

# Robust Recovery of PMU Signals under Corruption: Approaches and Guarantees



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CPS: Small: Fusion of Sensory Data and Expansivity of System Dynamics for Detection and Separation of Signature Anomaly in Energy CPS Wide-Area Monitoring and Control

[https://www.nsf.gov/awardsearch/showAward?AWD\\_ID=1739206](https://www.nsf.gov/awardsearch/showAward?AWD_ID=1739206)



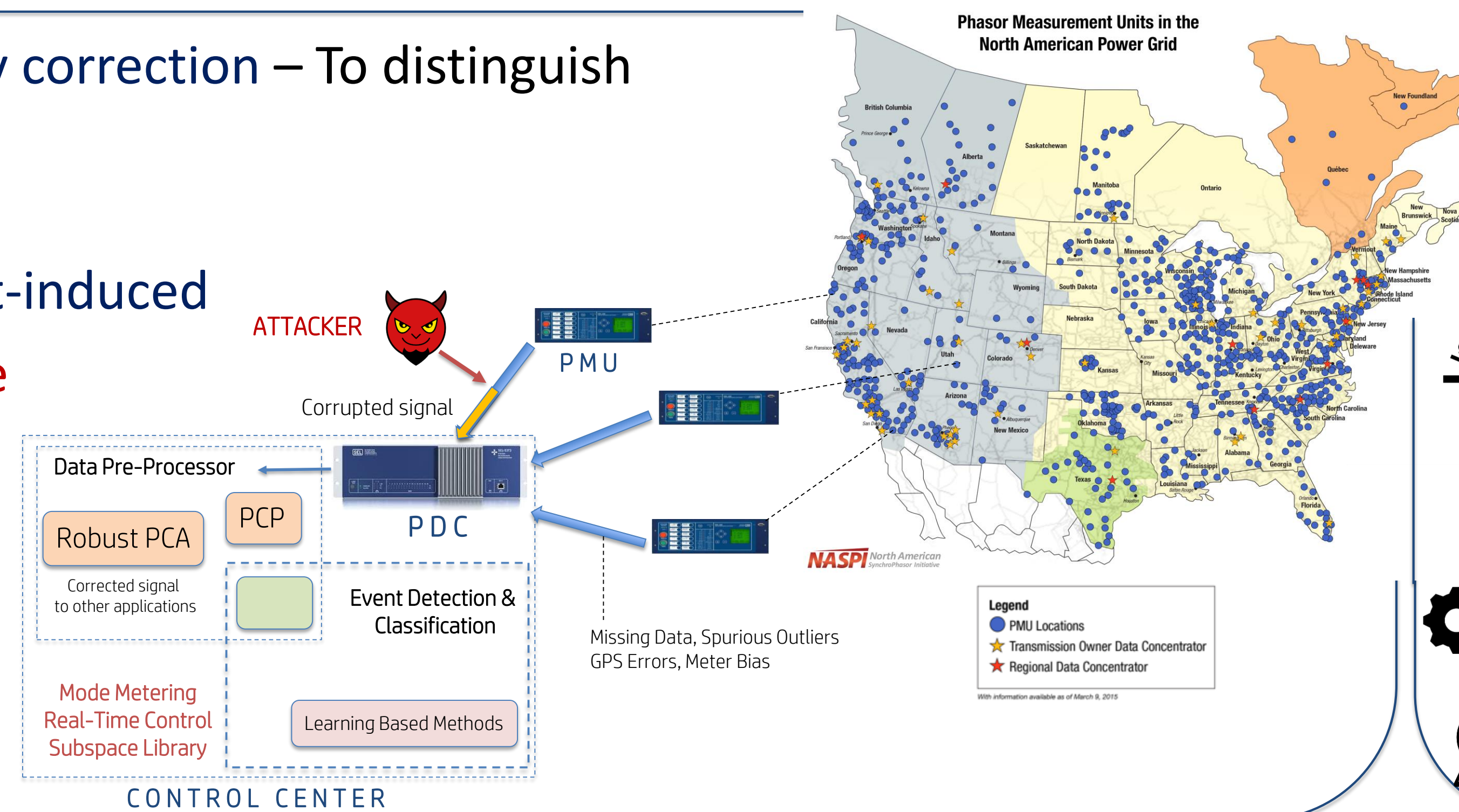
**Spurious or maliciously injected outliers** in PMU data – Need for anomaly correction – To distinguish between event-induced outliers and bad data – recover clean PMU data



