eur.J.Phys. 10 (2011) 1-31

Yuksel, Kistler, Stanev, PRL103.051101 (2009)

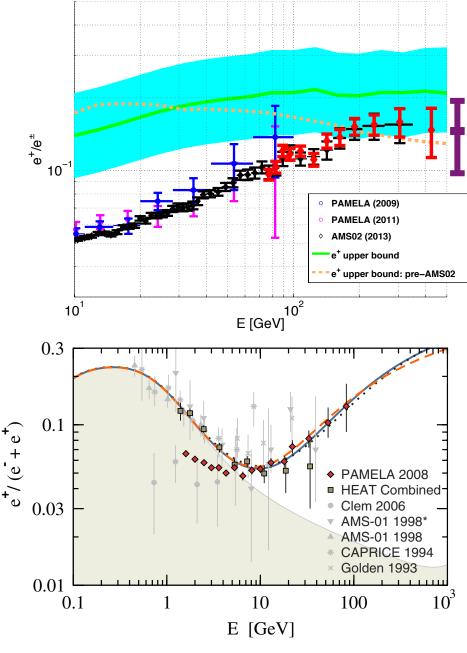
• Local, non steady state sources

Pulsars

Why would pulsars inject this e+ flux?



Profumo, Central Eur.J.Phys. 10 (2011) 1-31

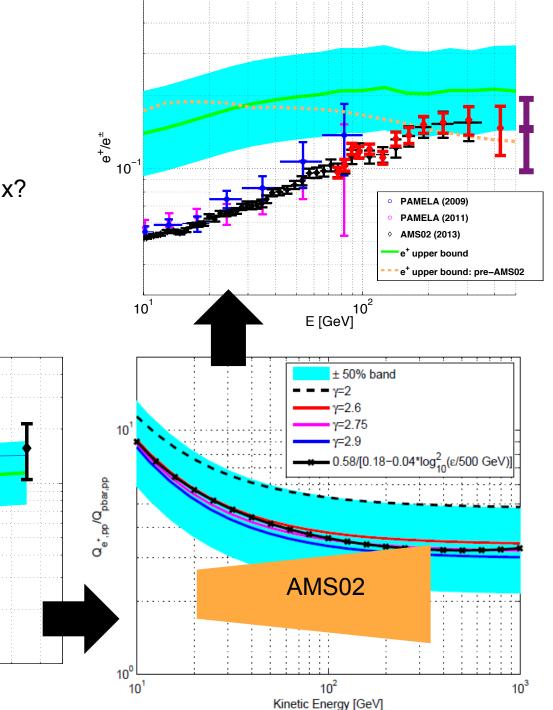


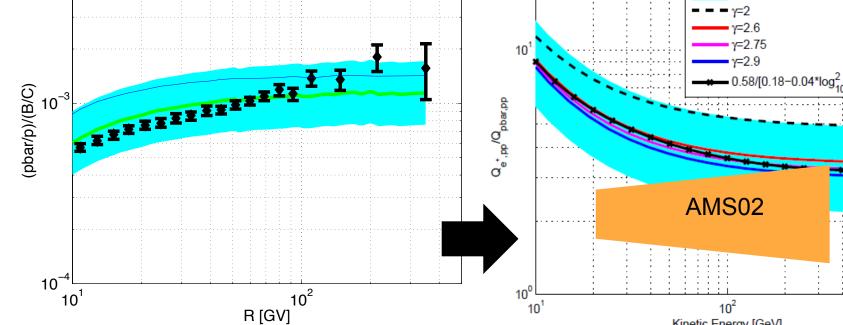
Yuksel, Kistler, Stanev, PRL103.051101 (2009)

Local, non steady state sources

**Pulsars** 

Why would pulsars inject this e+ flux?





# Summary

pbar consistent with secondary (pbar/p)/(B/C)
e+ consistent w/ pbar

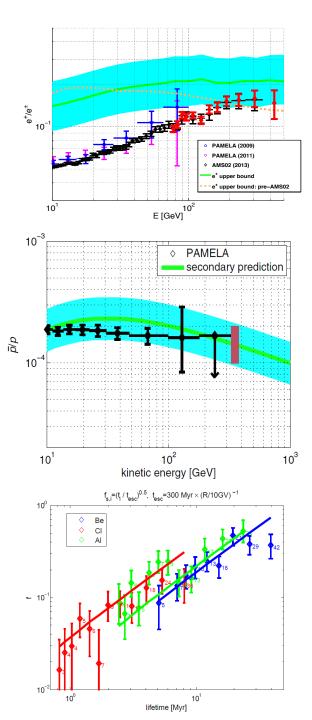
e+ rule out canonical diffusion model
secondary e+ require t<sub>esc</sub> ~ t<sub>cool</sub> (why?)
→ R-dependent mean ISM density
CR containment region may vary w/ R (why not?)
inferred density at 300GV ~ density of MW gas disc

Local secondary source/non steady state: pbar/p consistent w/ B/C  $\rightarrow$  source better spalate nuclei. If dominate pbar/p, should also dominate B/C,... p and C...

Pulsar/dark matter: Why would a primary source inject *this* J<sub>e+</sub>?

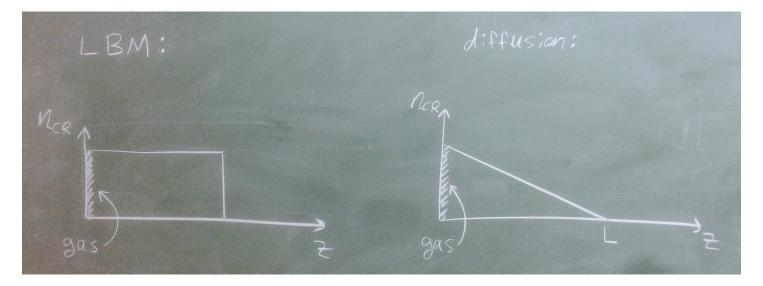
Future tests w/ AMS02: radioactive nuclei at 10-100GV

Thank you!

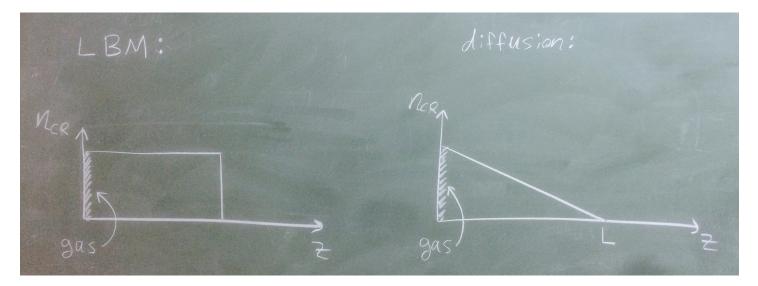


# **Xtras**

# Interpretation: model dependence



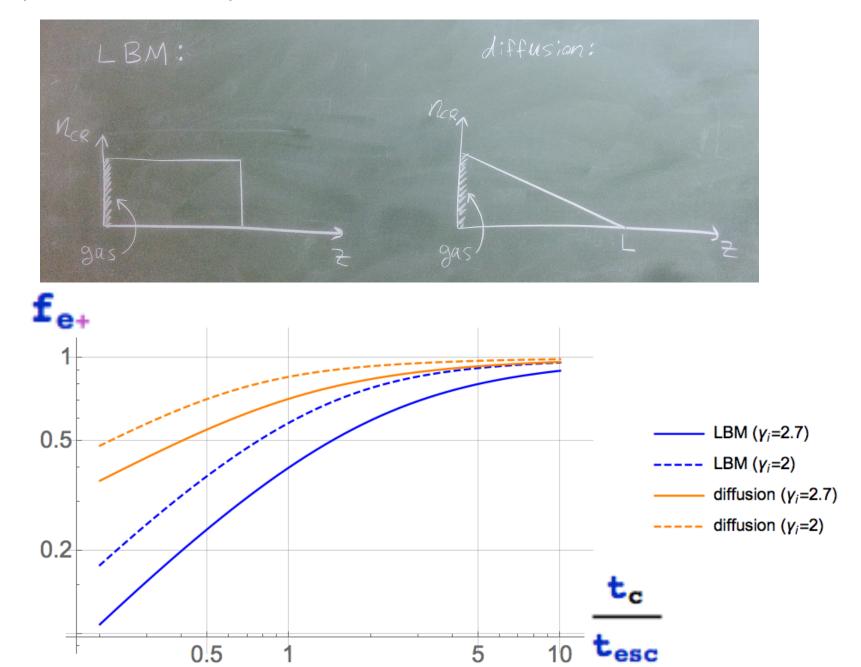
# Interpretation: model dependence



$$f_{e+}^{\text{LBM}}(\epsilon) = \frac{t_c(\epsilon)}{t_e(\epsilon)} \int_1^\infty dx x^{-\gamma_i} \exp\left[-\frac{t_c(\epsilon)}{t_e(\epsilon)} \frac{1-x^{\delta-1}}{1-\delta}\right] \longrightarrow \frac{1}{\gamma_i - 1} \frac{t_c(\epsilon)}{t_e(\epsilon)}$$

$$f_{e+}^{\text{diff}}(\epsilon) = \sqrt{\frac{t_c(\epsilon)}{t_e(\epsilon)}} \sqrt{\frac{1-\delta}{\pi}} \int_1^\infty dx \frac{x^{-\gamma_i}}{\sqrt{1-x^{\delta-1}}} \sum_{n=-\infty}^\infty (-1)^n \exp\left[-\frac{1-\delta}{1-x^{\delta-1}} \frac{t_c(\epsilon)}{t_e(\epsilon)} n^2\right] \\ \longrightarrow \sqrt{\frac{t_c(\epsilon)}{t_e(\epsilon)}} C_{\text{diff}}(\gamma_i, \delta), \quad C_{\text{diff}}(2.7, 0.4) \approx 0.8$$

