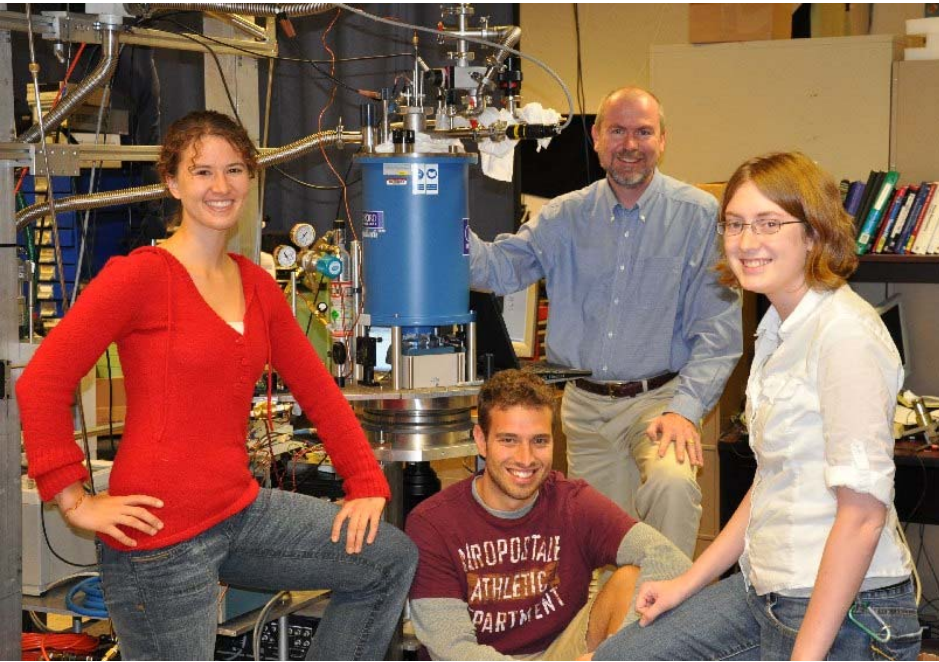


Visualization in quantum fluids

Dan Lathrop

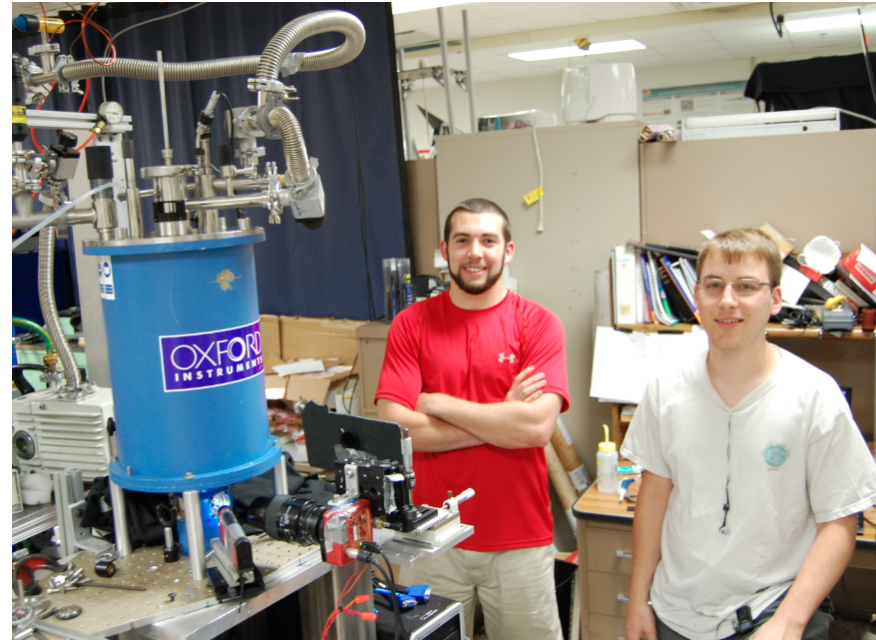


**Kristy (Gaff)
Johnson**

Matt Paoletti

Kaitlyn Tuley

**University of Maryland
National Science Foundation**



Chris Boughter and David Meichle



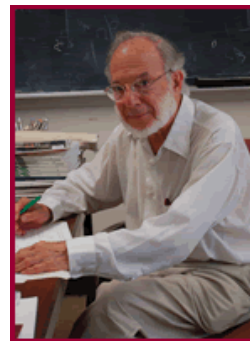
Enrico Fonda



Greg Bewley



K.R. Sreenivasan



Michael Fisher



Peter Megson

Quantum Fluids

A **state of matter** with long range quantum order

Type of synchronization

partial phase sync of the individual atomic wave functions

E.g.

BEC atomic systems

^4He

^3He

Cooper pair electrons in superconductors

Physical vacuum

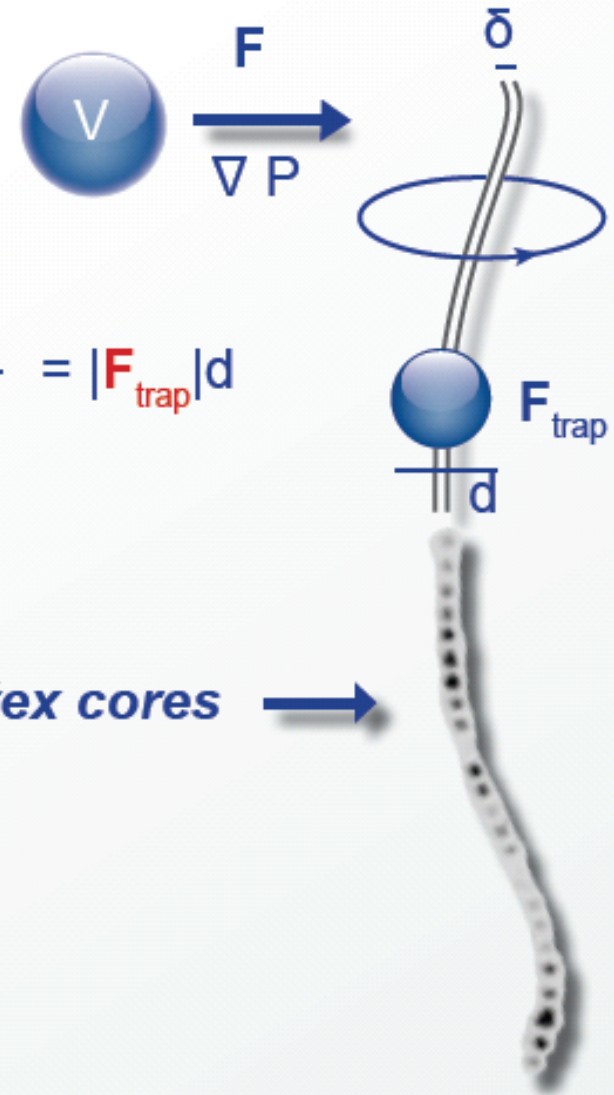
Quantum fluid dynamics and quantum disorder

Why does it matter?

Visualization of vortices - particle trapping

$$P = -\frac{\rho_s \kappa^2}{8\pi^2 r^2}$$

$$\mathbf{F} = \oint_{\partial\Omega} P \hat{n} dA$$



Decrease of energy $\Delta\varepsilon = \frac{\rho_s \kappa^2}{4\pi} d \ln \frac{d}{2\delta} = |\mathbf{F}_{\text{trap}}| d$

$$\frac{\mathbf{F}_{\text{trap}}}{V} \propto \frac{\ln d}{d^3}$$

Particles get trapped on vortex cores →

Ions in liquid He $\ominus 16 \text{ \AA}$ $\oplus 6 \text{ \AA}$

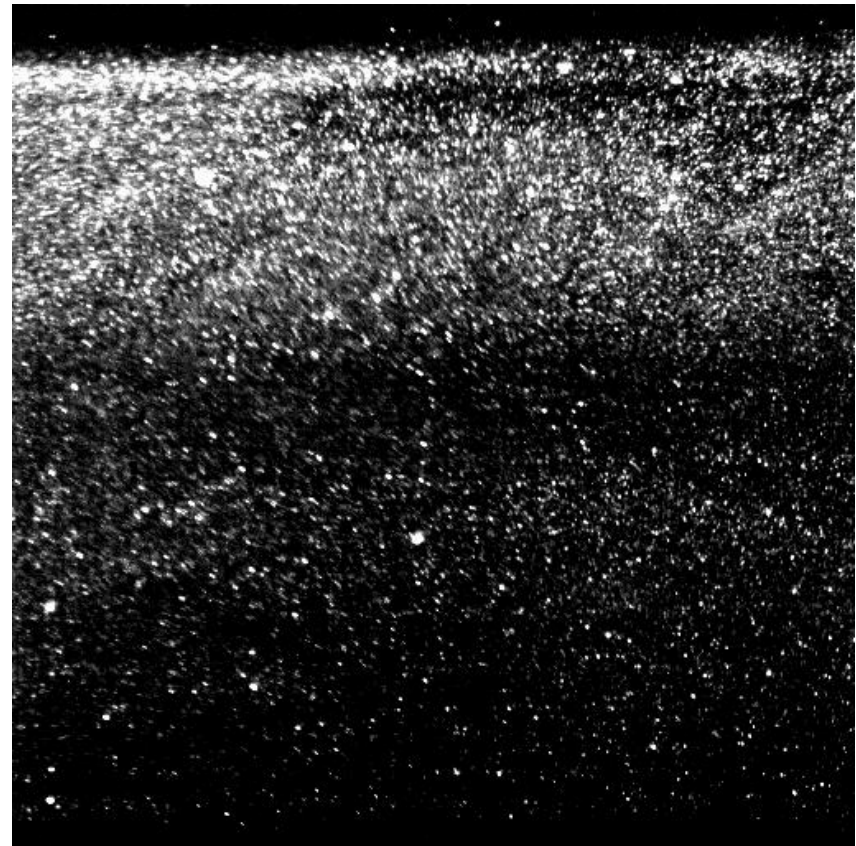
Parks and Donnelly (1966), Williams and Packard (1974)

Solid hydrogen particles $> 1 \mu\text{m}$

Bewley, Lathrop, Sreenivasan, Nature 441 588 (2006)

Visualizing Superfluid Vortices in He II

- Below T_λ hydrogen particles collect onto filaments
- Previous work has shown these filaments are particles trapped on the superfluid vortices (Bewley, *et al.*, *Nature* 2006)



8
mm

Movie in real time
Begins 180 s after transition
 $T_\lambda - T \sim 50$ mK

Sounds through transition caught with
MEMS microphone

Vortex reconnection

Theoretical work

Schwarz, PRB 1985 (LV)

de Waele and Aarts, PRL 1994 (LV)

Koplik and Levine, PRL 1993 (NLSE)

Tsubota and Maekawa, JPSJ 1992 (LV)

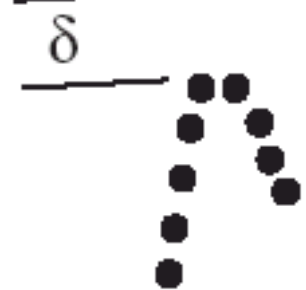
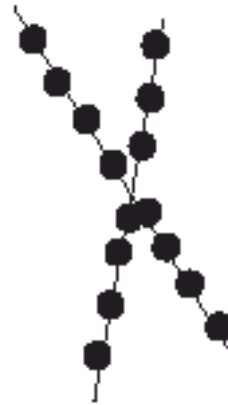
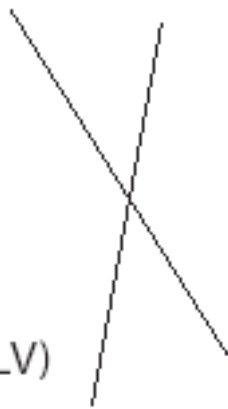
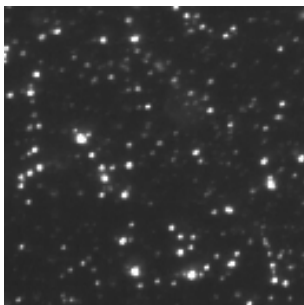
Nazarenko and West 2003 (NLSE)

Much more recent work!