A **moving window Kernel PCA**-based metric proposed for detecting event-induced outliers in presence of corruptions in PMU data -- A data-driven **recursive Bayesian framework** adopted for selecting the most appropriate subspace from the library for use in post-event signal recovery



Proposed approaches part of **RPCA-based Robust Anomaly Correction** and PMU Data Recovery scheme

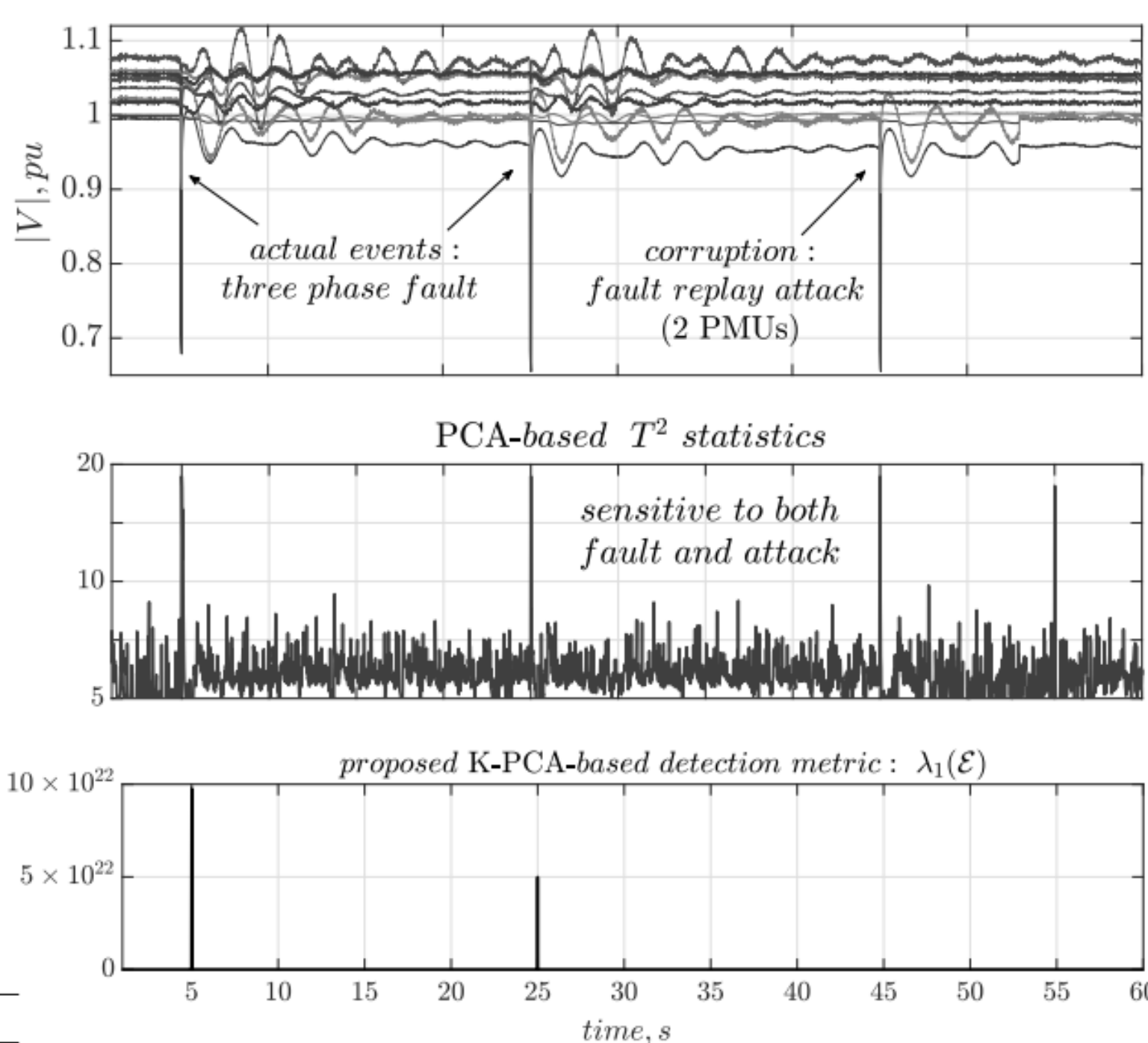
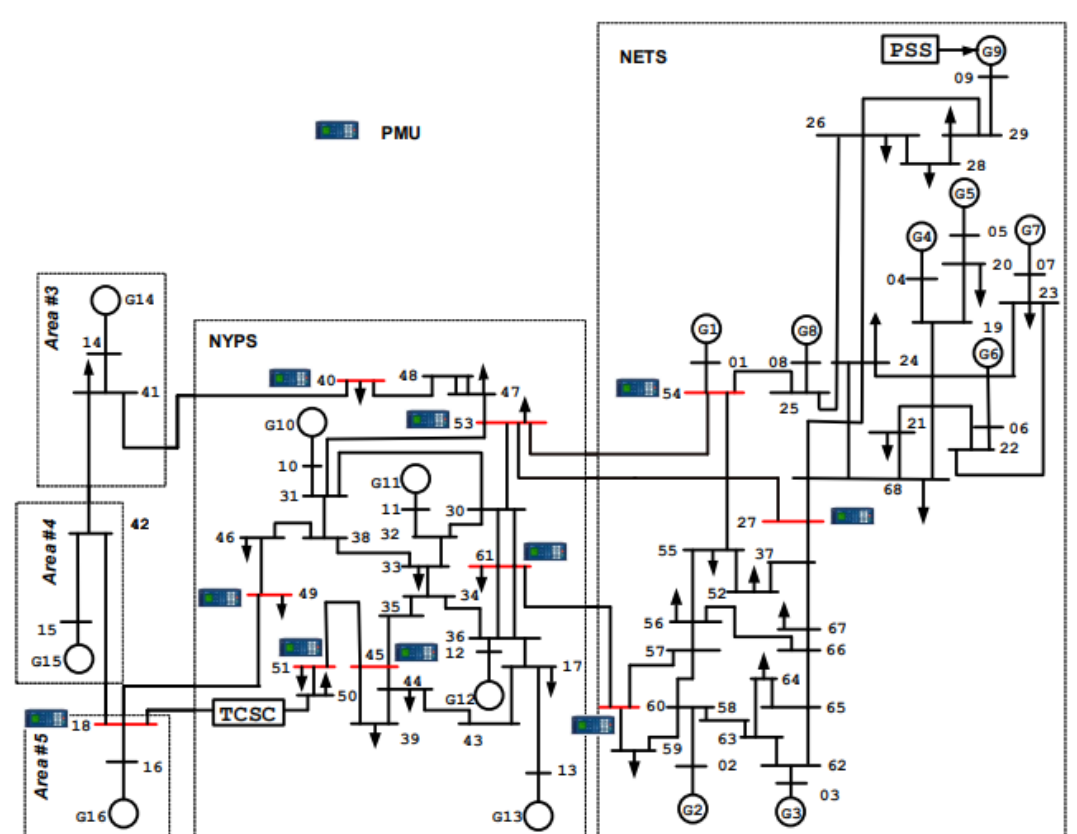