### Interpretation: model dependence

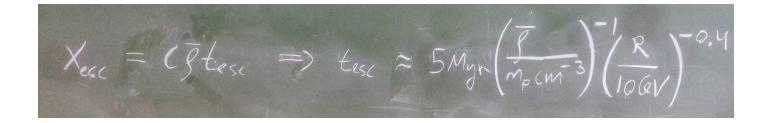


# Interpretation: t<sub>esc</sub>



dt dt tesc  $\int dt c f(\bar{X}(t)) >$ REE P







$$X_{esc} = (\overline{g} t_{esc} \Longrightarrow t_{esc} \approx 5 Myr \left(\frac{\overline{p}}{m_p cm^{-3}}\right)^{-1} \left(\frac{R}{10 GV}\right)^{-0.4}$$

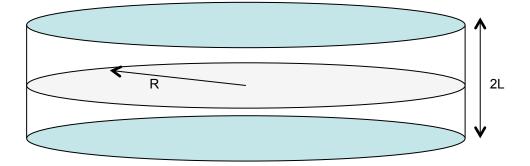
Common diffusion models:  $t_{esc} \sim X_{esc}$ 

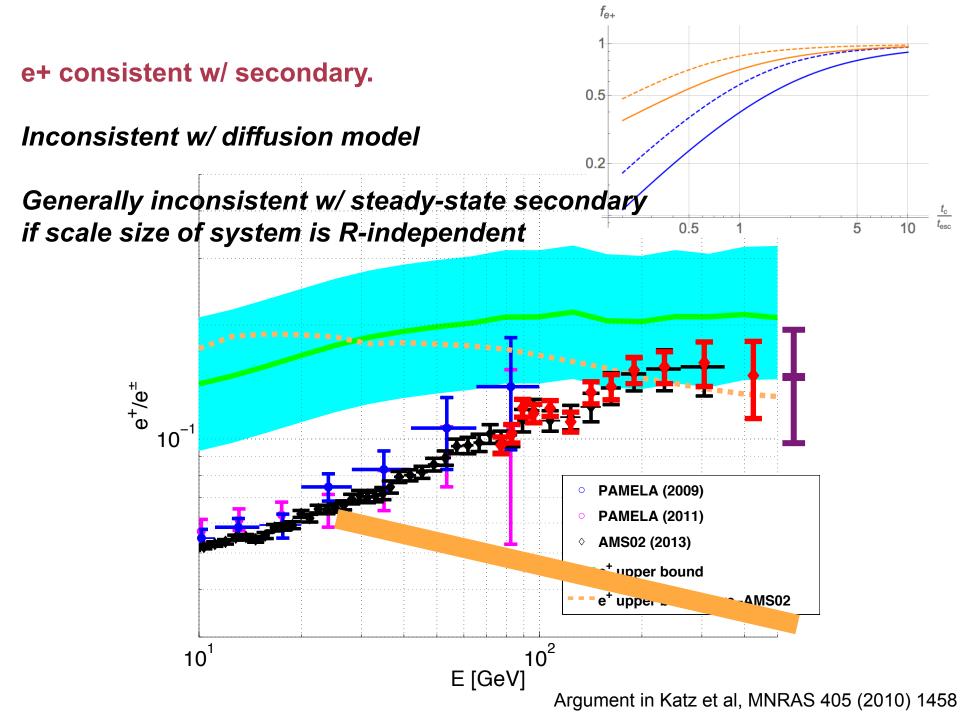
$$\label{eq:product} \begin{split} \rho &\sim X_{disc}/L, \ X_{esc} \sim (L/D) c X_{disc}, \\ t_{esc} &\sim X_{esc}/\rho c \sim L^2/D, \end{split}$$



because L is constant,

$$t_{esc} \sim X_{esc} \sim R^{-0.4}$$









R~300GV

More general (still steady state) set-up: p depends on CR rigidity

$$X_{\rm esc} = c \,\bar{\rho} \,t_{\rm esc} \quad \Rightarrow \quad t_{\rm esc} = 5 \,\,\mathrm{Myr} \left(\frac{\bar{\rho}}{m_p \,\mathrm{cm}^{-3}}\right)^{-1} \left(\frac{\mathcal{R}}{10 \,\,\mathrm{GV}}\right)^{-0.4}$$

\* More energetic CR fail to return from far above disc

\* Leads to  $\rho$  rising w/ CR rigidity



### Interpretation for secondary production

t<sub>c</sub>/t<sub>esc</sub> constant or *growing w/ rigidity*?

tc

 $t_{esc}$ 

5

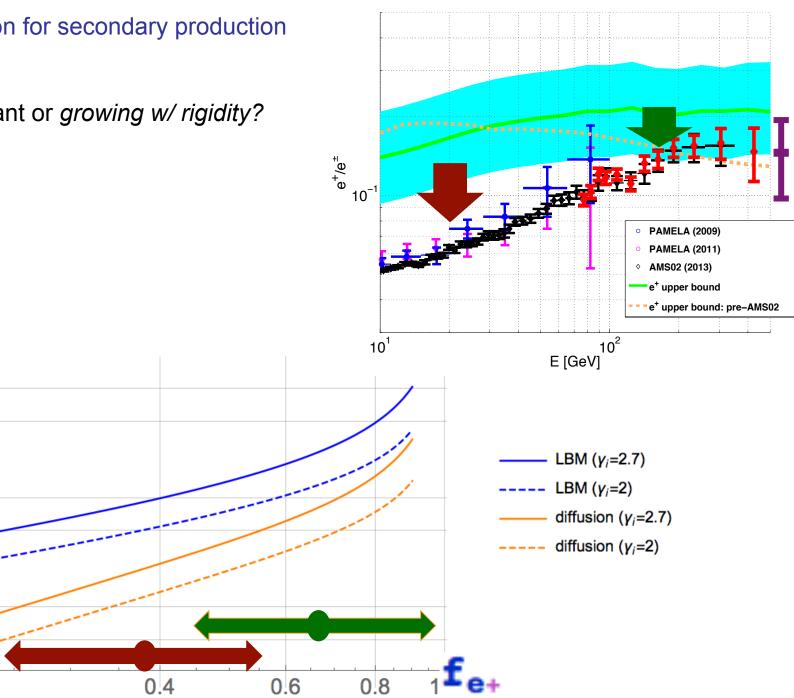
1

0.50

0.10

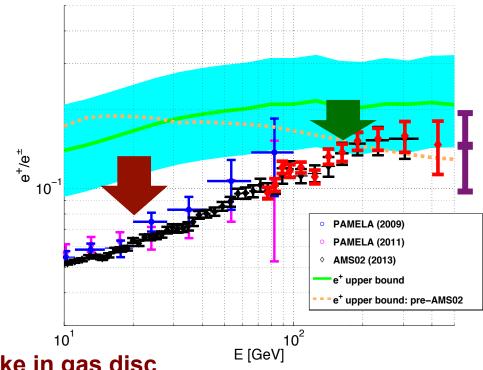
0.05

0.2



## Interpretation for secondary production

 $t_c/t_{esc}$  constant or growing w/ rigidity?



