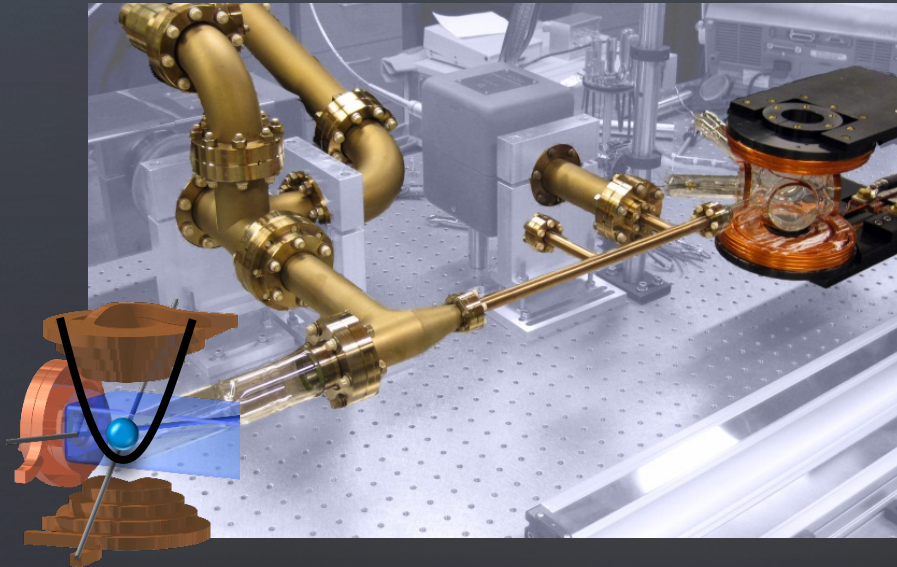


# Disordered Quantum Gases

{ What is the nature of disordered,  
{ strongly interacting quantum matter?