## SCIENTIFIC Impact

- Fusion of sensory data with the dynamic properties of the physical system
- Fundamental insight into the coupling between the cyber and the physical layer of Energy CPS
- Better visualization of dynamic events
- Real time monitoring and event detection
- Quantify the effect of PMU signature anomalies on Principal Components in the higher versus lower dimensional subspaces
- Can potentially benefit a wide range of CPS- process control, oil and gas, energy, robots and future transportation systems employing autonomous vehicles
- Protect critical infrastructures from cyber-attacks and facilitate improved system diagnosis, lower downtime, better service, and higher resiliency

## CASE STUDIES

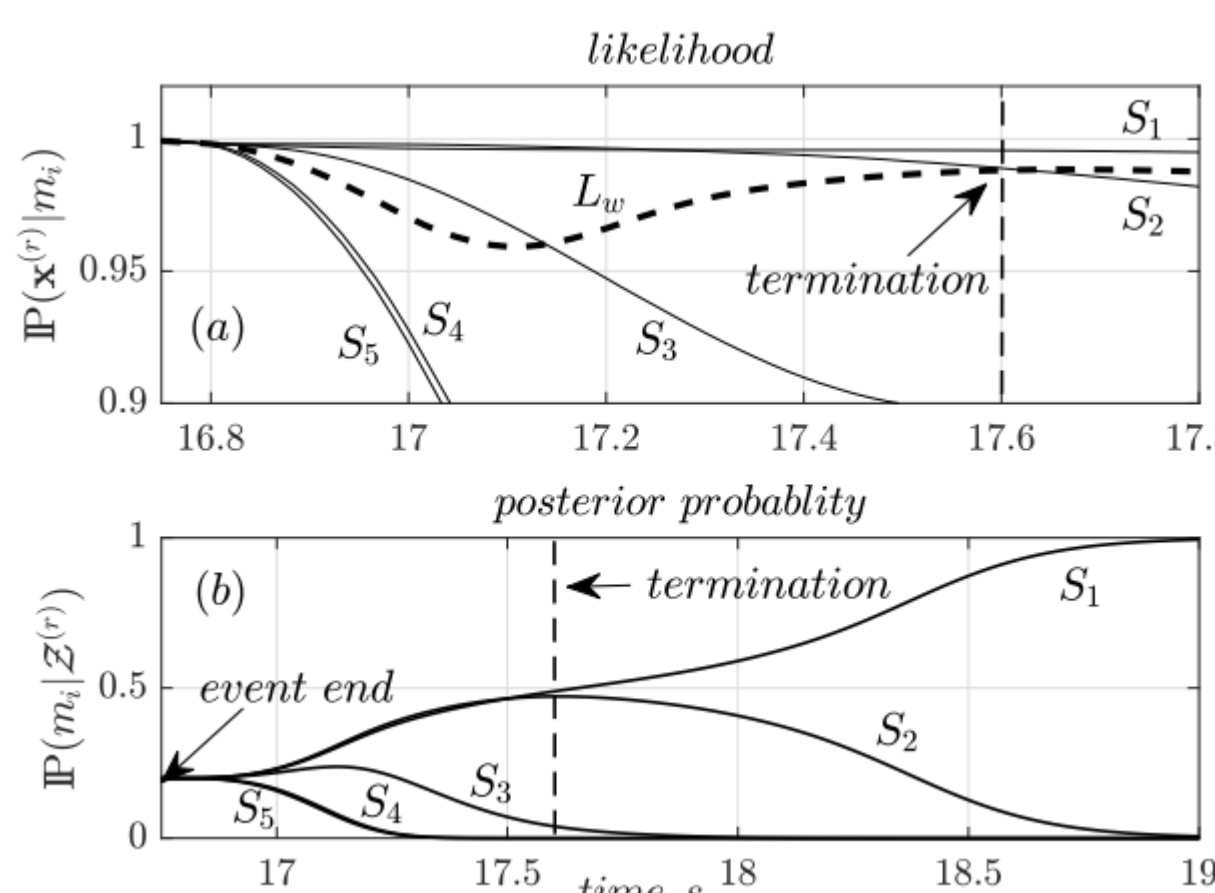
### IEEE 5-area 16-machine NY-NE Test System