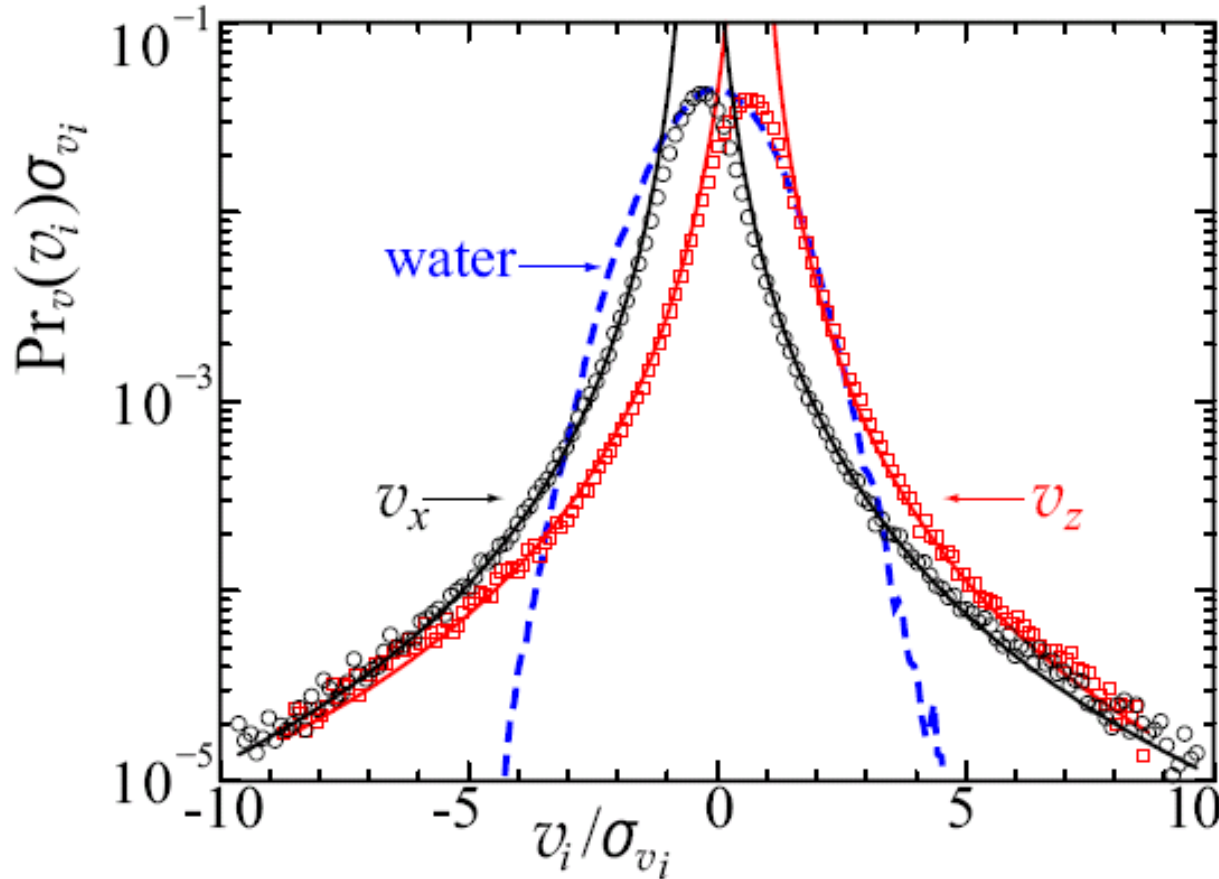
Kerr PRL 2011 (NLSE)

$$\delta \sim \kappa^{1/2}(t_0 - t)^{1/2}$$

$$\delta \sim \kappa^{1/2}(t - t_0)^{1/2}$$



Velocity Statistics



$$\delta = A \kappa^{1/2} (t-t_0)^{1/2}$$

$$\mathbf{v}(t) \sim \kappa^{1/2} |t-t_0|^{-1/2}$$

$$P(\mathbf{v}) d\mathbf{v} = P(t) dt$$

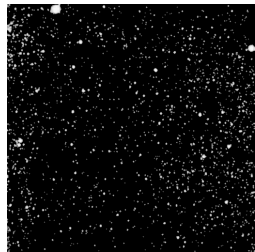
$$P(\mathbf{v}) \sim \left| \frac{dt}{d\mathbf{v}} \right|$$

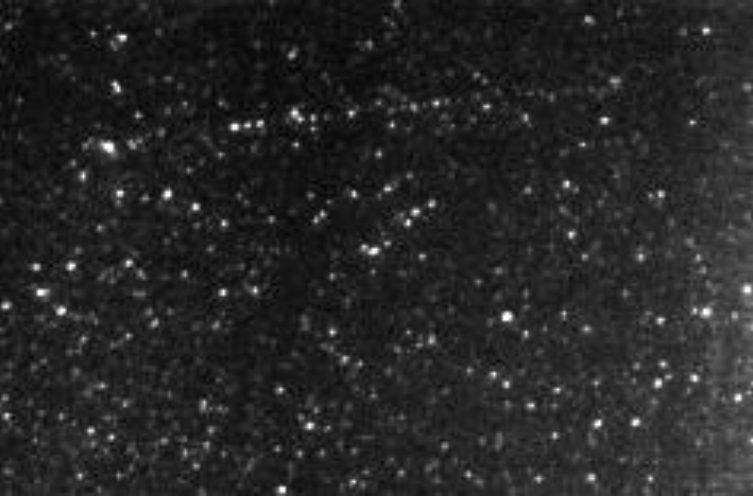
$$P(\mathbf{v}) \sim \left| \frac{1}{\mathbf{v}^3} \right|$$

Reconnection produces predictable
power-law velocity tails quite distinct
from classical turbulence

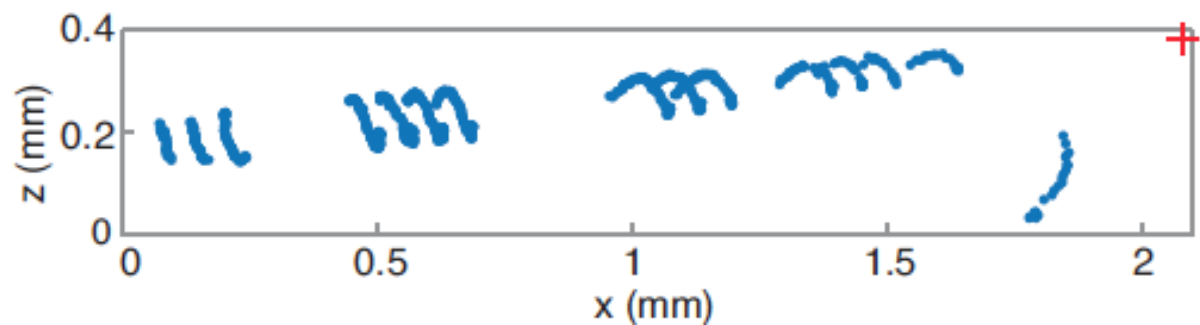
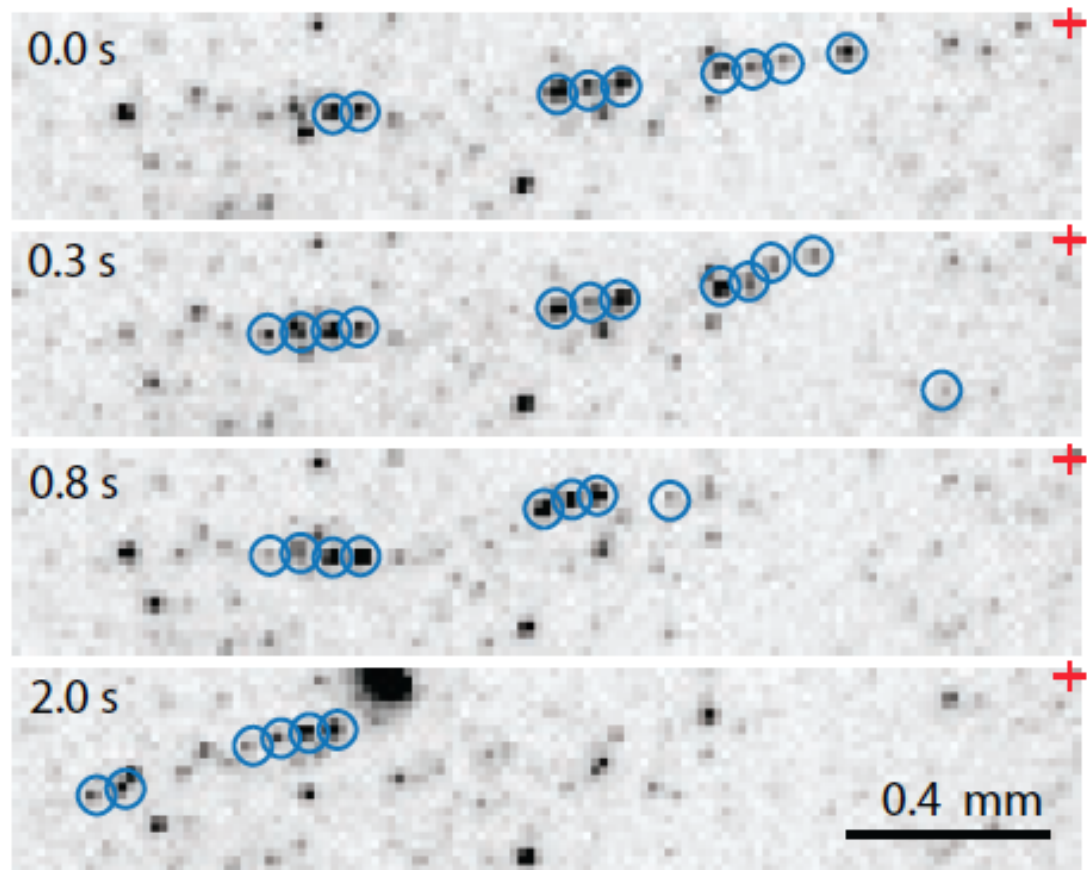
M.S. Paoletti, M.E. Fisher, K.R. Sreenivasan, and D.P. Lathrop, "Velocity statistics distinguish quantum from classical turbulence," Phys. Rev. Lett. (2008)