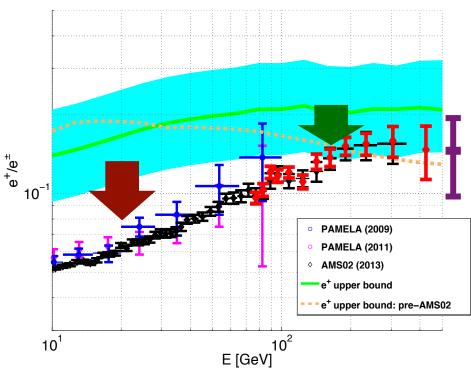
## Comments:

• Cooling time for 300GV e+ is ~1Myr. Setting  $t_{esc} \sim t_c$ , we get  $\rho \sim 1 m_p/cm^3$ , **like in gas disc** 

$$X_{esc} = (\overline{g} t_{esc} \Longrightarrow) t_{esc} \approx 5 M_{yr} \left( \frac{\overline{F}}{m_p cm^{-3}} \right)^{-1} \left( \frac{R}{10 GV} \right)^{-0.4}$$

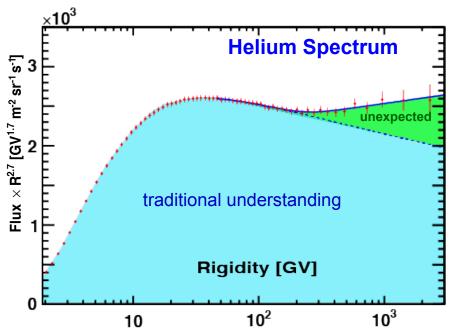
### Interpretation for secondary production

 $t_c/t_{esc}$  constant or growing w/ rigidity?



## Comments:

• Other things happen around 200GV?



Expect:

$$J_{p,\text{inject}} \propto \mathcal{R}^{-\gamma_0}, \quad \gamma_0 \gtrsim 2$$

Worry in literature: "if  $t_{esc} \sim R^{-1}$  then..."

$$J_{p,\text{obs}} \sim t_{\text{esc}} \times J_{p,\text{inject}} \propto \mathcal{R}^{-\gamma_0 - 1} \sim \mathcal{R}^{-2.8}$$
  
 $\gamma_0 < 2$ 

Expect:  $J_{p,\mathrm{inject}} \propto \mathcal{R}^{-\gamma_0}, \quad \gamma_0 \gtrsim 2$ 

Worry in literature: "if  $t_{esc} \sim R^{-1}$  then..."

$$J_{p,\text{obs}} \sim t_{\text{esc}} \times J_{p,\text{inject}} \propto \mathcal{R}^{-\gamma_0 - 1} \sim \mathcal{R}^{-2.8}$$
  
 $\gamma_0 < 2$ 

Answer: worry is based on constant halo assumption, that may be incorrect.

Steady state scaling is 
$$J_{p,obs} \sim \frac{Q_p \times t_{esc}}{V} \propto \frac{J_{p,inject} \times t_{esc}}{V}$$

V could depend on rigidity: V=V(R)Example: homogeneous thin-disc diffusion,  $V \sim L = L(R)$ 

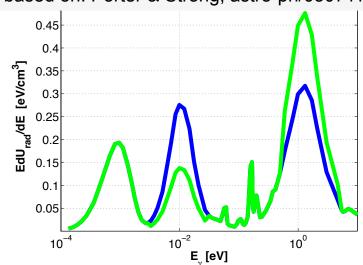
$$t_{\rm esc} \propto \frac{L^2}{D}, \quad X_{\rm esc} \propto \frac{L c}{D} \times X_{\rm disc}$$
  
 $\Rightarrow \quad J_{p,{\rm obs}} \sim X_{\rm esc} \times J_{p,{\rm inject}} \propto \mathcal{R}^{-\gamma_0 - 0.4} \sim \mathcal{R}^{-2.8}$ 

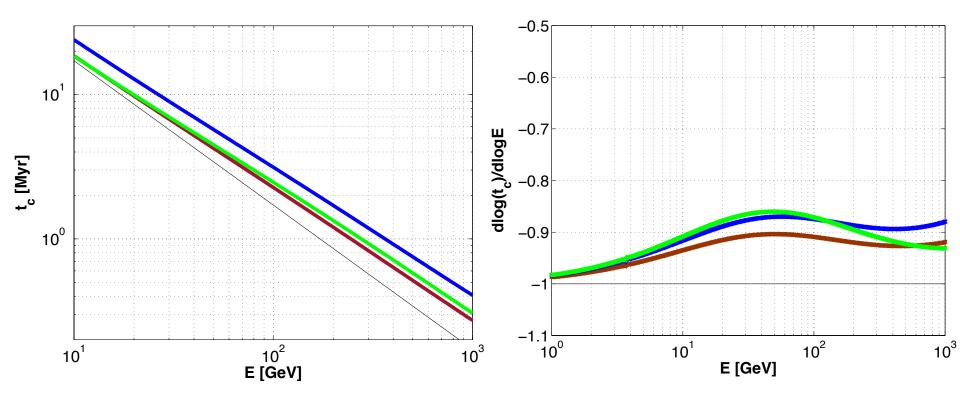
#### What is the cooling time of CR e±?

K-N bump @E~10-100 GeV due to starlight.

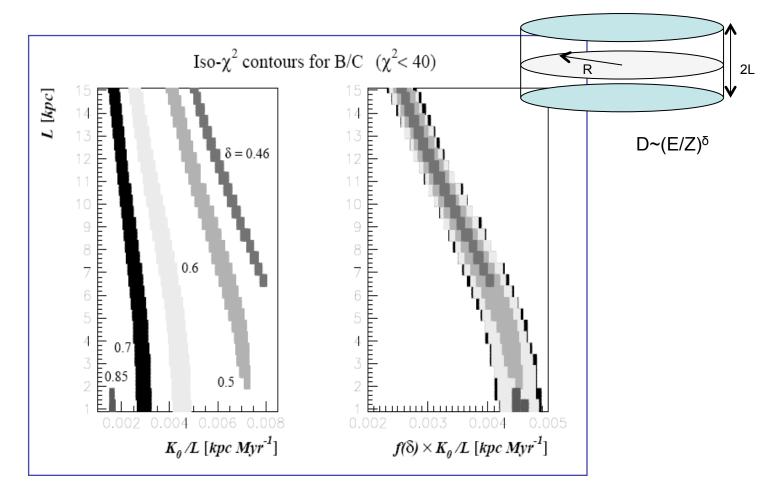
Index ~ 0.8-0.9 t<sub>cool</sub> ~ 1 Myr @ 300 GeV

#### based on: Porter & Strong, astro-ph/0507119



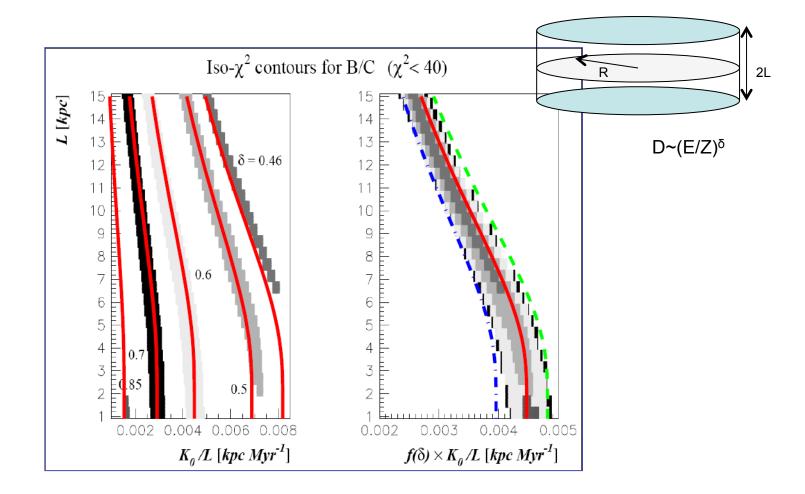


#### Global diffusion model was tuned to fit local stable nuclei



Maurin et al, Astrophys.J.555:585-596,2001

#### Global diffusion model was tuned to fit local stable nuclei

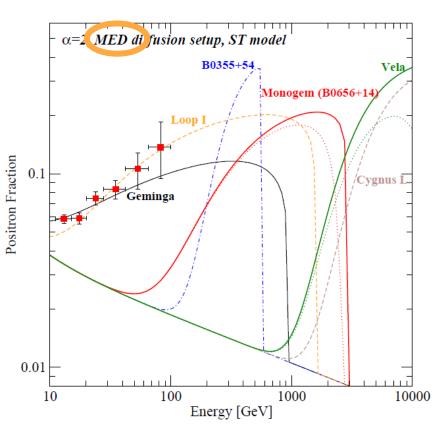


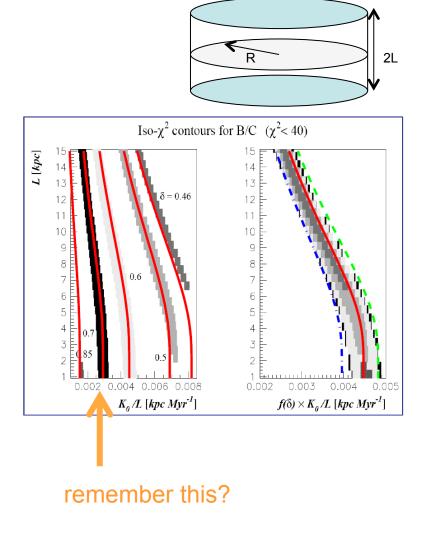
diffusion models fit grammage: 
$$X_{esc} = X_{disc} \frac{Lc}{2D} \frac{2R}{L} \sum_{k=1}^{\infty} J_0 \left[ v_k (r_s/R) \right] \frac{\tanh \left[ v_k (L/R) \right]}{v_k^2 J_1 (v_k)}$$