Brian DeMarco  
University of Illinois



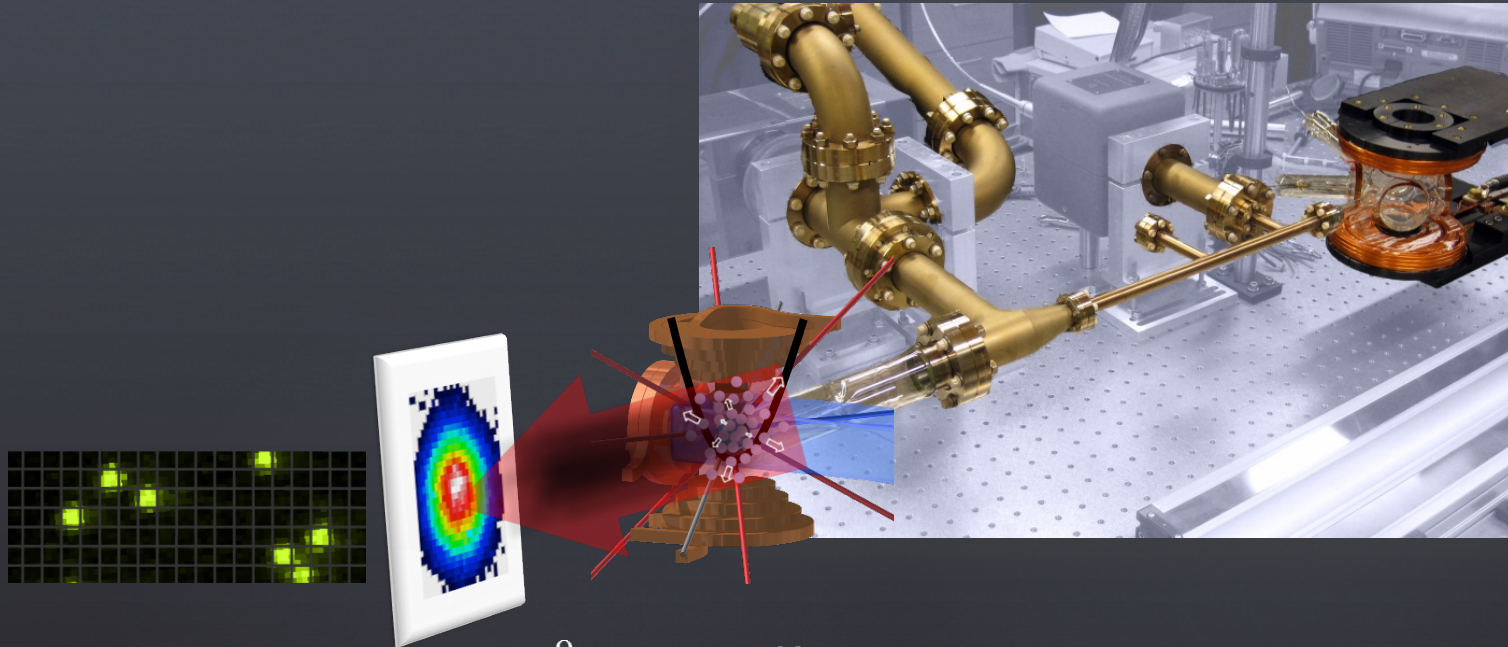
$1 - 10^9$  atoms, nK temperatures

$10 - 100 \mu m$  in diameter

Bosons ( $^{87}\text{Rb}$ ,  $^{23}\text{Na}$ , ...), fermions ( $^{40}\text{K}$ ,  $^6\text{Li}$ , ...)

Interact through collisions: contact potential  $4\pi a \hbar^2 \delta^3(\vec{r}_i - \vec{r}_j)/m$   
(attractive, repulsive, tunable)





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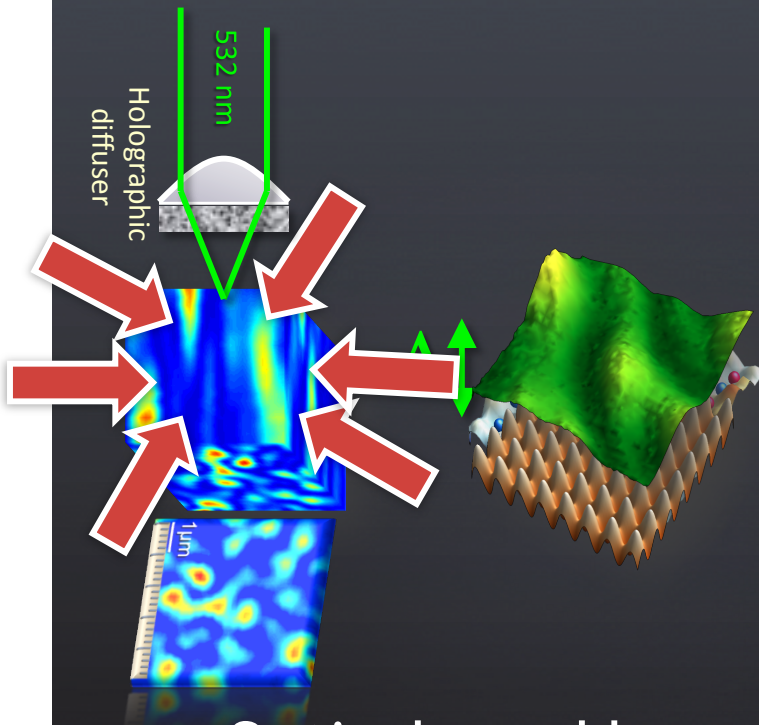
Interact through collisions: contact potential  $4\pi a \hbar^2 \delta^3(\vec{r}_i - \vec{r}_j)/m$   
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Manipulated using lasers & optical potentials