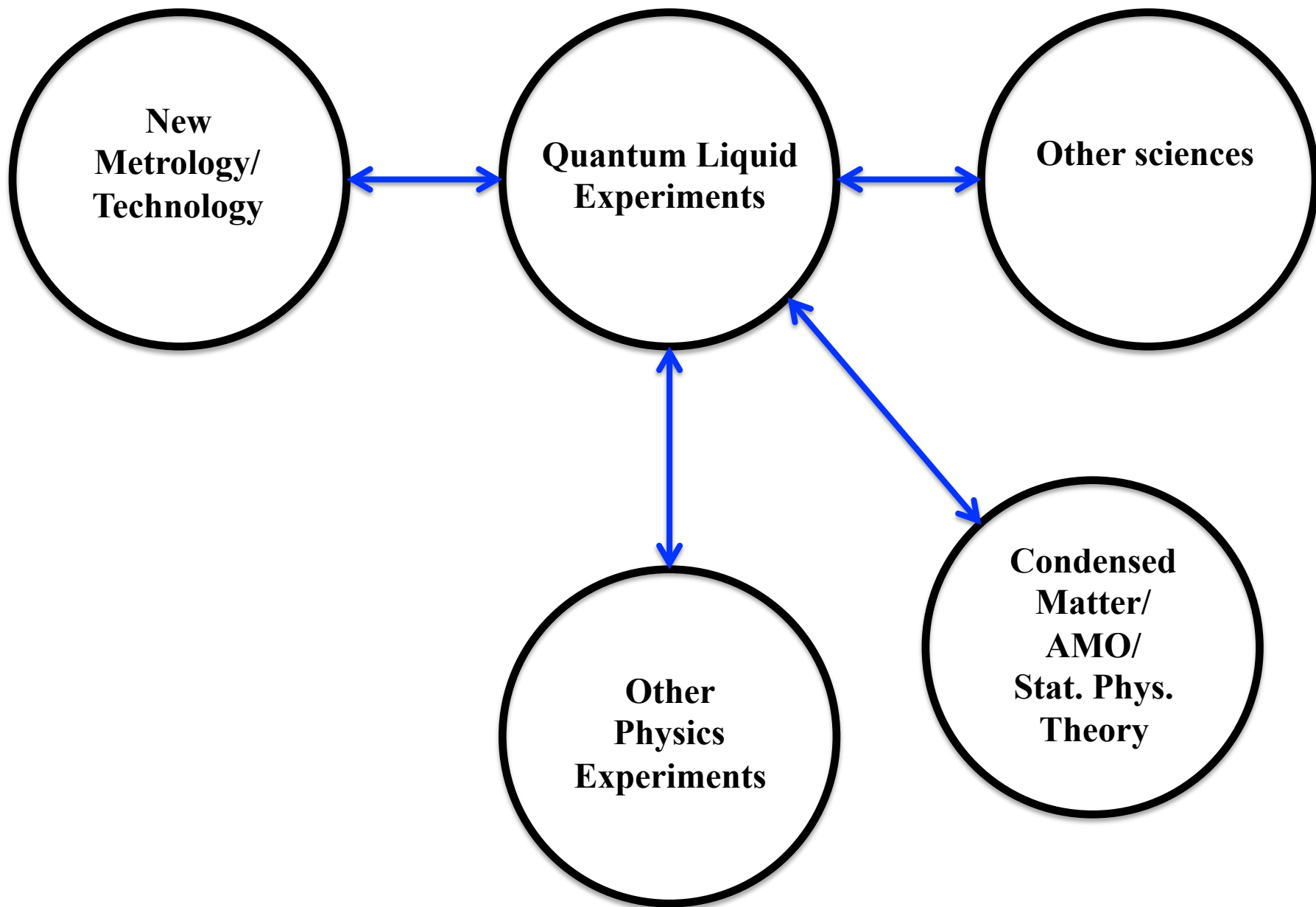
Baggaley and Barenghi, PRE (2011).

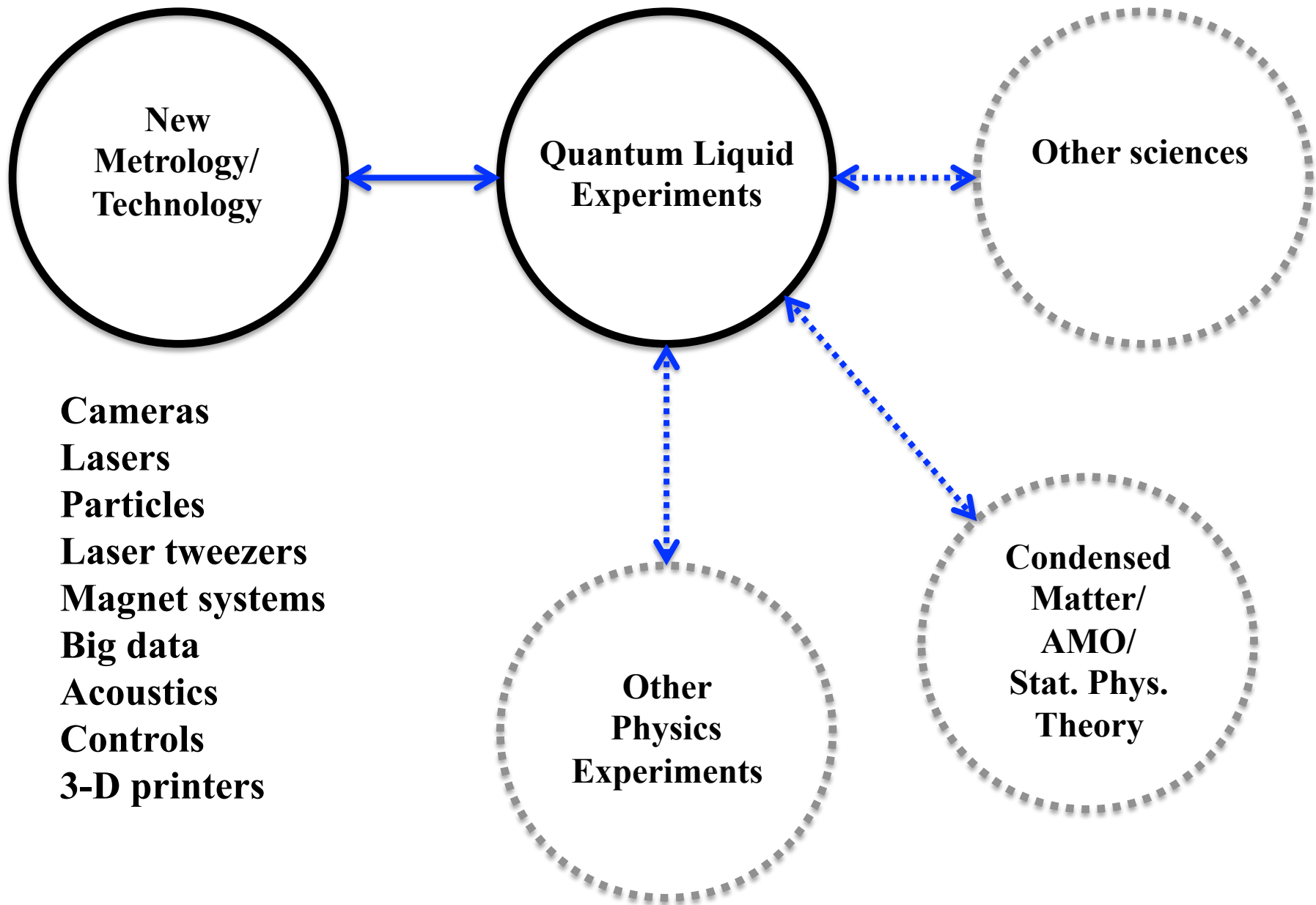




Kelvin waves!







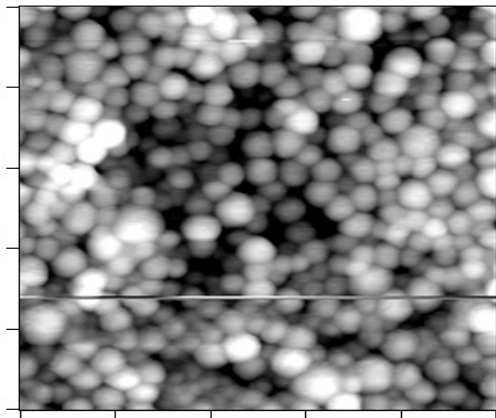
Fluorescent Nanoparticle Dispersion

Particle type	Manufacturer	Part number	Shipped form	Size (nm)	Excitation & Emission(nm)
Quantum Dots	Ocean Nanotech	QSP600	Powder	5	532 / 602
Gold Nanorods	Nanopartz	E16-532	Organic Solvent	25x35	533 / 556
FluoroSpheres	Life Technologies	F8784	Aqueous	20	532 / 575
FluoroSpheres	Life Technologies	F8800	Aqueous	100	540 / 560
FluoroSpheres	Life Technologies	F8819	Aqueous	1000	535 / 575

TABLE I. Details of all particle types successfully dispersed in both liquid helium and nitrogen.

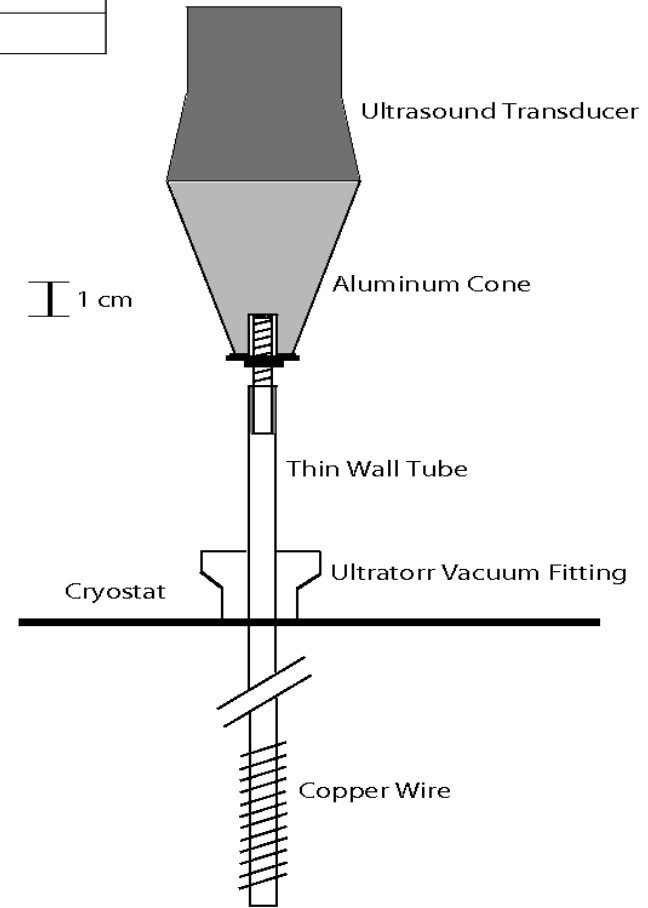
D.P. Meichle and D.P. Lathrop. "Nanoparticle dispersion in superfluid helium." *Rev. Sci. Inst.* 85.7 (2014): 073705.