Katz et al, MNRAS 405 (2010) 1458

Other ideas:

- Local, non steady state sources
- Pulsars





Profumo, Central Eur.J.Phys. 10 (2011) 1-31

2. Propagation time scales: radioactive nuclei

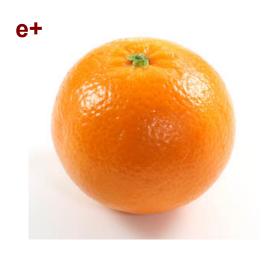
➔ Secondary radioactive nuclei carry time info (like positrons)





reaction	$t_{1/2}$ [Myr]	$\sigma \; [mb]$
${}^{10}_4{ m Be}  ightarrow {}^{10}_5{ m B}$	1.51(0.06)	210
$^{26}_{13}\mathrm{Al}  ightarrow ~^{26}_{12}\mathrm{Mg}$	0.91(0.04)	411
$^{36}_{17}\mathrm{Cl} ightarrow^{36}_{18}\mathrm{Ar}$	0.307(0.002)	516
$^{54}_{25}\mathrm{Mn}$ $ ightarrow$ $^{54}_{26}\mathrm{Fe}$	$0.494(0.006)^*$	685

How to compare radioactive decay of a nucleus, with energy loss of e+?







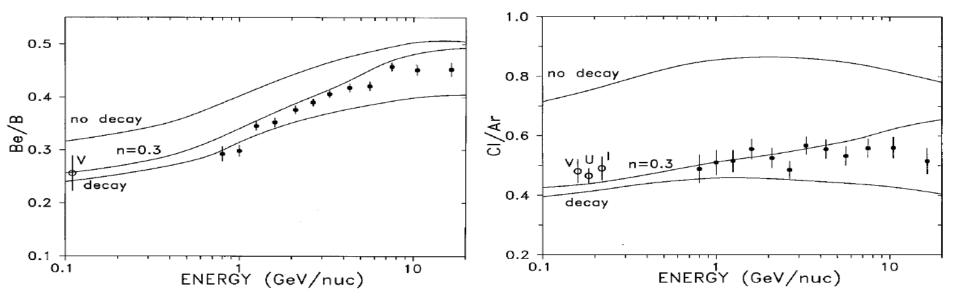
### We'll get there in a few slides.

Radioactive nuclei: Charge ratio

#### A STUDY OF THE SURVIVING FRACTION OF THE COSMIC-RAY RADIOACTIVE DECAY ISOTOPES <sup>10</sup>Be, <sup>26</sup>Al, <sup>36</sup>Cl, and <sup>54</sup>Mn AS A FUNCTION OF ENERGY USING THE CHARGE RATIOS Be/B, Al/Mg, Cl/Ar, AND Mn/Fe MEASURED ON *HEAO-3*

W. R. WEBBER<sup>1</sup> AND A. SOUTOUL Received 1997 November 6; accepted 1998 May 11

(WS98)



Radioactive nuclei: Charge ratio vs. isotopic ratio

Charge ratios

**Isotopic ratios** 

Be/B, Al/Mg, Cl/Ar, Mn/Fe <sup>10</sup>Be/<sup>9</sup>Be, <sup>26</sup>Al/<sup>27</sup>Al, <sup>36</sup>Cl/Cl, <sup>54</sup>Mn/Mn Charge ratios Be/B, Al/Mg, Cl/Ar, Mn/Fe Isotopic ratios <sup>10</sup>Be/<sup>9</sup>Be, <sup>26</sup>Al/<sup>27</sup>Al, <sup>36</sup>Cl/Cl, <sup>54</sup>Mn/Mn

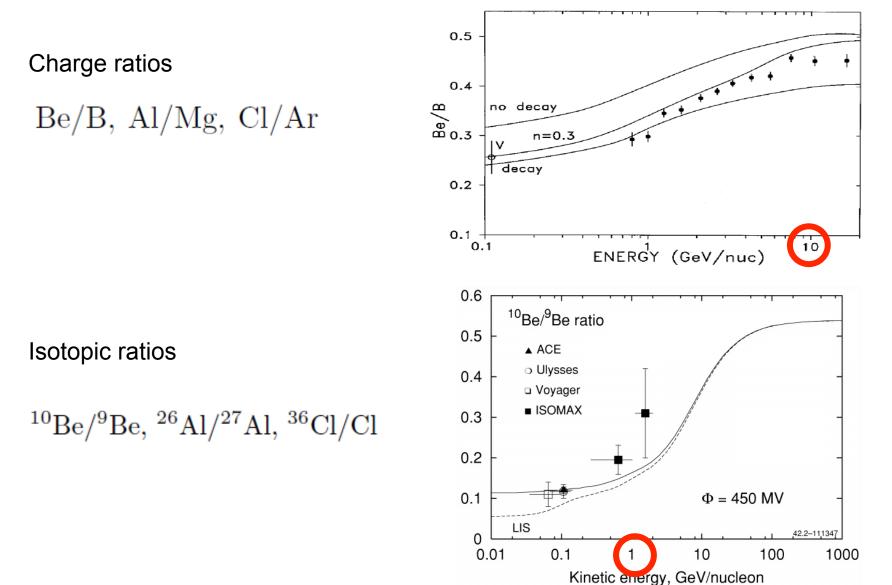
High energy isotopic separation <u>difficult</u>. Need to resolve mass.
 Isotopic ratios were measured only up to ~ 2 GeV/nuc (ISOMAX)

 Charge separation easier. Charge ratios up to ~ 16 GeV/nuc (HEAO3-C2) (AMS-02: Charge ratios to ~ TeV/nuc. Isotopic ratios ~ 10 GeV/nuc )

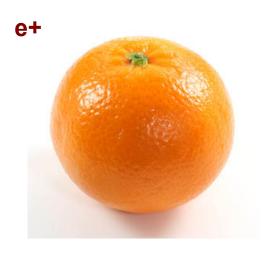
• Benefit: avoid low energy complications; significant range in rigidity

• Drawback: systematic uncertainties (cross sections, primary contamination)

#### Radioactive nuclei: Charge ratio vs. isotopic ratio



How to compare radioactive decay of a nucleus, with energy loss of e+?







Suppression factor due to decay ~ suppression factor due to radiative loss,
 *if compared at rigidity such that cooling time = decay time*

Explain:

$$t_c = \left| \mathcal{R}/\dot{\mathcal{R}} \right| \propto \mathcal{R}^{-\delta_c} \qquad \qquad n_{e^+} \sim \mathcal{R}^{-\gamma}$$



Suppression factor due to decay ~ suppression factor due to radiative loss,
 *if compared at rigidity such that cooling time = decay time*

Explain:

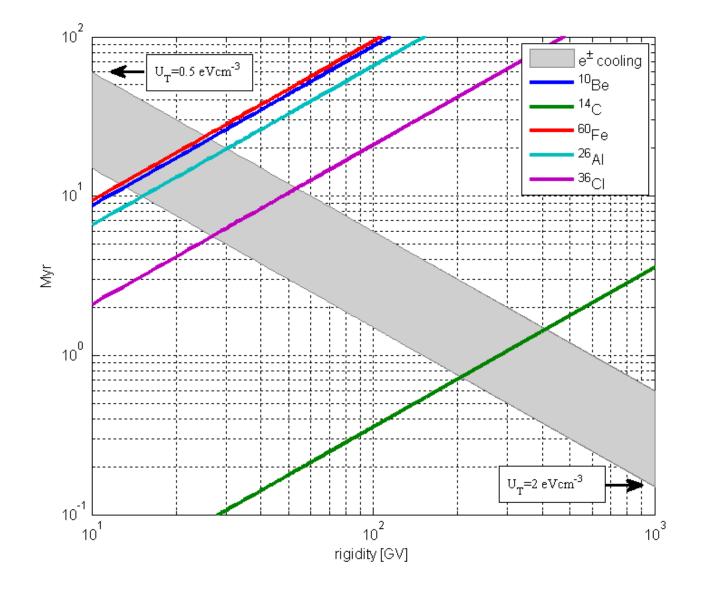
$$t_c = \left| \mathcal{R}/\dot{\mathcal{R}} \right| \propto \mathcal{R}^{-\delta_c} \qquad \qquad n_{e^+} \sim \mathcal{R}^{-\gamma}$$