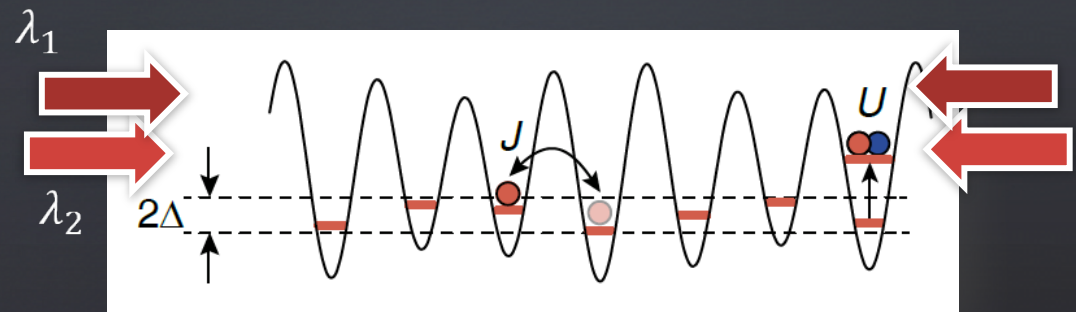
Data from images

Test-bed for theory & numerics,  
discovery of new phenomena

# Optical disorder



Optical speckle

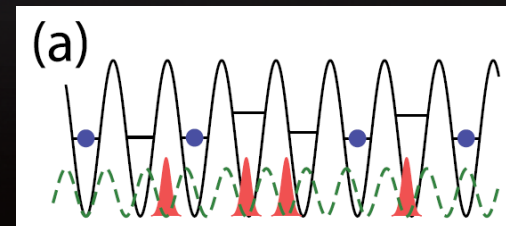


Bloch, arXiv: 1501.05661 (2015)

Incommensurate lattices

Precisely known, tunable

Also: atomic impurities

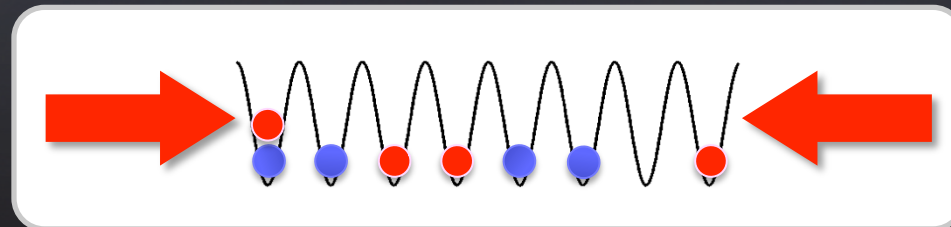
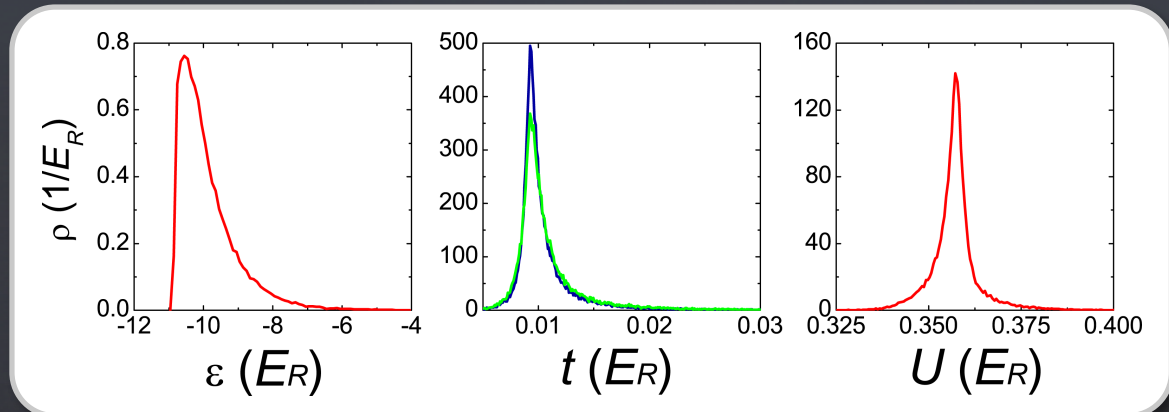
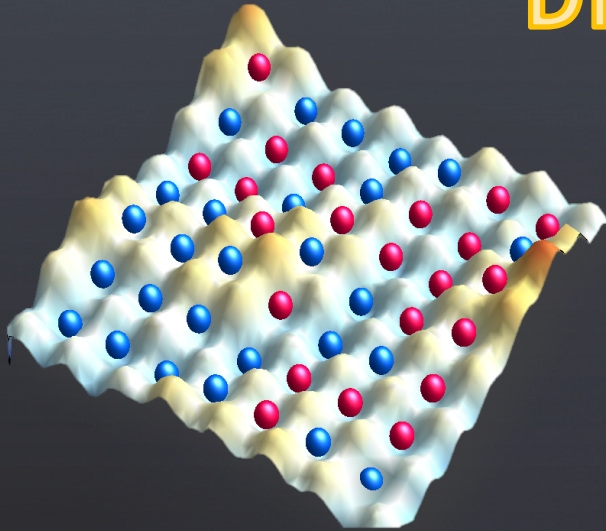


Scheible



Most significant impact:

## Disordered Hubbard models



$$H = \sum_i n_{i,\sigma} \varepsilon_i - \sum_{\langle ij \rangle} t_{ij} b_i^\dagger b_j + \sum_i U_i n_i (n_i - 1) / 2$$

Simplest paradigms for understanding  
interplay of disorder and strong interactions

# Importance

Spectacular fundamental phenomena

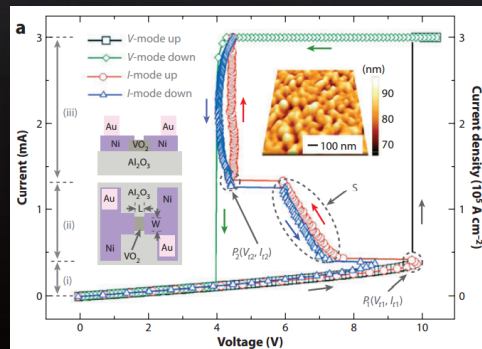
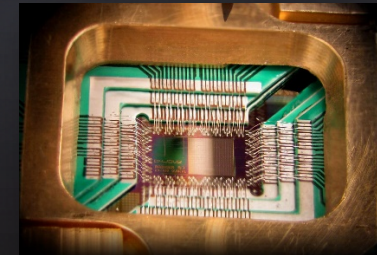
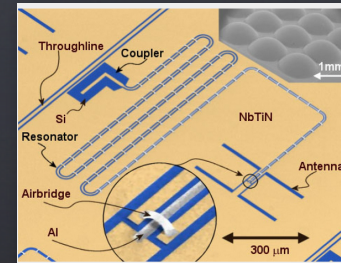
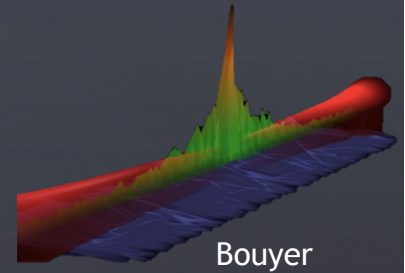
Open fundamental questions: especially dynamics

Practical applications

Disordered superconductors

Optimization via quantum annealing

Mott-tronics



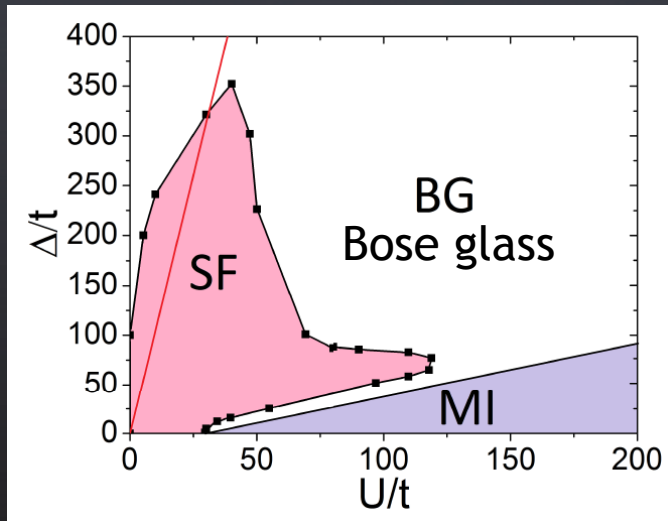
Lee et al., Appl. Phys. Lett. 92:162903



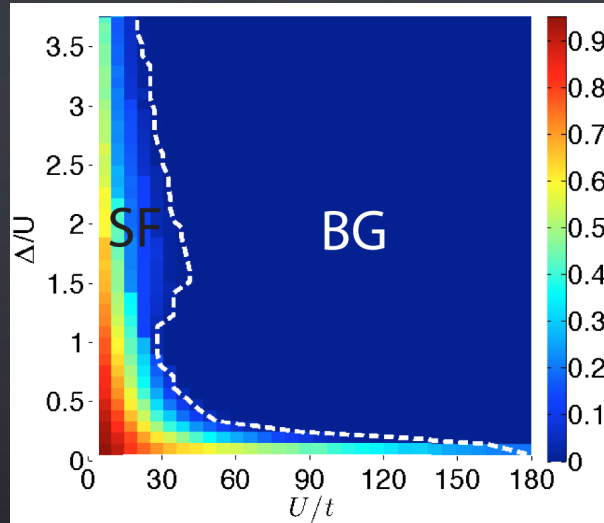
# What's known

## Disordered Bose-Hubbard Model

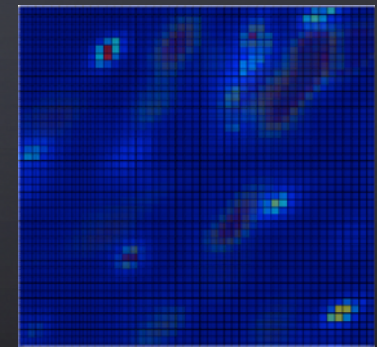
Equilibrium ground-state phase diagrams in 1D, 2D, 3D