Provisional Patent 2014, Application No. US 62/014,564

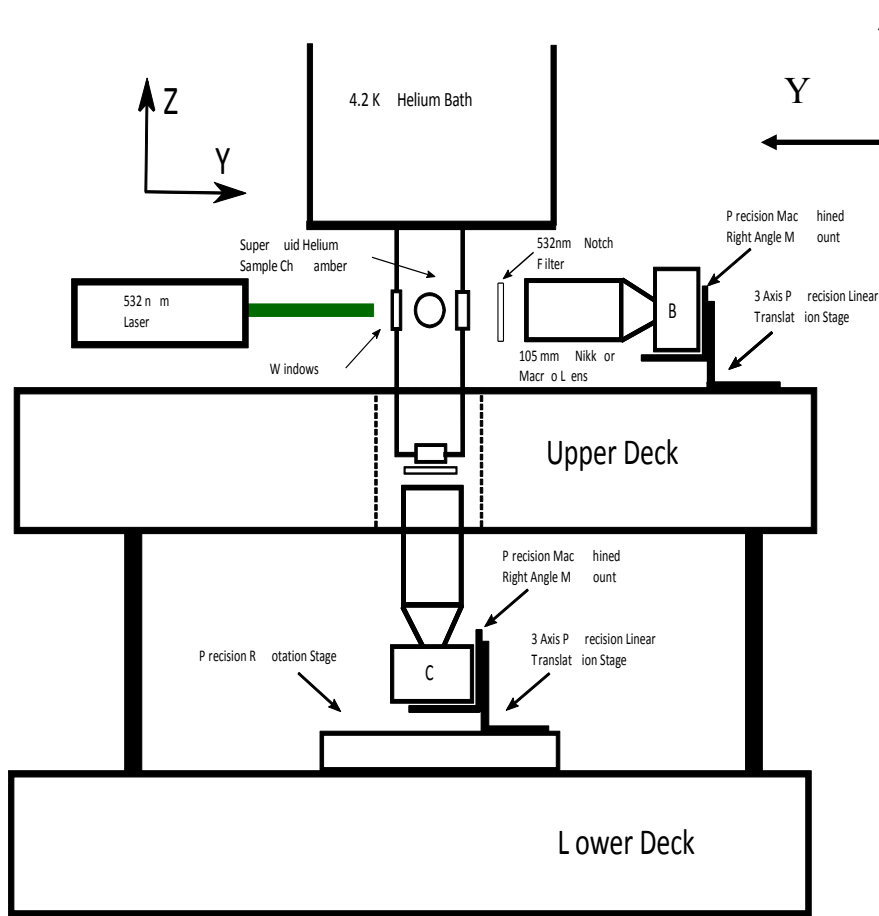


500 nm

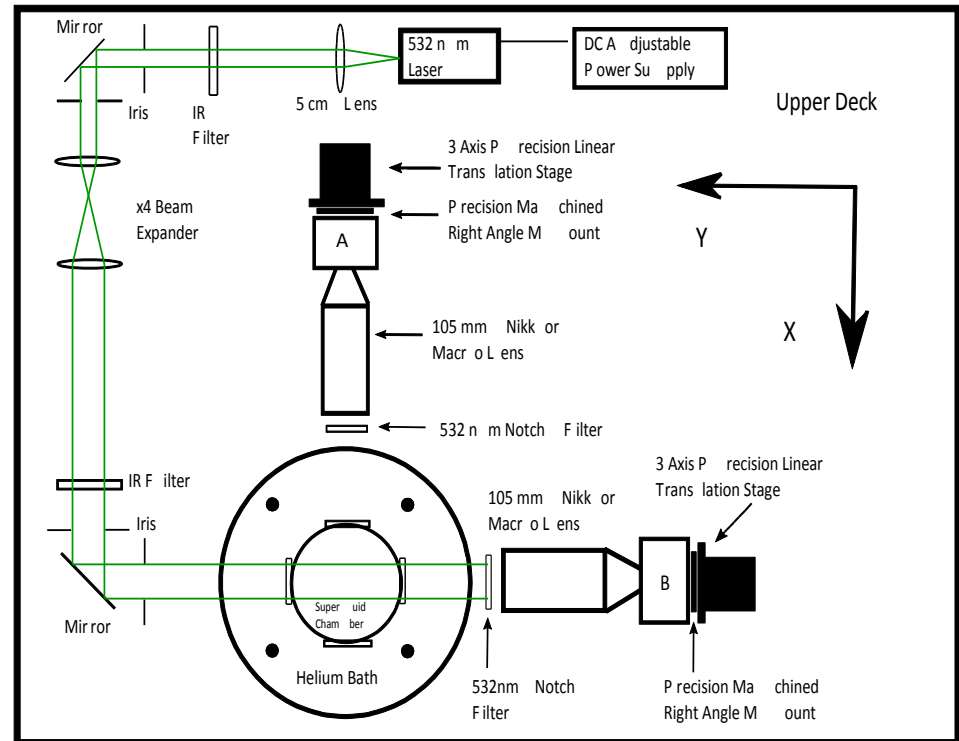
AFM Image Courtesy of Joe Garrett at UMD



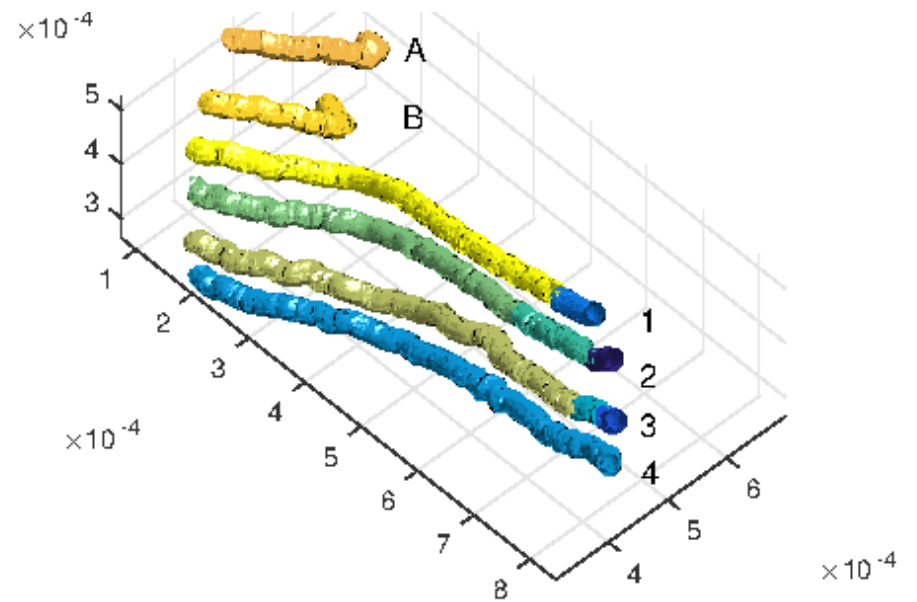
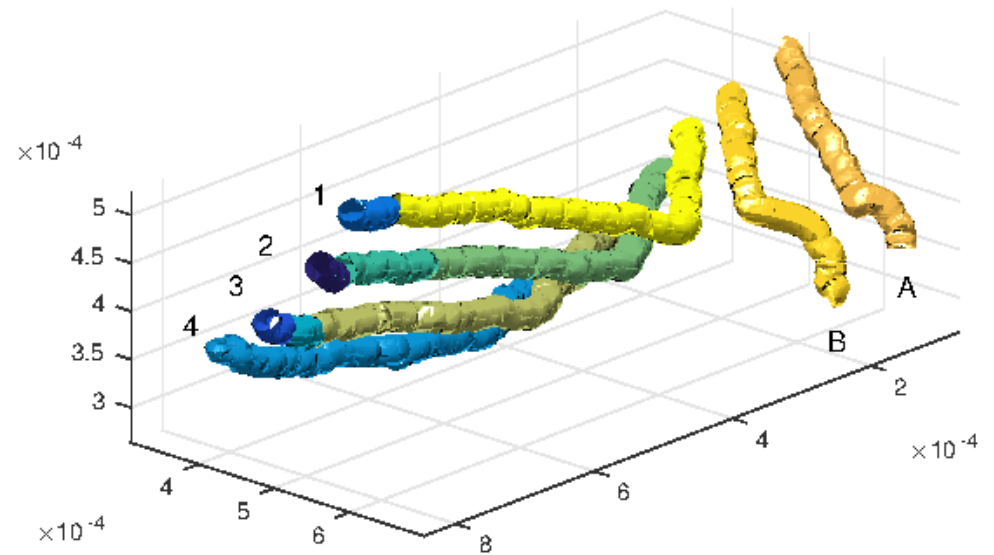
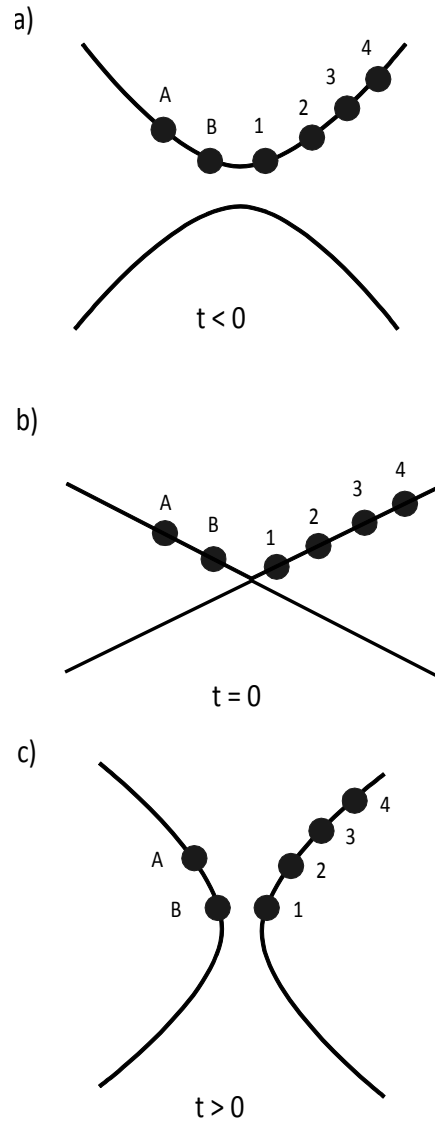
3D Stereographic Microscope Setup