Consider decay term of nuclei and loss term of e+ in general transport equation.

decay: 
$$\partial_t n_i = -\frac{n_i}{t_i}$$
 loss:  $\partial_t n_{e^+} = \partial_{\mathcal{R}} \left( \dot{\mathcal{R}} n_{e^+} \right) = -\frac{n_{e^+}}{\tilde{t}_c}$   
 $\tilde{t}_c = \frac{t_c}{\gamma - \delta_c - 1}$   
 $\gamma \sim 3 \Rightarrow \tilde{t}_c \approx t_c$ 

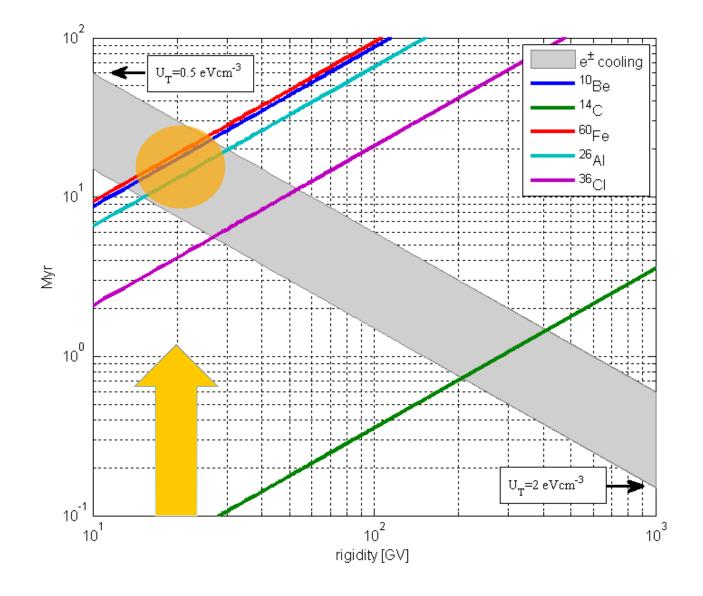
Time scales:

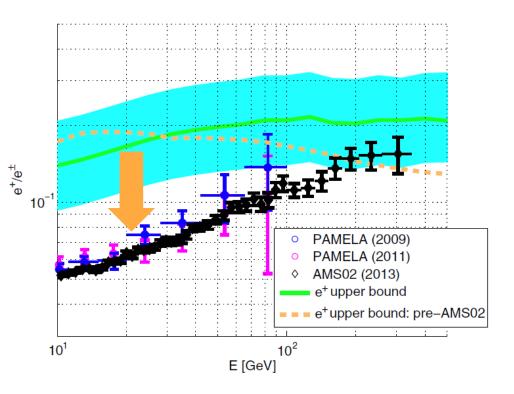
cooling vs decay

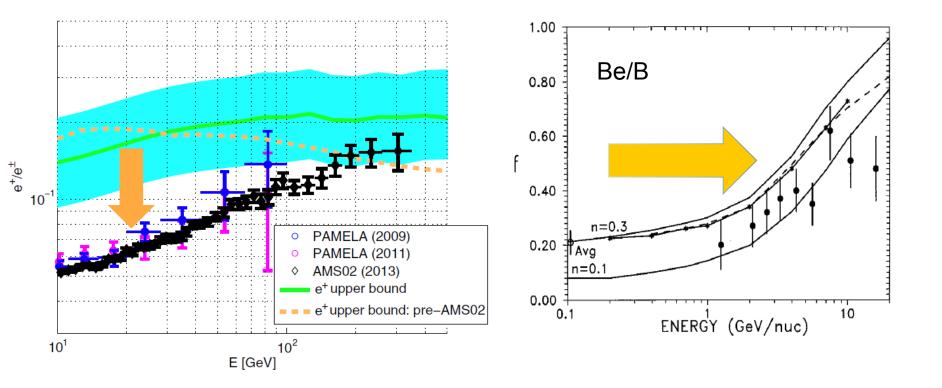


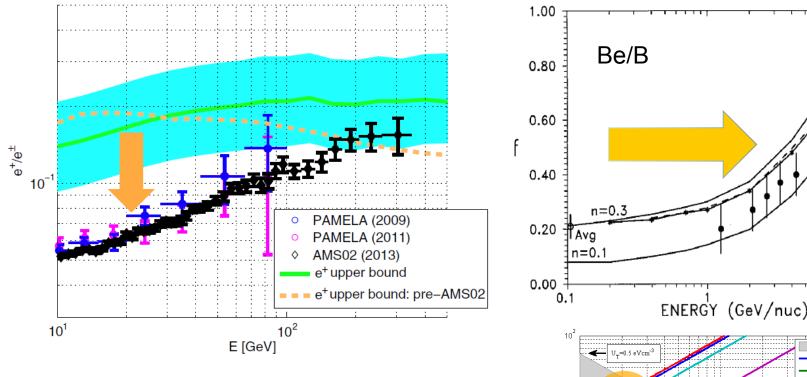
Time scales:

cooling vs decay

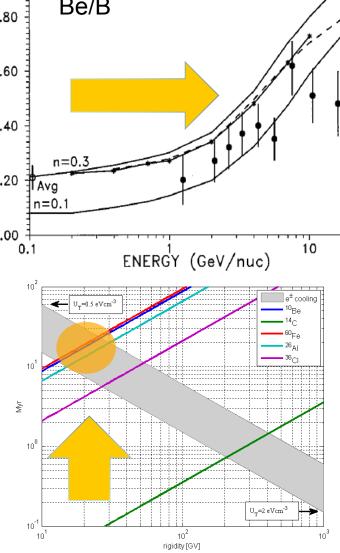








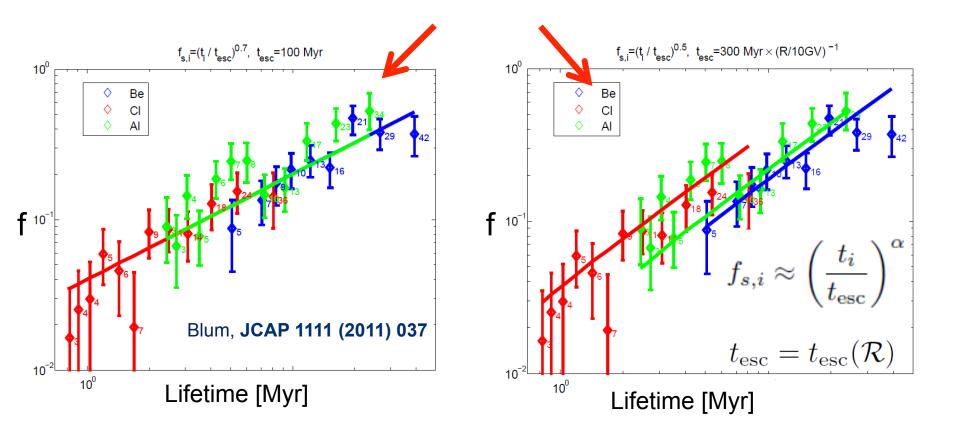
$$\begin{array}{l} f_{s,^{10}\mathrm{Be}}\approx 0.4\\ f_{s,e^+}\approx 0.3 \end{array}$$



Radioactive nuclei: constraints on  $t_{
m esc}$ 

- Cannot (yet) exclude rapidly decreasing escape time
- AMS-02 should do better!

Need to tell between these fits



1. For the first time, limit cosmic ray propagation time @100's GV:

$$t_{
m esc} \left( E/Z = 300 \ {
m GeV} 
ight) \ \lesssim \ 1 \ {
m Myr}$$

Together with B/C and pbar/p data, this *may* suggest that *high energy CRs do not return from* too far above the Galactic gas disc:

$$\langle n_{\rm ISM}(\mathcal{R}) \rangle = \frac{X_{\rm esc}(\mathcal{R})}{c \, m_{\rm ISM} \, t_{\rm esc}(\mathcal{R})} \sim 1/{\rm cm^3 \, @R=300 GV}$$

AMS updates on B/C together w/ p, He, and e+ flux important to check n at yet higher energies.
 ( will we be led to surprisingly large n>>1? )

2. As rigidity R increases, loss suppression does not decrease (*perhaps even gets closer to unity?*),

imply  $t_{esc}(R)/t_{cool}(R) \sim constant$  (*perhaps decreasing?*) with R

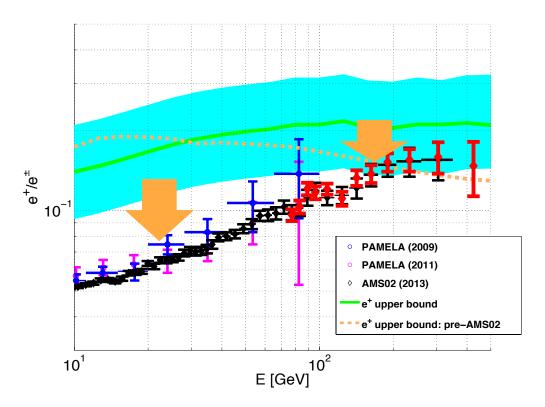
→  $t_{esc}(R)$  decreases faster than  $X_{esc}(R)$ 

could do with e.g.