### Subspace Library

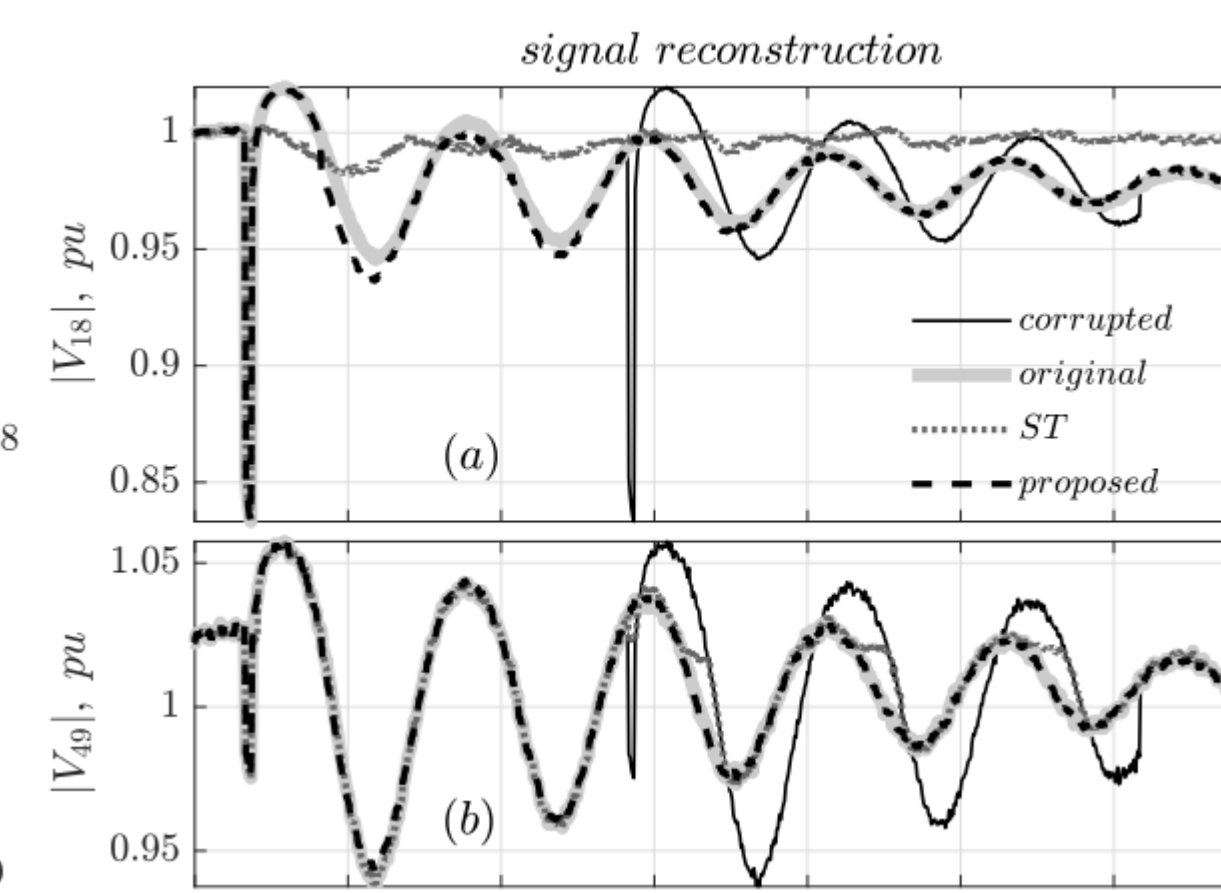
$S_1$	$S_2$	$S_3$	$S_4$	$S_5$
18 - 42 out <sup>1</sup>	18 - 49 out <sup>1</sup>	40 - 41 out <sup>1</sup>	53 - 54 out <sup>1</sup>	Nominal Condition

K-PCA-based detection of event-induced outlier: Data recovery is suspended in event window