Pollet



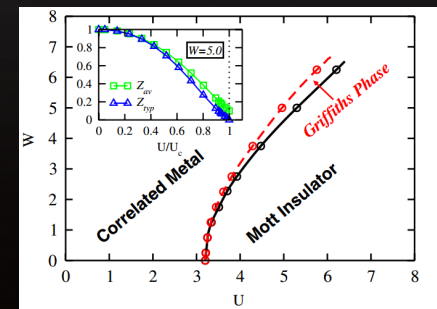
Ray, Ceperley



Trap, varied fillings, non-zero  $T$  for large  $N$  accessible to QMC

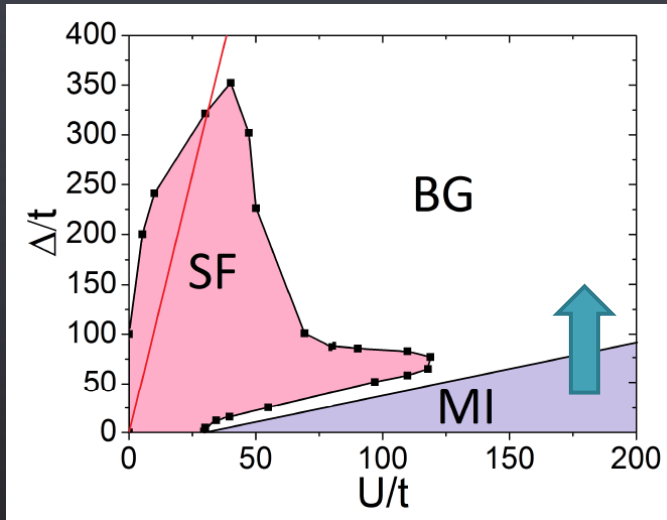
## Disordered (Fermi)-Hubbard Model

Much less is certain! Ex:  $U > 0$ , mean field



Dobrosavljevic

# What's unknown / Questions



Mott insulator (MI)-BG transition:  
Griffiths transition

How do Griffiths  
transitions play out in nature?

Phase diagram of DFH model

$U < 0, U > 0$  Superfluid phases?

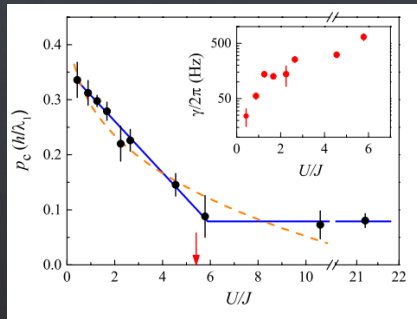
Properties of Many-body localized (MBL) phases?