R-dependent boundary

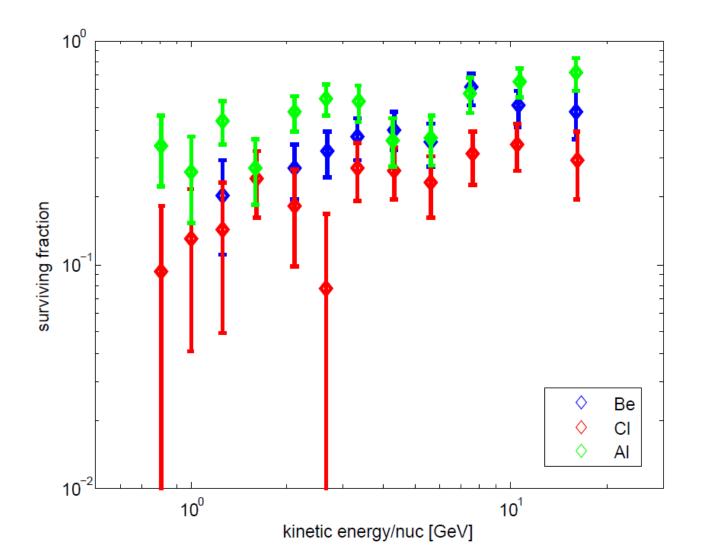
need care w/ e+ production cross section,

as well as consistent B/C, p, He data.



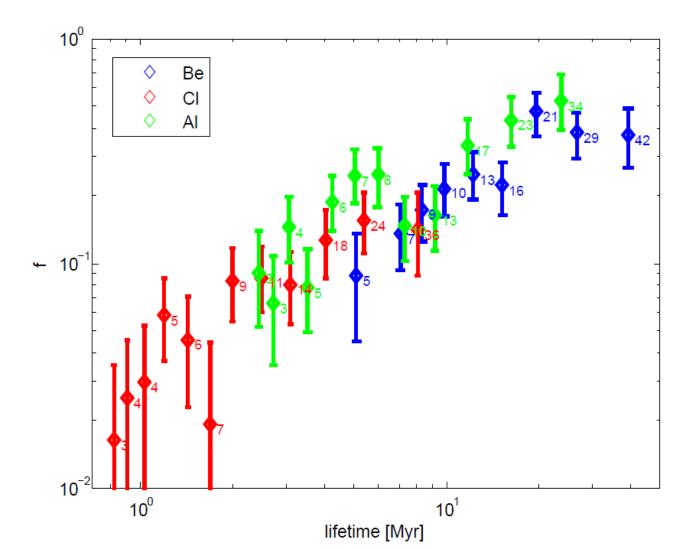
# Radioactive nuclei: data

Surviving fraction vs. energy (WS98)



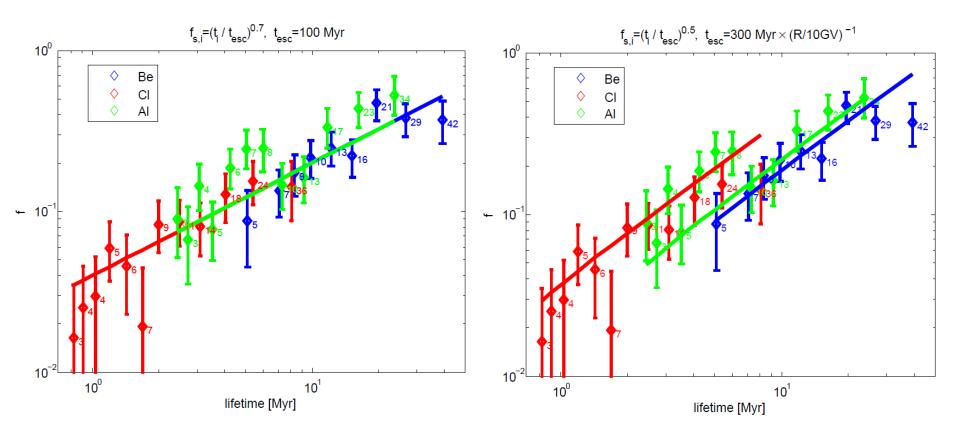
# Radioactive nuclei: data

Suppression factor vs. lifetime

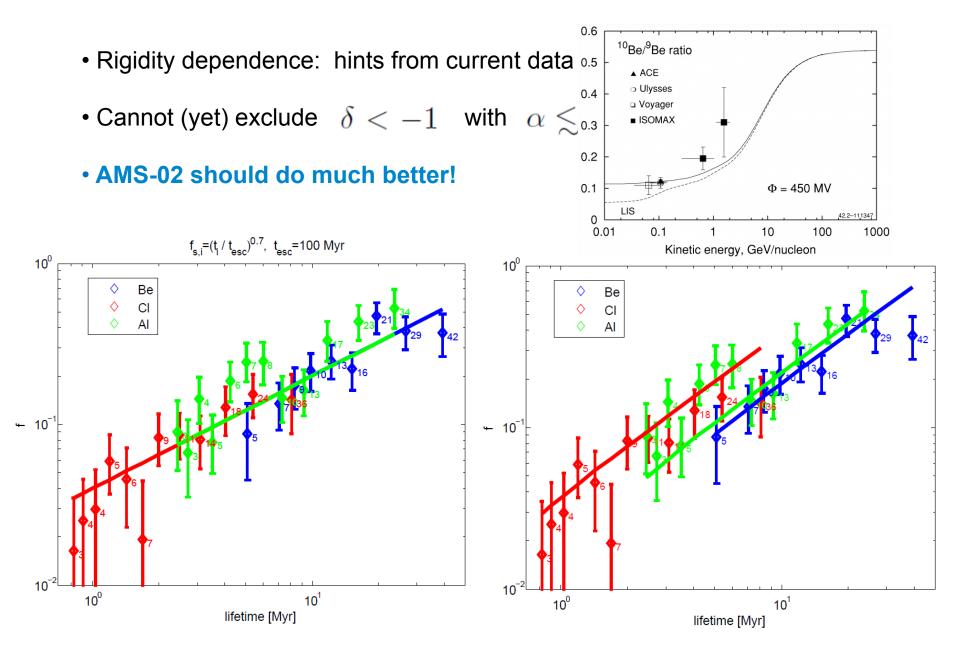


# Radioactive nuclei: constraints on $t_{\rm esc}$

- Rigidity dependence: hints from current data
- Cannot (yet) exclude  $~~\delta < -1~~$  with  $~~lpha \lesssim 0.5~$
- AMS-02 should do much better!



# Radioactive nuclei: constraints on $t_{ m esc}$

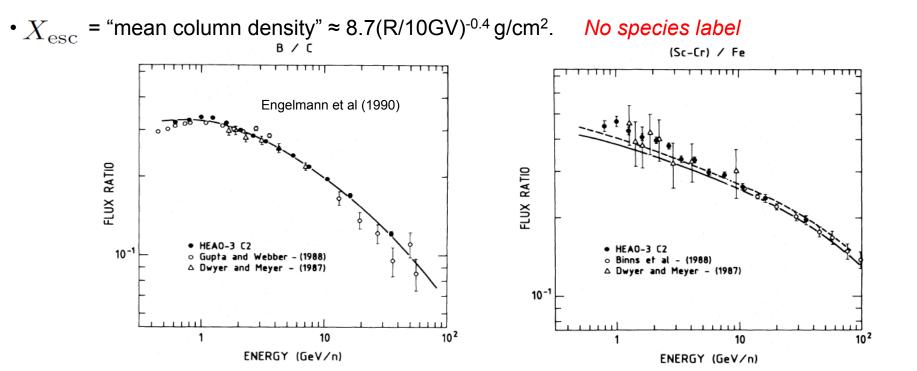


#### Stable secondaries with no energy loss (B, pbar, sub-Fe,...)

• Empirical relation:  $\frac{n_A}{n_B} = \frac{Q_A}{Q_B}$ 

•  $Q_A(\mathcal{R})$  = Local net production per unit column density of target, for species A

$$\frac{n_A(\mathcal{R})}{n_B(\mathcal{R})} = \frac{Q_A(\mathcal{R})}{Q_B(\mathcal{R})} \quad \text{equivalent to:} \quad n_A(\mathcal{R}) = Q_A(\mathcal{R}) \times X_{\text{esc}}(\mathcal{R})$$

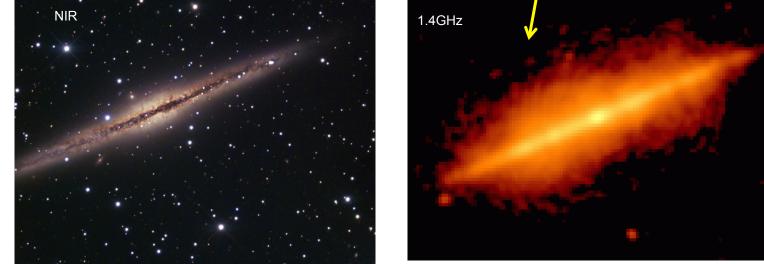


Theoretically, this is a natural relation.