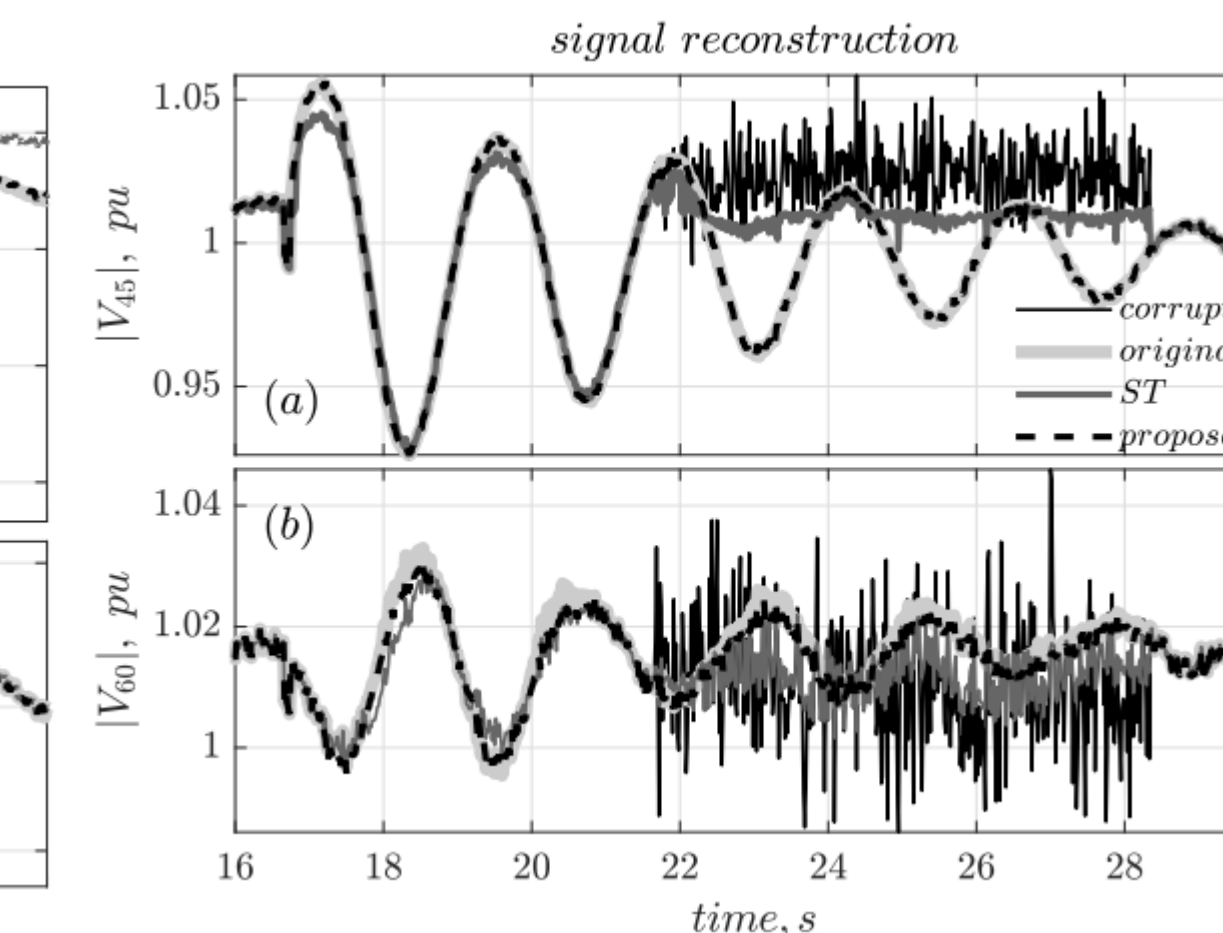
**Recursive Bayesian Approach for Subspace Selection:** Likelihood and Posterior probabilities of a subspace being the true subspace given a set of PMU observations