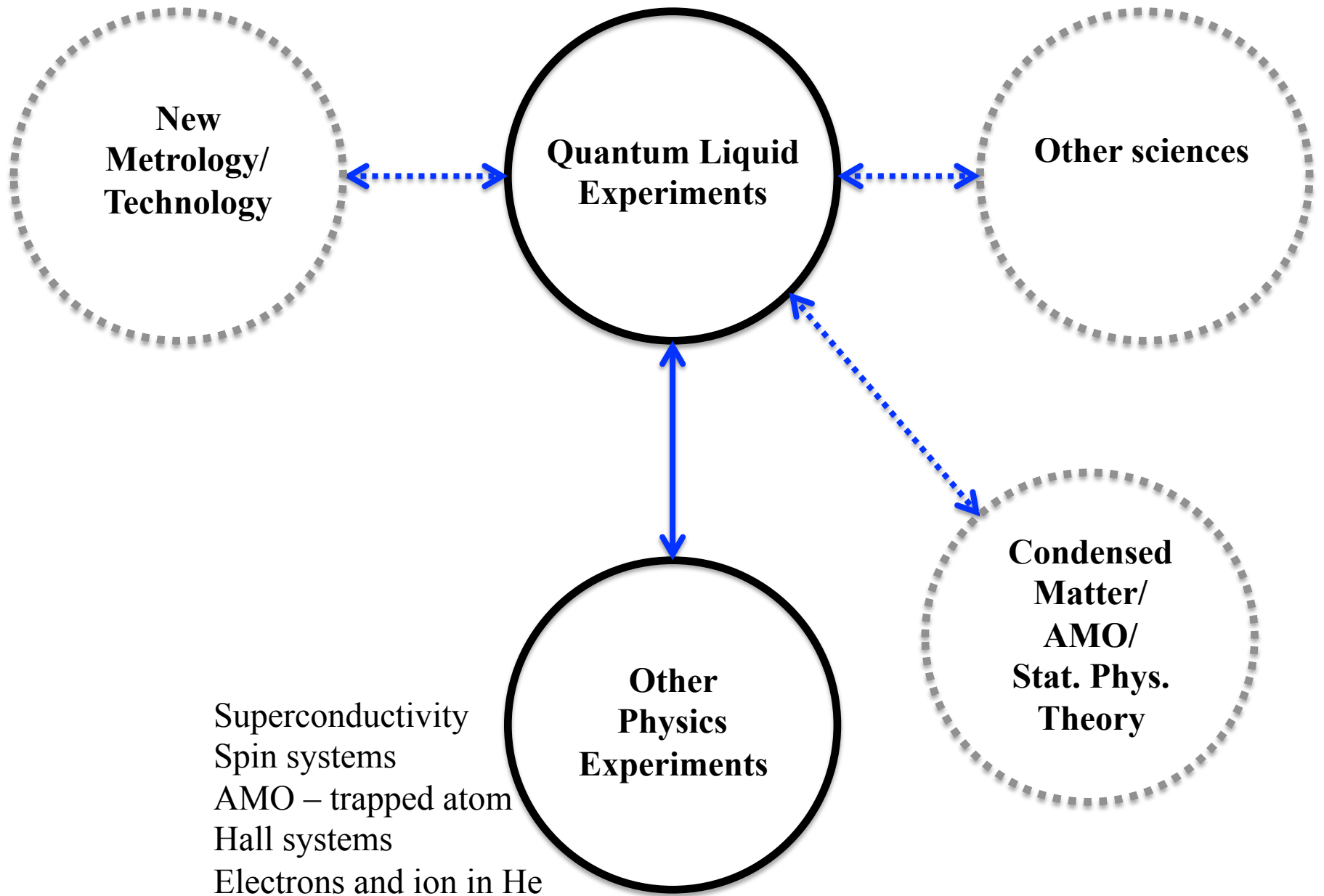
- Camera mounts hand-machined and aligned to .001 inch and .1 degree tolerances
- All three cameras mutually perpendicular and share axes

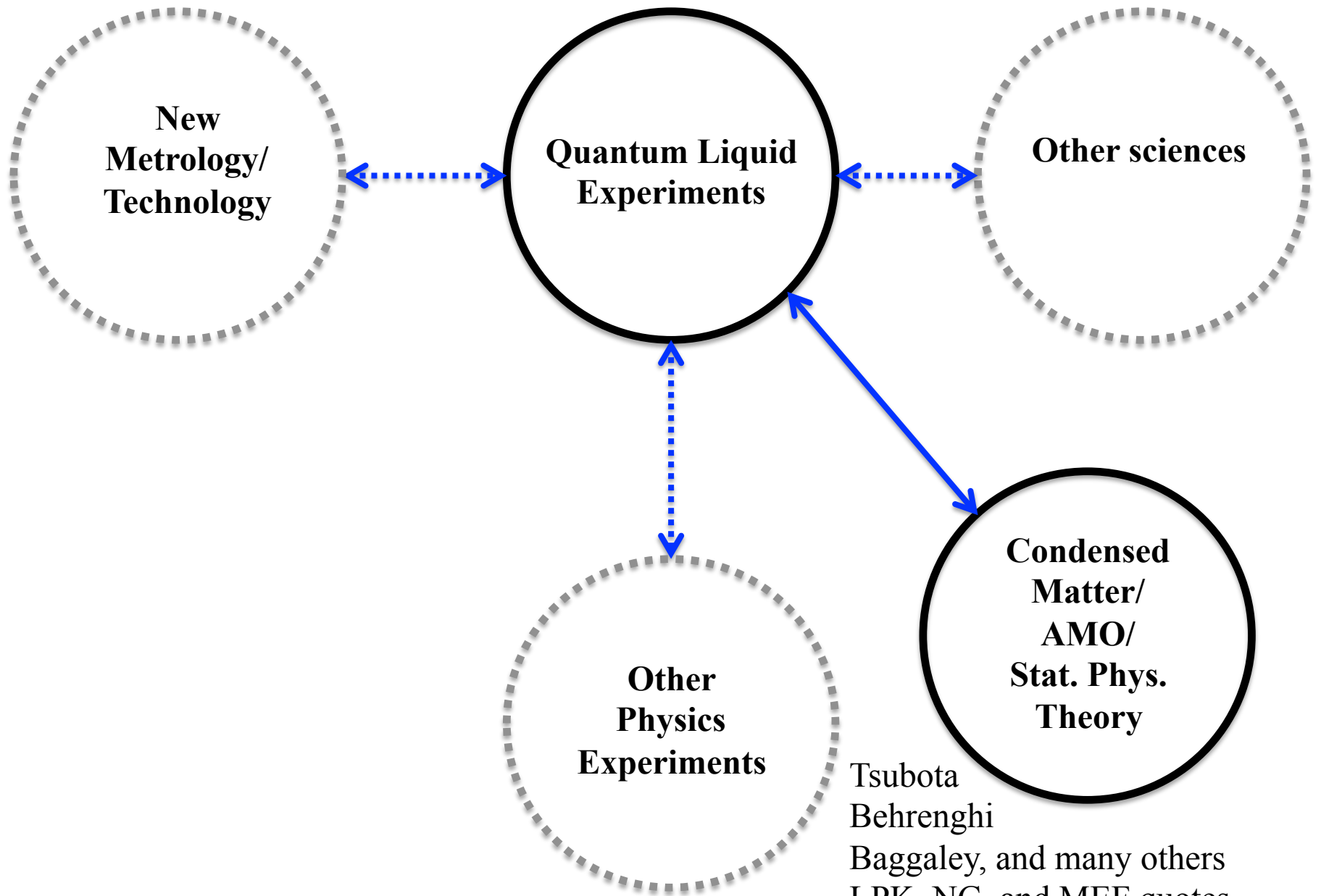


First 3D Vortex Reconnection



^3He experiments with nanoparticles





Supplement to

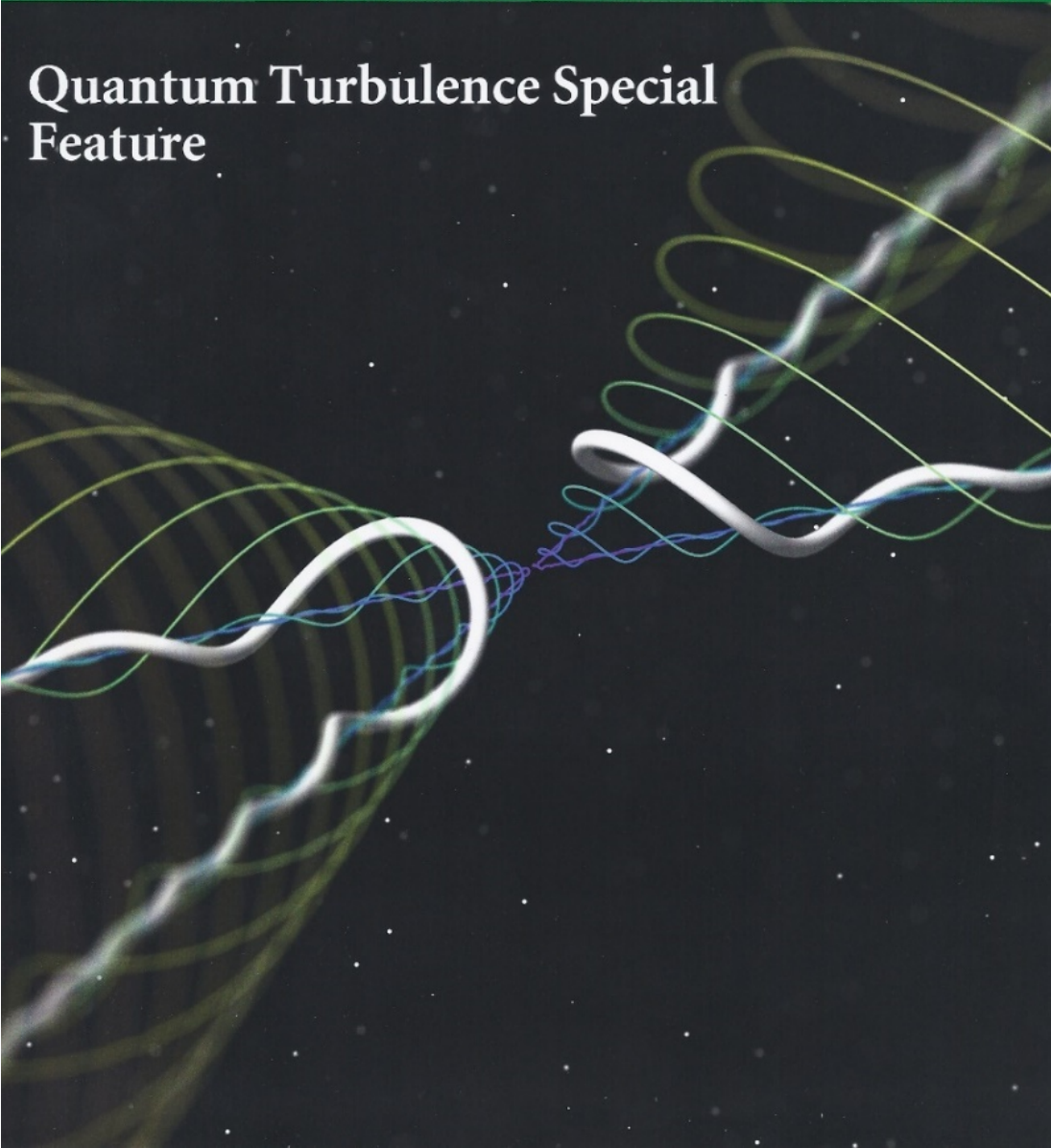
PNAS

March 25, 2014 | vol. 111 | suppl. 1 | pp. 4647-4734

Proceedings of the National Academy of Sciences of the United States of America

www.pnas.org

Quantum Turbulence Special Feature



E. Fonda, D.P. Meichle, S. Hormoz, N.T. Ouellette, D.P. Lathrop. "Direct observation of Kelvin waves excited by quantized vortex reconnection." *Proc. Nat. Acad. Sci. USA.* 111. Supplement 1 (2014): 4707-4710. (Special Feature Cover)

Quantum fluid dynamics theory snapshot

Nonlinear Schrödinger – Gross Pitaevskii equation

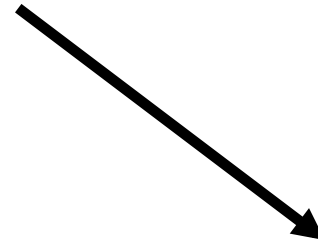
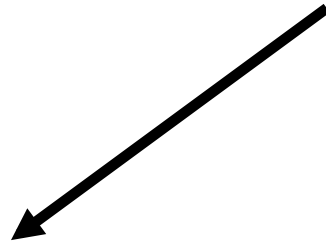
Biot-Savart Models

Line interaction models

Other models involving Euler equations – caution!