Guaranteed to apply if the *composition* of CRs and ISM is uniform (well mixed) in the region of the Galaxy where spallation happens

$$\frac{n_A(\mathcal{R})}{n_B(\mathcal{R})} = \frac{Q_A(\mathcal{R})}{Q_B(\mathcal{R})} \quad \text{equivalent to:} \quad n_A(\mathcal{R}) = Q_A(\mathcal{R}) \times X_{\text{esc}}(\mathcal{R})$$

$$\nu \approx 0.29 \times \frac{3eB}{4\pi m_e c} \left(\frac{\epsilon}{m_e c^2}\right)^2 \approx 1 \text{ GHz} \left(\frac{B}{1 \ \mu\text{G}}\right) \left(\frac{\epsilon}{15 \text{ GeV}}\right)^2$$
NGC 891

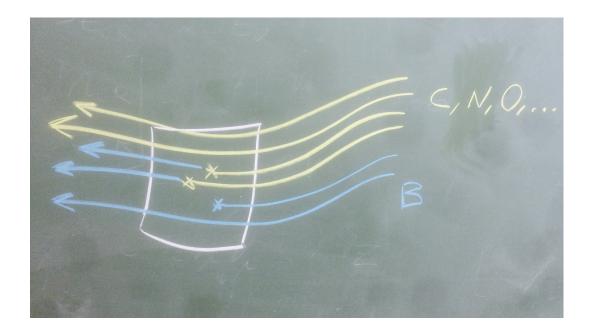




$$Q_B(\mathcal{R}, \vec{r}, t) = \sum_{i=C, N, O, \dots} \left(\frac{\sigma_{i \to B}}{\bar{m}}\right) n_i(\mathcal{R}, \vec{r}, t) - \left(\frac{\sigma_B}{\bar{m}}\right) n_B(\mathcal{R}, \vec{r}, t)$$

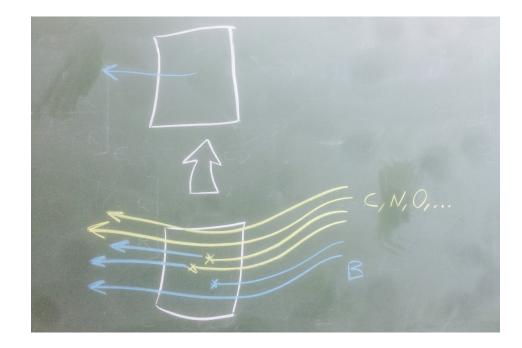


$$Q_B(\mathcal{R}, \vec{r}, t) = \sum_{i=C, N, O, \dots} \left(\frac{\sigma_{i \to B}}{\bar{m}}\right) n_i(\mathcal{R}, \vec{r}, t) - \left(\frac{\sigma_B}{\bar{m}}\right) n_B(\mathcal{R}, \vec{r}, t)$$





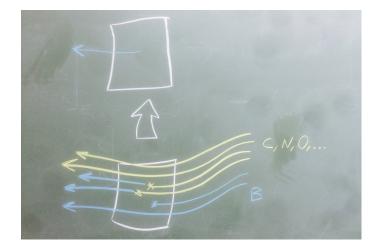
$$Q_B(\mathcal{R}, \vec{r}, t) = \sum_{i=C, N, O, \dots} \left(\frac{\sigma_{i \to B}}{\bar{m}}\right) n_i(\mathcal{R}, \vec{r}, t) - \left(\frac{\sigma_B}{\bar{m}}\right) n_B(\mathcal{R}, \vec{r}, t)$$





$$Q_B(\mathcal{R}, \vec{r}, t) = \sum_{i=C, N, O, \dots} \left(\frac{\sigma_{i \to B}}{\bar{m}}\right) n_i(\mathcal{R}, \vec{r}, t) - \left(\frac{\sigma_B}{\bar{m}}\right) n_B(\mathcal{R}, \vec{r}, t)$$

High-energy fragmentation CH  $\rightarrow$  BX: B inherits Lorentz factor  $\Gamma$  of parent C So B inherits magnetic rigidity,  $R_B \approx R_C$   $R = \frac{p}{Z} = \frac{\Gamma A m_p}{Z} \approx 2\Gamma m_p$ 

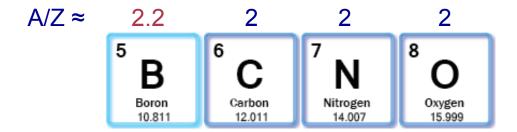




$$Q_B(\mathcal{R}, \vec{r}, t) = \sum_{i=C, N, O, \dots} \left(\frac{\sigma_{i \to B}}{\bar{m}}\right) n_i(\mathcal{R}, \vec{r}, t) - \left(\frac{\sigma_B}{\bar{m}}\right) n_B(\mathcal{R}, \vec{r}, t)$$

High-energy fragmentation CH  $\rightarrow$  BX: B inherits Lorentz factor  $\Gamma$  of parent C So B inherits magnetic rigidity,  $R_B \approx R_C$   $R = \frac{p}{Z} = \frac{\Gamma A m_p}{Z} \approx 2\Gamma m_p$ 

 $CNO \rightarrow B$ : accurate to O(10%)...





$$Q_B(\mathcal{R}, \vec{r}, t) = \sum_{i=C, N, O, \dots} \left(\frac{\sigma_i \to B}{\bar{m}}\right) n_i(\mathcal{R}, \vec{r}, t) - \left(\frac{\sigma_B}{\bar{m}}\right) n_B(\mathcal{R}, \vec{r}, t)$$

In general:

$$n_B(\mathcal{R}, \vec{r}_{\odot}, t_{\odot}) = \int d^3r \int dt \, c \, \rho_{ISM}(\vec{r}, t) \, Q_B(\mathcal{R}, \vec{r}, t) \, P\left(\mathcal{R}; \{\vec{r}, t\}, \{\vec{r}_{\odot}, t_{\odot}\}\right)$$



$$Q_B(\mathcal{R}, \vec{r}, t) = \sum_{i=C, N, O, \dots} \left(\frac{\sigma_{i \to B}}{\bar{m}}\right) n_i(\mathcal{R}, \vec{r}, t) - \left(\frac{\sigma_B}{\bar{m}}\right) n_B(\mathcal{R}, \vec{r}, t)$$

In general:

$$\begin{split} n_B(\mathcal{R}, \vec{r}_{\odot}, t_{\odot}) &= \int d^3r \int dt \, c \, \rho_{ISM}(\vec{r}, t) \, Q_B(\mathcal{R}, \vec{r}, t) \, P\left(\mathcal{R}; \{\vec{r}, t\}, \{\vec{r}_{\odot}, t_{\odot}\}\right) \\ &= Q_B(\mathcal{R}, \vec{r}_{\odot}, t_{\odot}) \, \int d^3r \int dt \, c \, \rho_{ISM}(\vec{r}, t) \, \frac{n_C\left(\mathcal{R}, \vec{r}, t\right)}{n_C\left(\mathcal{R}, \vec{r}_{\odot}, t_{\odot}\right)} \, P\left(\mathcal{R}; \{\vec{r}, t\}, \{\vec{r}_{\odot}, t_{\odot}\}\right) \, F_B \end{split}$$

$$F_B = \frac{\sum_{i=C,N,O,\dots} \left(\frac{\sigma_{i\to B}}{\bar{m}}\right) \frac{n_i(\mathcal{R},\vec{r},t)}{n_C(\mathcal{R},\vec{r},t)} - \left(\frac{\sigma_B}{\bar{m}}\right) \frac{n_B(\mathcal{R},\vec{r},t)}{n_C(\mathcal{R},\vec{r},t)}}{\sum_{i=C,N,O,\dots} \left(\frac{\sigma_{i\to B}}{\bar{m}}\right) \frac{n_i(\mathcal{R},\vec{r}_{\odot},t_{\odot})}{n_C(\mathcal{R},\vec{r}_{\odot},t_{\odot})} - \left(\frac{\sigma_B}{\bar{m}}\right) \frac{n_B(\mathcal{R},\vec{r}_{\odot},t_{\odot})}{n_C(\mathcal{R},\vec{r}_{\odot},t_{\odot})}}$$



$$Q_B(\mathcal{R}, \vec{r}, t) = \sum_{i=C, N, O, \dots} \left(\frac{\sigma_i \to B}{\bar{m}}\right) n_i(\mathcal{R}, \vec{r}, t) - \left(\frac{\sigma_B}{\bar{m}}\right) n_B(\mathcal{R}, \vec{r}, t)$$