Selection accelerated with a suitable termination criteria

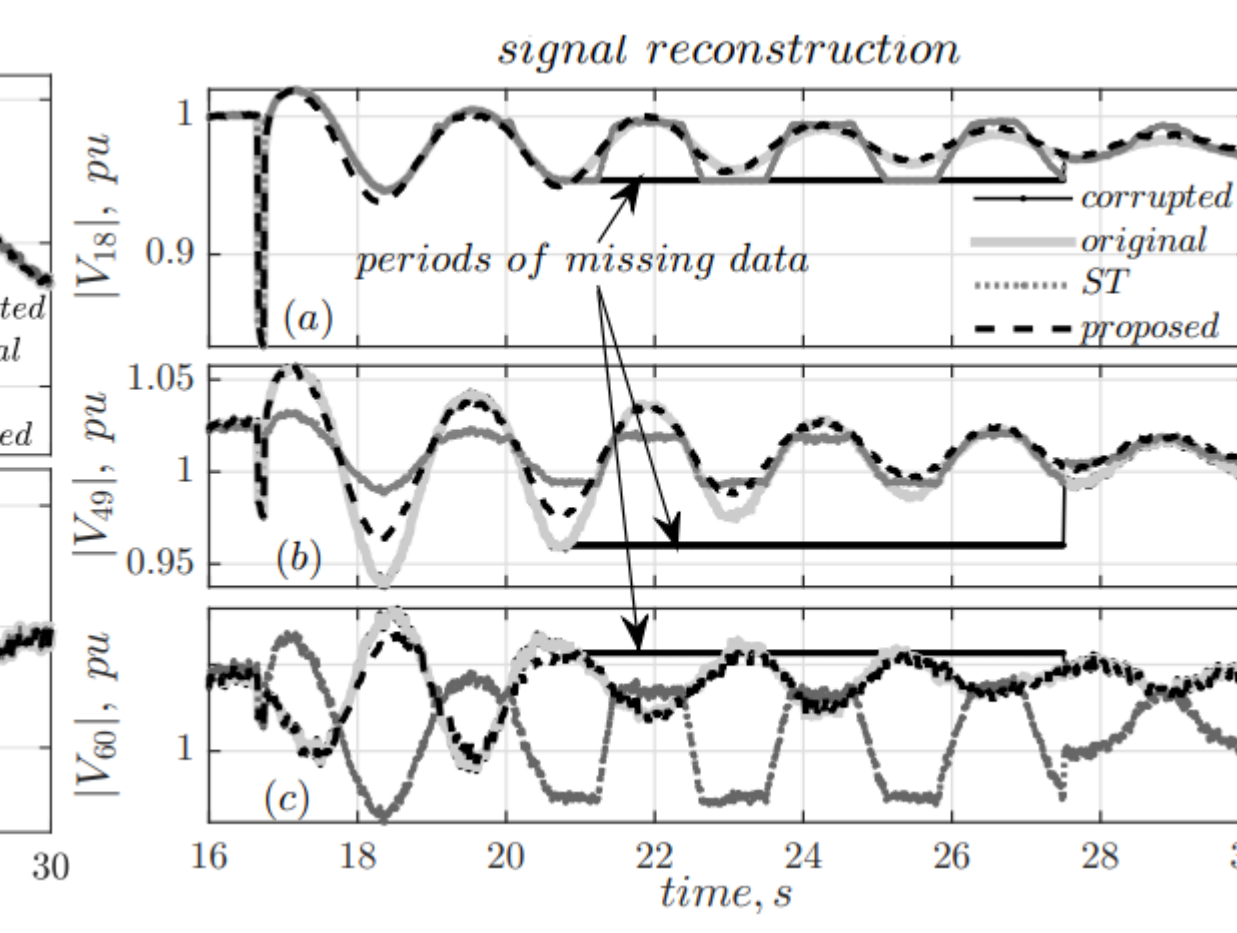


**Signal recovery under fault resembling attack** in 2 PMUs – also shown, no recovery during actual event (fault)

Subspace selection is accurate, therefore, reconstruction quality is good

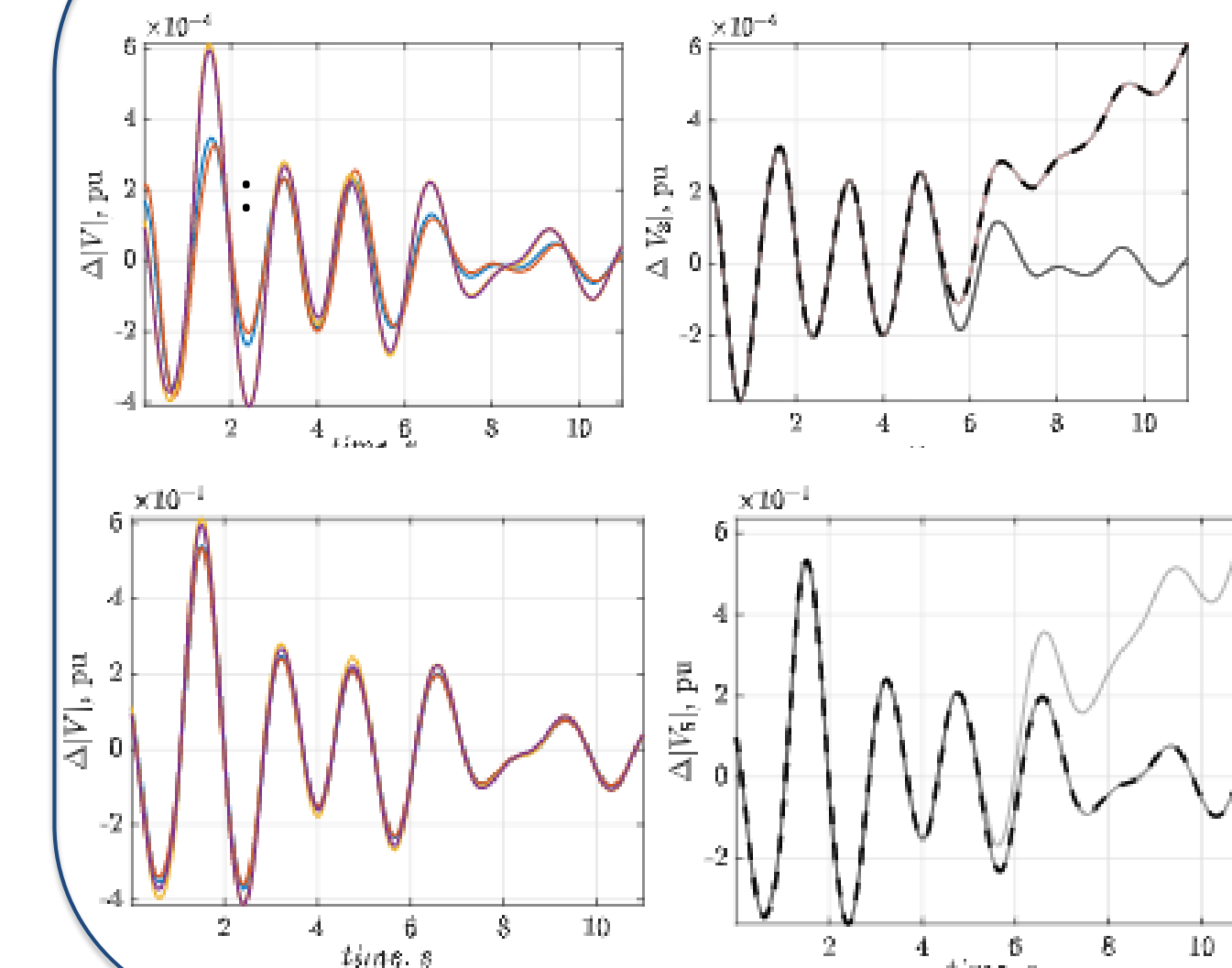


**Signal recovery under noise injection attack** in 2 PMUs



**Signal recovery under missing data attack** in 3 PMUs

**Guarantees for Data Recovery:** Signal grouping to ensure that for a given set Restricted Isometry Constant is below a threshold



**Signal set I : poor RIC** -- recovery not guaranteed -- shows incorrect reconstruction

**Signal set II : RIC below threshold** -- recovery guaranteed -- shows correct reconstruction

## Broader Impact on EDUCATION & OUTREACH



To include the outcome of our research as a module of one course **EE 488: Power Systems Analysis** at Penn State through Problem-based Learning (PBL).



To integrate the proposed research into **iTech: Summer Technology Camp for Teens** - a free week-long interactive day camp, coordinated through Penn State's College of Information Sciences and Technology (IST), designed to introduce high school students (9th-12th grades) to information technology.