Superfluid Vortex Models

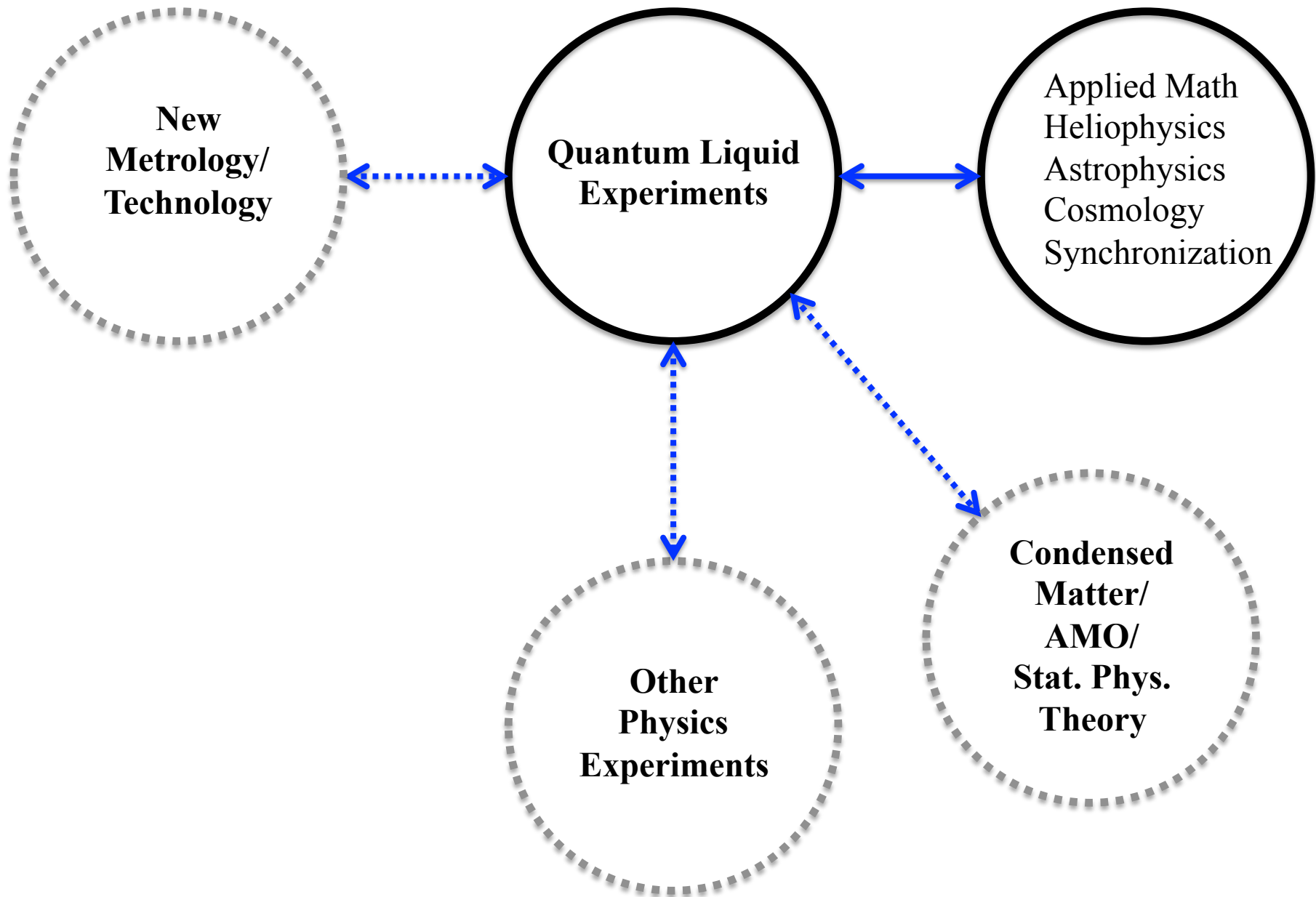


Microscopic (Angstrom Scale)

- Quantum Mechanical
- Zero Temperature Only
- Captures Vortex Reconnection Intrinsically
- Time Reversal Symmetric & Conservative

Macroscopic (Micrometers and larger)

- Heuristic / Phenomenological
- Includes Mutual Friction
- Ad-Hoc Reconnection Only
- Non-Conservative, Dissipative



The formation of vortices as one cools below transition:

We always see vortices

Possible formation mechanisms:

1) Kibble-Zurek mechanism

transition happens too quickly for phase uniformity
coherence length relevant

2) Remnant vortices

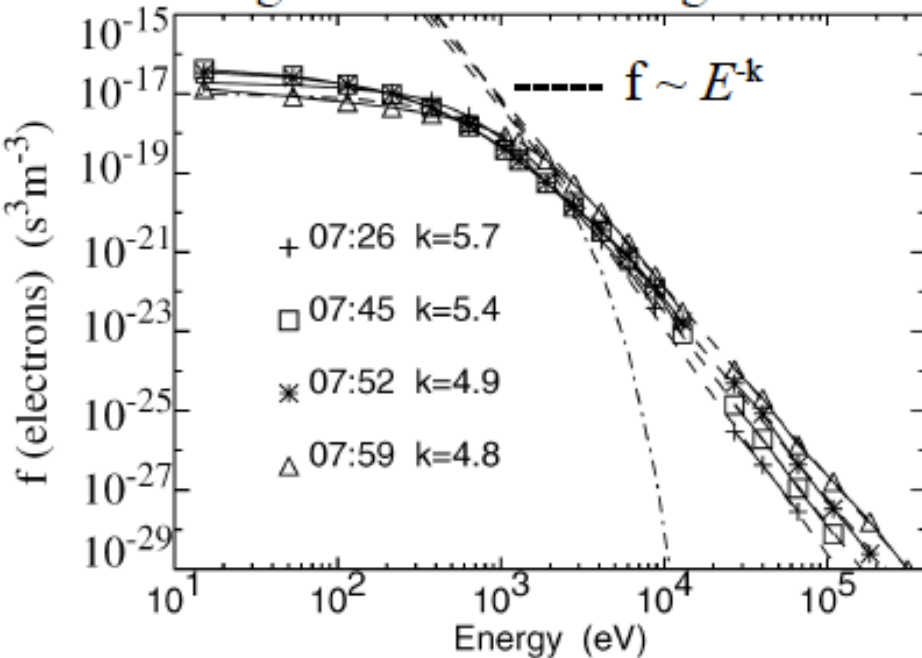
momentum and angular momentum in normal component
goes to Ψ as ρ_n decreases

3) Counterflow vortices created just below transition

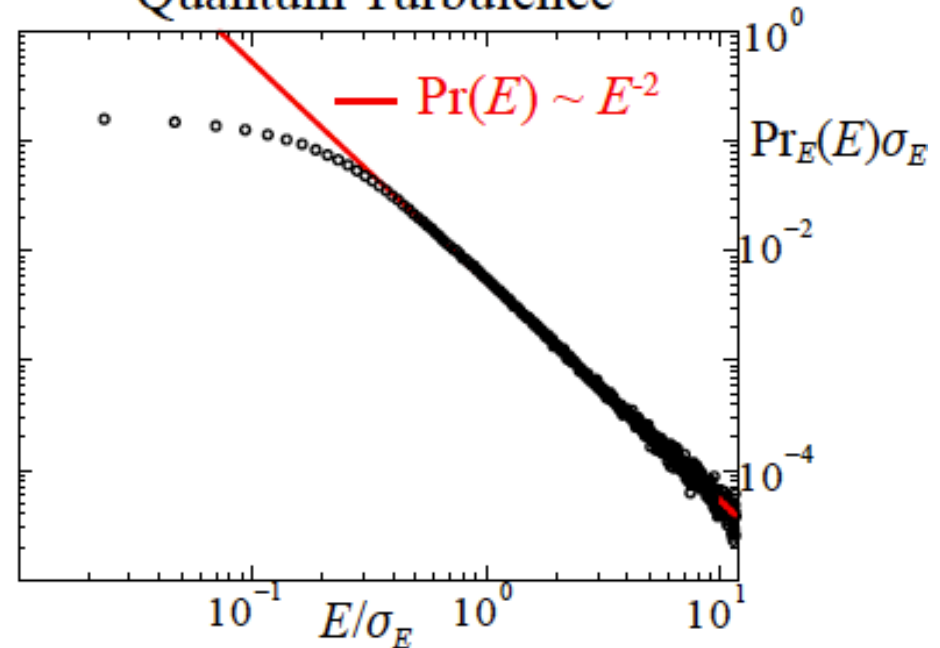
v_c is exceeded near transition no matter how little heat
flows

Analogies with MHD Turbulence

Magnetic Reconnection Diffusion
Region of Earth's Magnetotail



Reconnection-dominated
Quantum Turbulence



Magnetic field lines in highly-magnetized plasmas reconnect producing similar power-law distributions of energy