**Excited States,  
Dynamics, Out-of-equilibrium behavior**

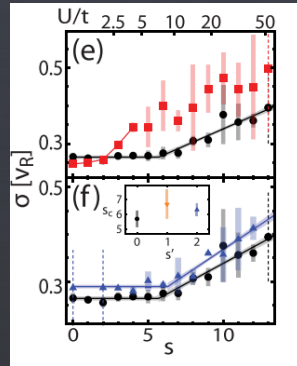


# Progress / Highlights

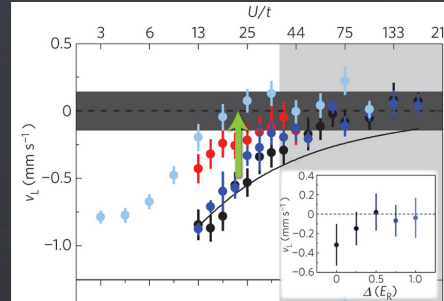
## 1D & 3D SF-BG transition



Inguscio



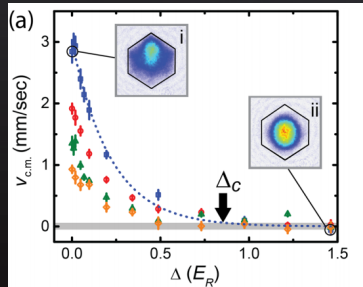
Schneble



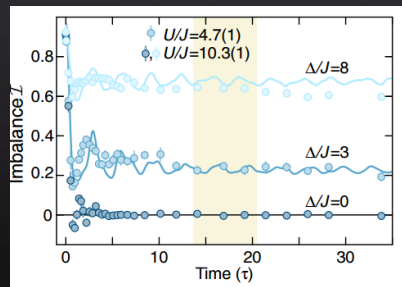
DeMarco

## MBL (fermions, strongly correlated M-IN transition)

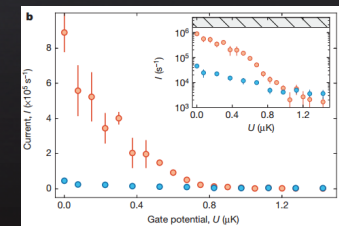
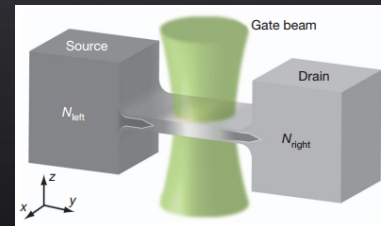
## 2D paired-SF Diffusion



DeMarco



Bloch

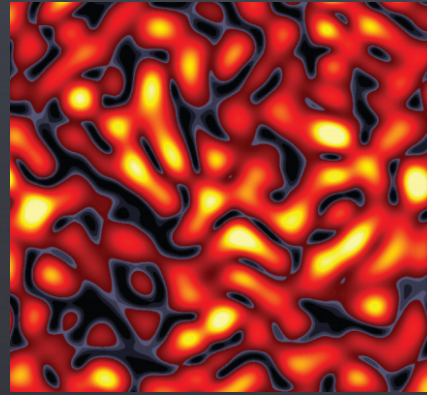


Esslinger

Anderson localization, Coherent back scattering, ...  
See also work by Aspect, Hulet, Rolston, ...

# Challenges

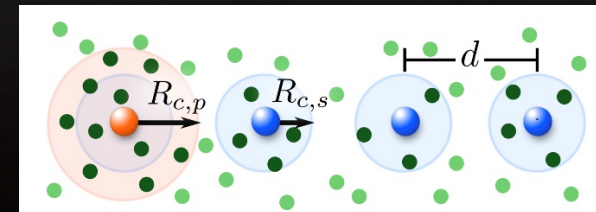
2D Localization



Measuring temperature



More complex interactions

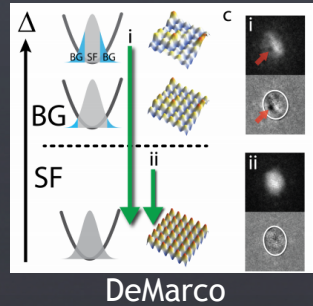


Wüster

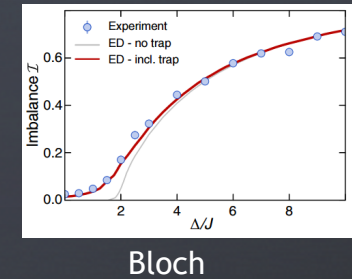


# Opportunities

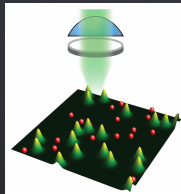
Dynamics;  
Annealing;  
Quenching;  
Critical Properties



Ergodicity;  
Equilibrium

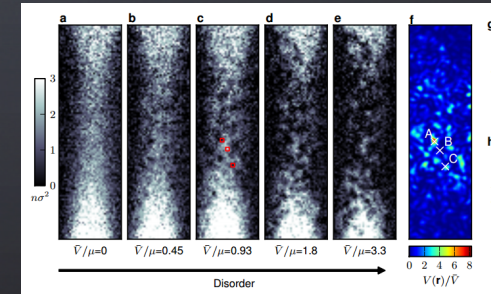


2D



DeMarco

Fermions,  
paired superfluids



Esslinger

Non-zero temperature

Magnetic impurities / disorder

Measurement is fully controlled

“Material” is fully characterized and tunable

Closed quantum systems

All dynamical timescales accessible