## Publications from this Award

- Mahapatra, Kaveri and Chaudhuri, Nilanjan Ray. "Malicious Corruption-Resilient Wide-Area Oscillation Monitoring using Principal Component Pursuit," *IEEE Transactions on Smart Grid*, 2018. doi:10.1109/TSG.2017.2778054
- Mahapatra, Kaveri and Chaudhuri, Nilanjan Ray and Kavasseri, Rajesh G. and Brahma, Sukumar M.. "Online Analytical Characterization of Outliers in Synchronphasor Measurements: A Singular Value Perturbation Viewpoint," *IEEE Transactions on Power Systems*, v.33, 2018. doi:10.1109/TPWRS.2017.2771782
- Chatterjee, Kaustav and Mahapatra, Kaveri and Chaudhuri, Nilanjan Ray. "Robust Recovery of PMU Measurements with Outlier Characterization and Stochastic Subspace Selection." Submitted to *IEEE Transactions on Smart Grid*
- Chatterjee, Kaustav and Chaudhuri, Nilanjan Ray. "Corruption-Resilient Detection of Event-Induced Outliers in PMU Data: A Kernel PCA Approach", *IEEE Power and Energy Society General Meeting*, Atlanta, GA, USA, Aug 2019.
- Chatterjee, Kaustav and Chaudhuri, Nilanjan Ray. "Grouping PMU Signals with Guaranteed Recovery under Corruption: Insights and Recommendation", Submitted to *IEEE Power and Energy Society General Meeting*, Montreal, Canada, Aug 2020.