Dissertations: complex.umd.edu

Youtube channel: n3umh

Bewley, Lathrop, and Sreenivasan Nature 2006

Bewley, Sreenivasan, and Lathrop, Exp. in Fluids 2008

Paoletti, Fiorito, Sreenivasan, and Lathrop, J. Phys. Soc. Japan 2008

Bewley, Paoletti, Sreenivasan, and Lathrop, Proc. Nat. Acad. Sci. 2008

Paoletti, Fisher, Sreenivasan, and Lathrop, PRL 2008

Paoletti, Fisher, and Lathrop, Physica D 2008

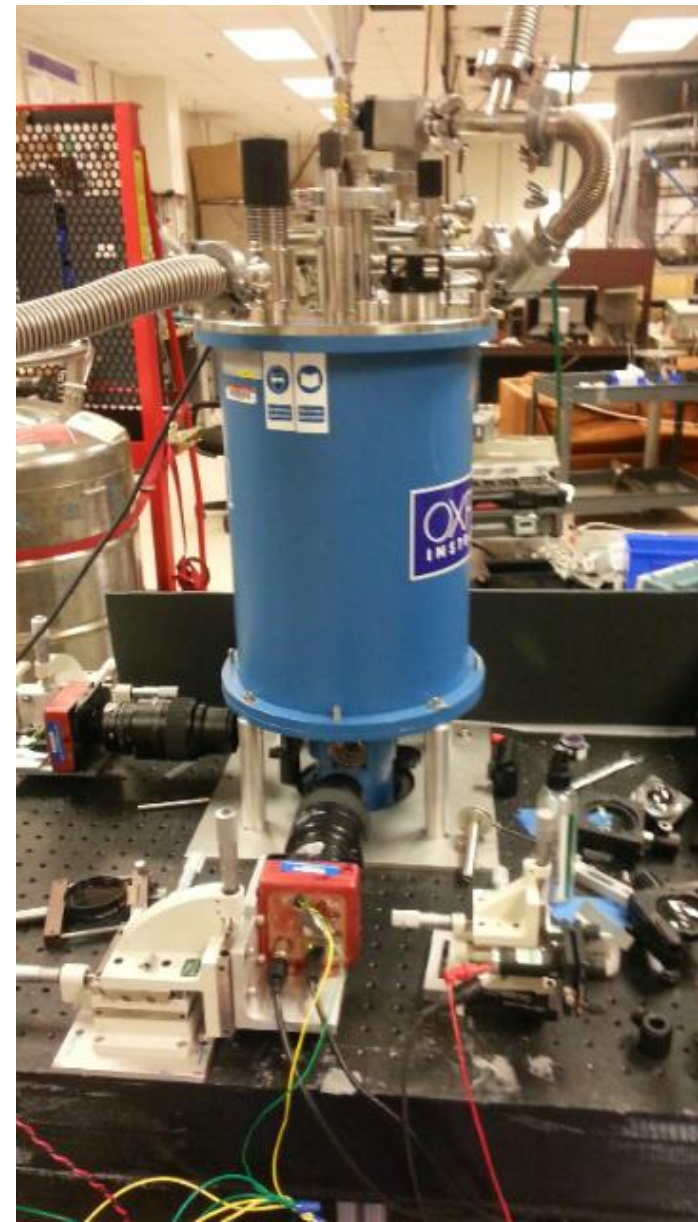
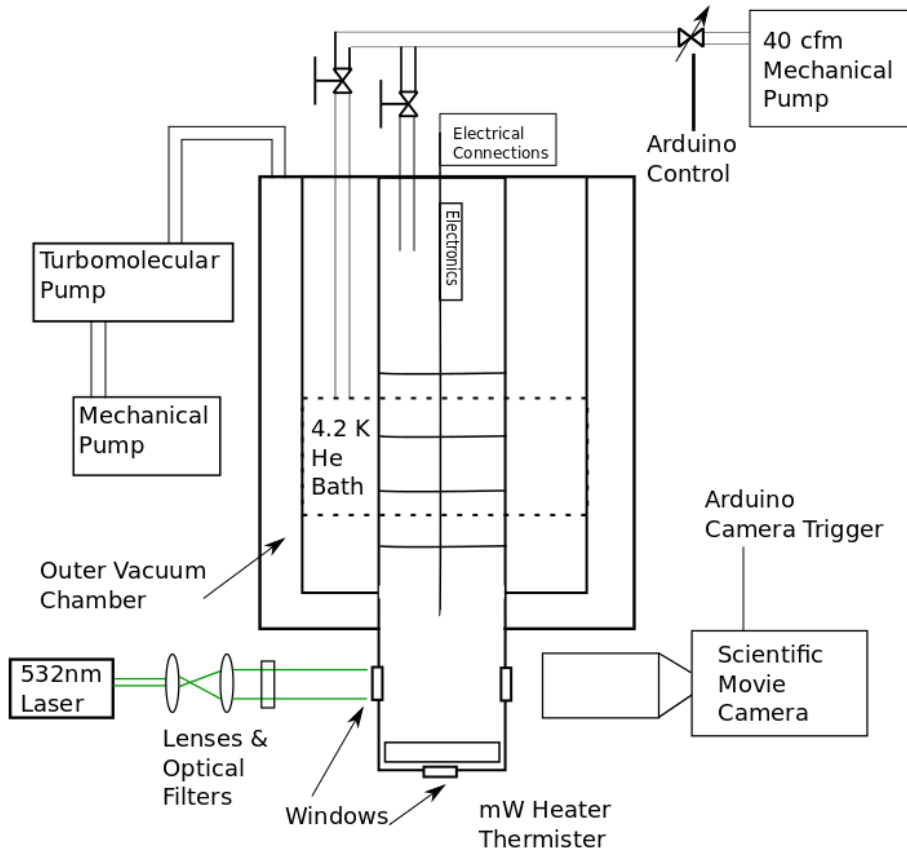
Paoletti and Lathrop, Ann. Rev. of Cond. Matter Phys. 2011

Meichle, Rorai, Fisher, and Lathrop, PRB 2012

Fonda, Meichle, Ouellette, Hormoz, and Lathrop PNAS 2014

Meichle and Lathrop Rev. Sci. Inst. 2014

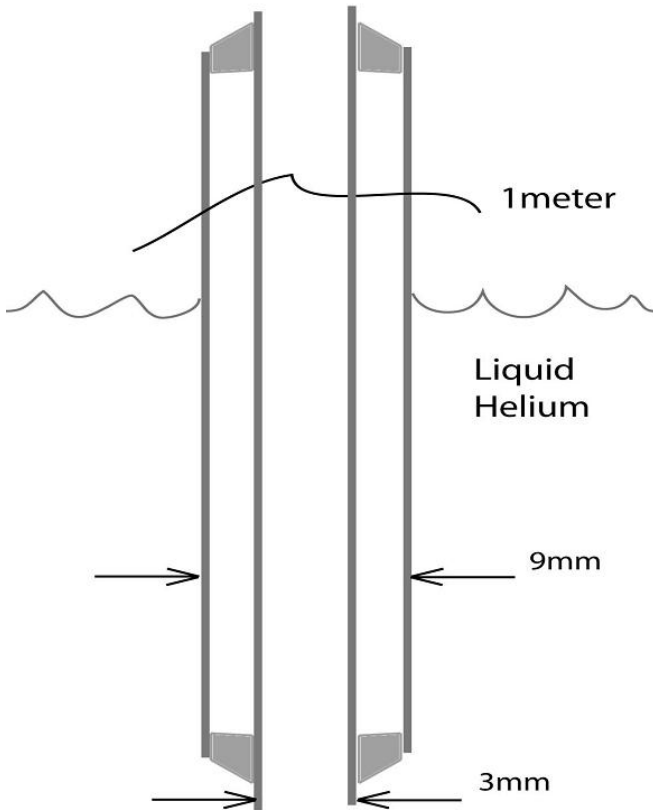
- 4.2 K to 1.48 K by evaporative cooling, superfluid fraction nearly 90%
- Disperse particles (either frozen hydrogen, atmosphere or fluorescent nanoparticles) into Helium
- Illuminate with 532 nm CW laser
- Image particles with CCD movie camera and track with sub-pixel localization (~ 3 microns) up to 200 fps



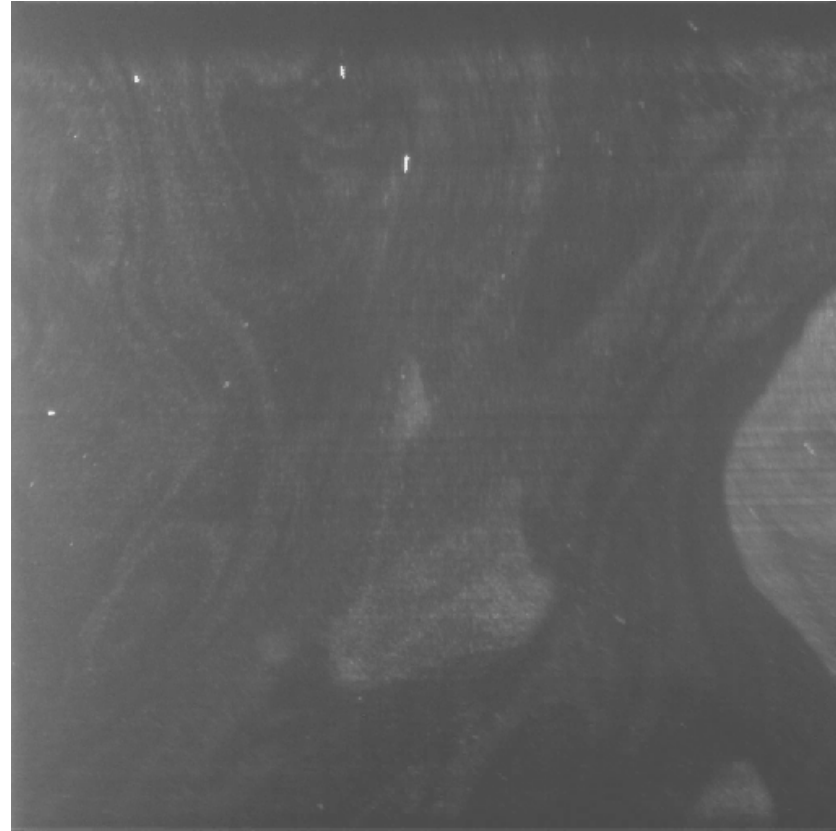
Particle Production

$1 \text{ H}_2 : \chi \text{ He } \chi \gg 1$

↓ mixture pressure applied here

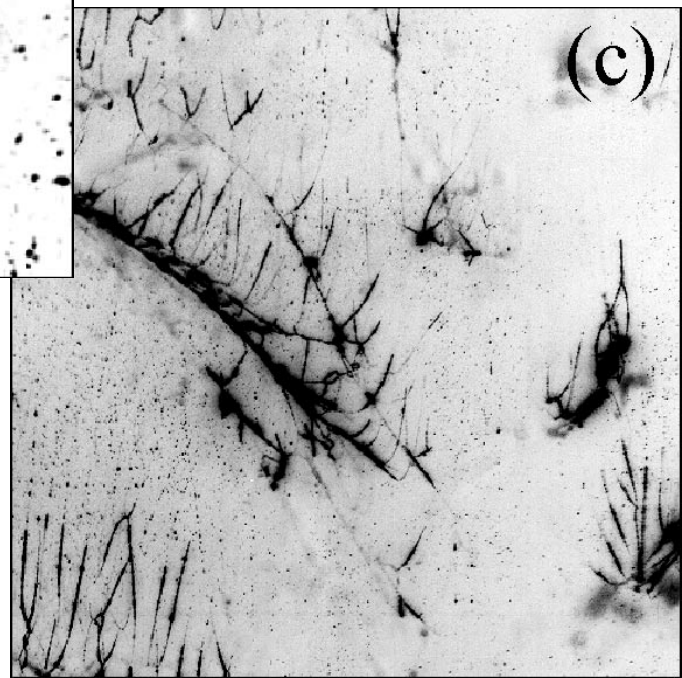
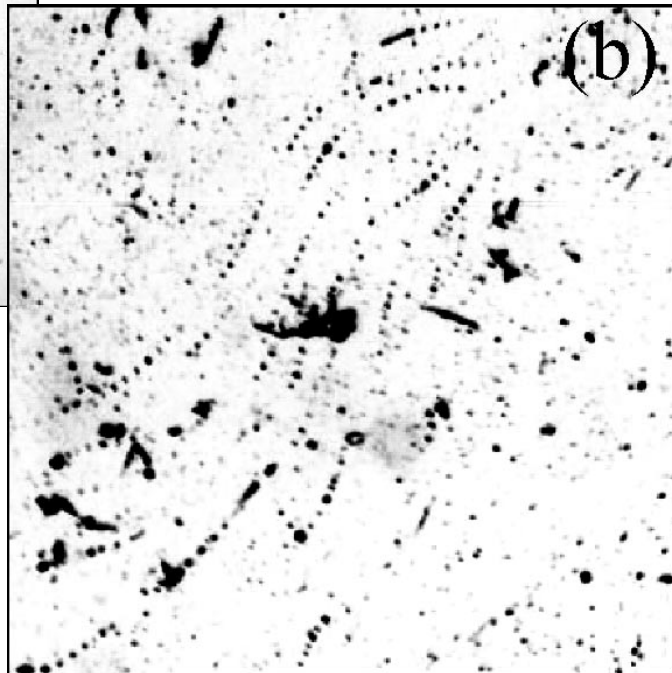
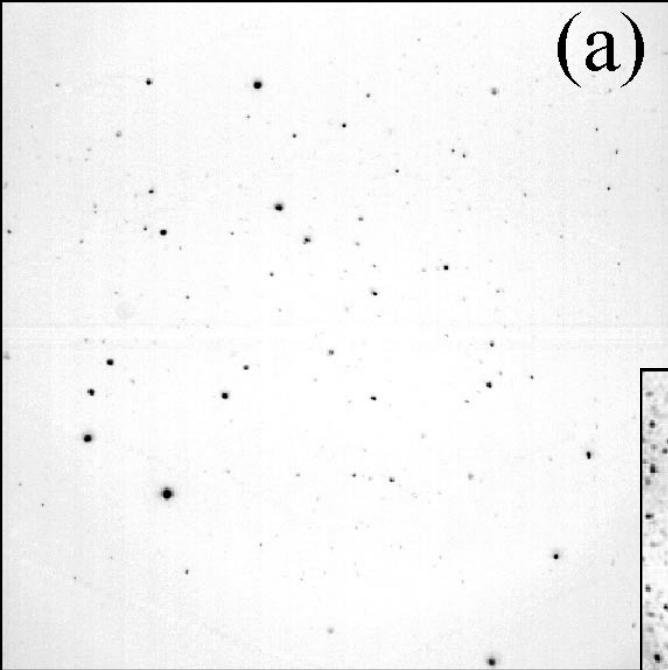