In general:

$$n_B(\mathcal{R}, \vec{r}_{\odot}, t_{\odot}) = \int d^3r \int dt \, c \, \rho_{ISM}(\vec{r}, t) \, Q_B(\mathcal{R}, \vec{r}, t) \, P\left(\mathcal{R}; \{\vec{r}, t\}, \{\vec{r}_{\odot}, t_{\odot}\}\right)$$
$$= Q_B(\mathcal{R}, \vec{r}_{\odot}, t_{\odot}) \, \int d^3r \int dt \, c \, \rho_{ISM}(\vec{r}, t) \, \frac{n_C\left(\mathcal{R}, \vec{r}, t\right)}{n_C\left(\mathcal{R}, \vec{r}_{\odot}, t_{\odot}\right)} \, P\left(\mathcal{R}; \{\vec{r}, t\}, \{\vec{r}_{\odot}, t_{\odot}\}\right) \, F_B$$

Uniform *composition:* 

 $\frac{n_i(\mathcal{R}, \vec{r}, t)}{n_j(\mathcal{R}, \vec{r}, t)} = f_{ij}(\mathcal{R}) \qquad \text{independent of r,t}$ 

$$F_B = \frac{\sum_{i=C,N,O,\dots} \left(\frac{\sigma_{i\to B}}{\bar{m}}\right) \frac{n_i(\mathcal{R},\vec{r},t)}{n_C(\mathcal{R},\vec{r},t)} - \left(\frac{\sigma_B}{\bar{m}}\right) \frac{n_B(\mathcal{R},\vec{r},t)}{n_C(\mathcal{R},\vec{r},t)}}{\sum_{i=C,N,O,\dots} \left(\frac{\sigma_{i\to B}}{\bar{m}}\right) \frac{n_i(\mathcal{R},\vec{r}_{\odot},t_{\odot})}{n_C(\mathcal{R},\vec{r}_{\odot},t_{\odot})} - \left(\frac{\sigma_B}{\bar{m}}\right) \frac{n_B(\mathcal{R},\vec{r}_{\odot},t_{\odot})}{n_C(\mathcal{R},\vec{r}_{\odot},t_{\odot})}} \approx 1$$



$$Q_B(\mathcal{R}, \vec{r}, t) = \sum_{i=C, N, O, \dots} \left(\frac{\sigma_i \to B}{\bar{m}}\right) n_i(\mathcal{R}, \vec{r}, t) - \left(\frac{\sigma_B}{\bar{m}}\right) n_B(\mathcal{R}, \vec{r}, t)$$

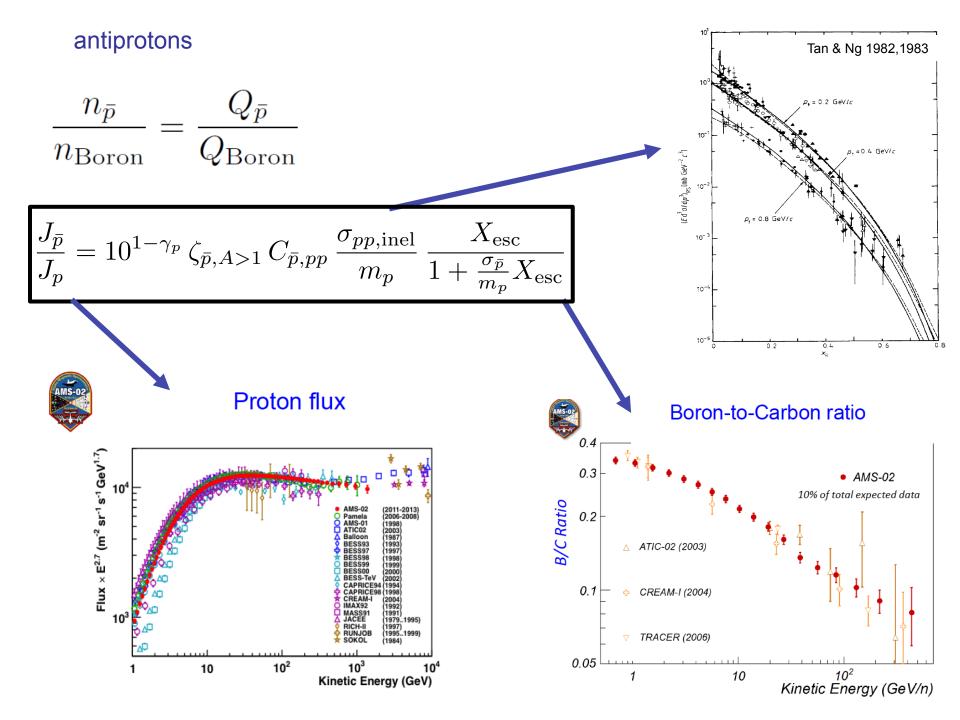
In general:

$$n_B(\mathcal{R}, \vec{r}_{\odot}, t_{\odot}) = \int d^3r \int dt \, c \, \rho_{ISM}(\vec{r}, t) \, Q_B(\mathcal{R}, \vec{r}, t) \, P\left(\mathcal{R}; \{\vec{r}, t\}, \{\vec{r}_{\odot}, t_{\odot}\}\right)$$
$$= Q_B(\mathcal{R}, \vec{r}_{\odot}, t_{\odot}) \, \int d^3r \int dt \, c \, \rho_{ISM}(\vec{r}, t) \, \frac{n_C\left(\mathcal{R}, \vec{r}, t\right)}{n_C\left(\mathcal{R}, \vec{r}_{\odot}, t_{\odot}\right)} \, P\left(\mathcal{R}; \{\vec{r}, t\}, \{\vec{r}_{\odot}, t_{\odot}\}\right) \, F_B$$

Uniform *composition* 

$$n_B(\mathcal{R}, \vec{r}_{\odot}, t_{\odot}) \approx Q_B(\mathcal{R}) X_{\rm esc}(\mathcal{R})$$

$$X_{\rm esc} = \int d^3r \int dt \, c \, \rho_{ISM}(\vec{r}, t) \, \frac{n_C \left(\mathcal{R}, \vec{r}, t\right)}{n_C \left(\mathcal{R}, \vec{r}_{\odot}, t_{\odot}\right)} \, P\left(\mathcal{R}; \{\vec{r}, t\}, \{\vec{r}_{\odot}, t_{\odot}\}\right)$$



## Ginzburg & Ptuskin, Rev.Mod.Phys. 48 (1976) 161-189

## On the origin of cosmic rays: Some problems in highenergy astrophysics\*

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This paper reviews the present state of the problem of the origin of cosmic rays. Primary attention is paid to galactic diffusion models with a halo, and questions of cosmic-ray chemical composition, electron component, and synchrotron galactic radioemission. The authors' conclusion is that models with a large halo with a characteristic cosmic-ray age  $T_{\rm cr} \sim 10^8$  years are confirmed by radio data, and at least do not contradict the information on cosmic-ray chemical composition. The paper also deals with the problems of anisotropy, plasma phenomena in cosmic rays, and the prospects of gamma-ray astronomy.

## Ginzburg & Ptuskin, Rev.Mod.Phys. 48 (**1976**) 161-189

## On the origin of cosmic rays: Some problems in highenergy astrophysics\*

We should note here that the applicability of the diffusion approximations (2.8)-(2.9) to cosmic-ray propagation in the magnetic fields is not at all obvious. For this approximation to be valid it is not enough that the field have a strongly pronounced irregular random component since in this case there also exists a strong tendency for particle propagation along the lines of force of the magnetic field, even if they are rather tangled. But in the

> Galaxy, for example, differential rotation and the motion of gas clouds and spiral arms cause a constant mixing of the lines of force. At the same time we are usually interested not only in a picture averaged over rather large space regions (say, regions of tens and hundreds of parsecs) but also in a picture which is extended in time. To estimate average cosmic-ray gradients and their lifetime  $T_{\rm cr}$  in the Galaxy it is in fact sufficient to know the concentration  $N_i$  averaged for the time  $t \ll T_{\rm cr}$  $\sim 10^6-10^8$  yr, which means that the time of averaging may well be  $10^5$  yr.