$T > T_\lambda$

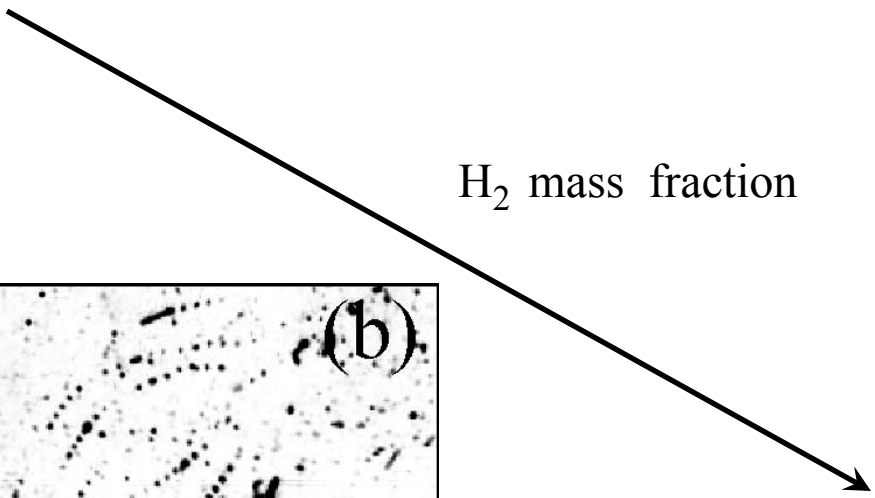


↑
1/2 image
8 mm
↓

Bewley et al., *Experiments in Fluids* 2008



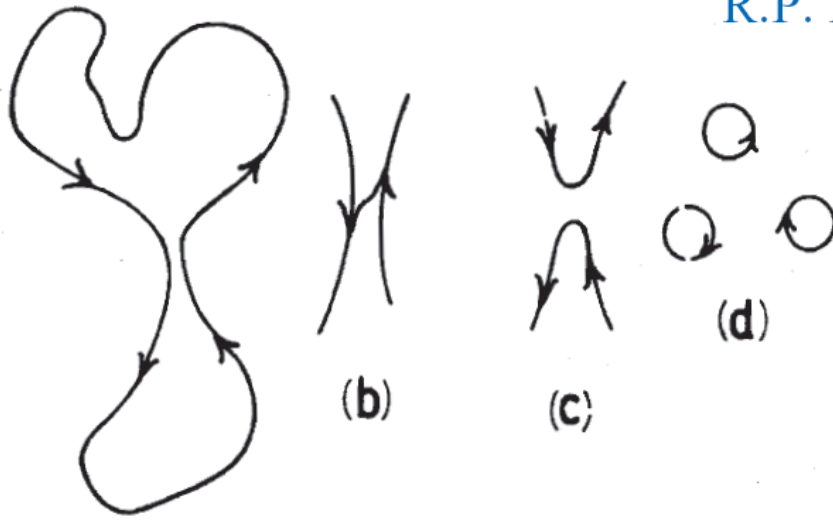
H₂ mass fraction



Smaller is better

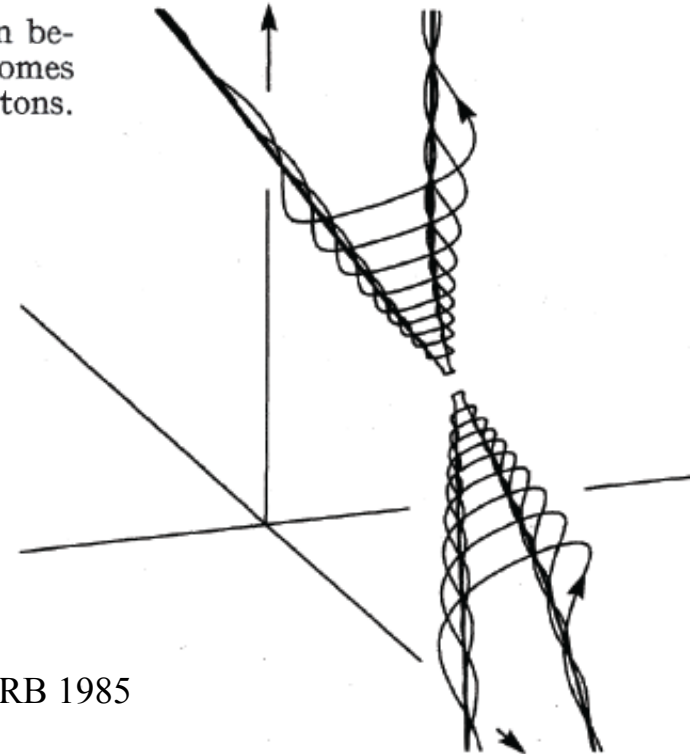
Fewer is better

Particles are not passive!



(a) Prog. Low Temp. Phys. 1, 17 (1955)

Fig. 10. A vortex ring (a) can break up into smaller rings if the transition between states (b) and (c) is allowed when the separation of vortex lines becomes of atomic dimensions. The eventual small rings (d) may be identical to rotons.



Pre-reconnection: $\delta(t) = A[\kappa(t_0-t)]^{1/2}[1+c(t_0-t)]$

Post-reconnection: $\delta(t) = A[\kappa(t-t_0)]^{1/2}[1+c(t-t_0)]$

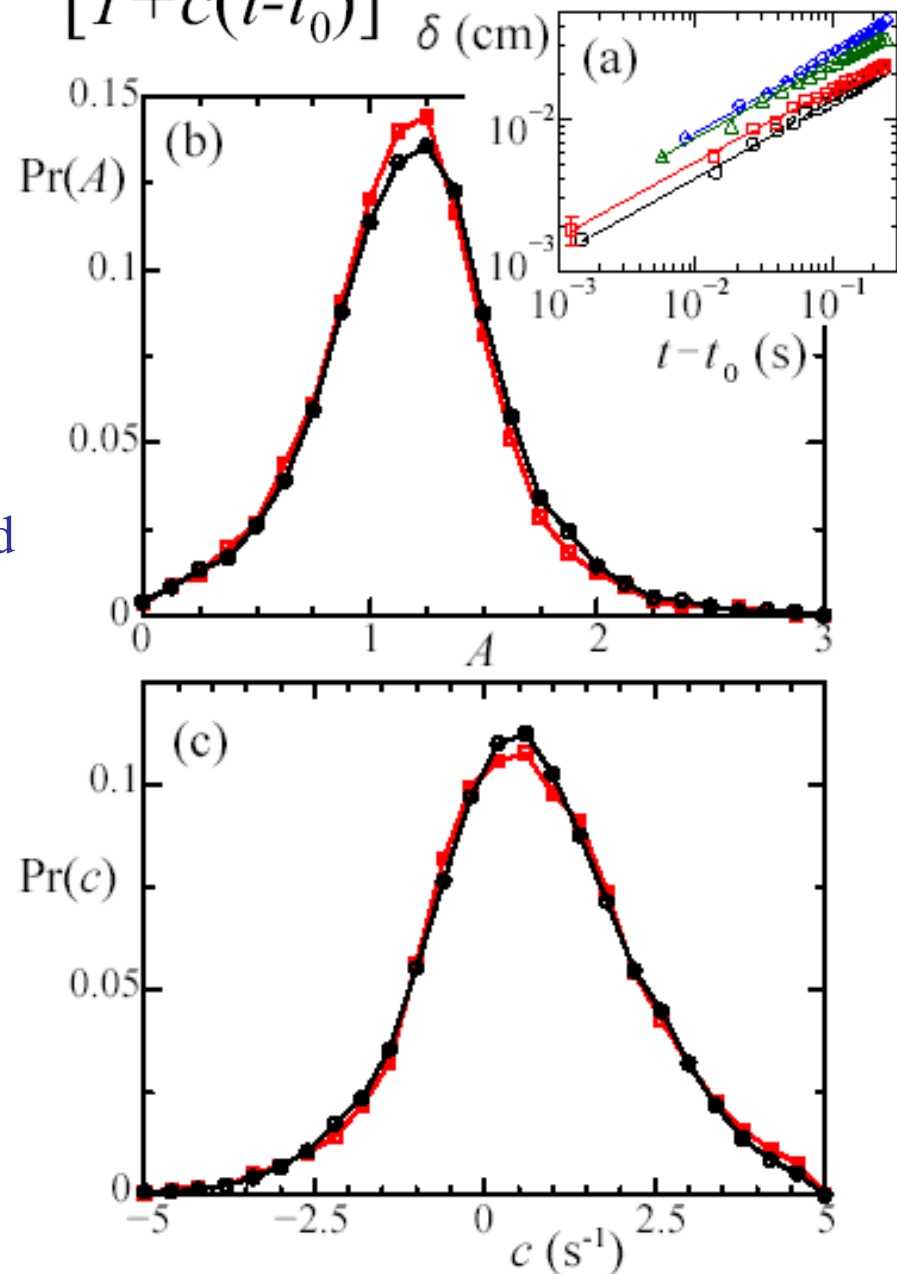
Only small pre- and post- differences

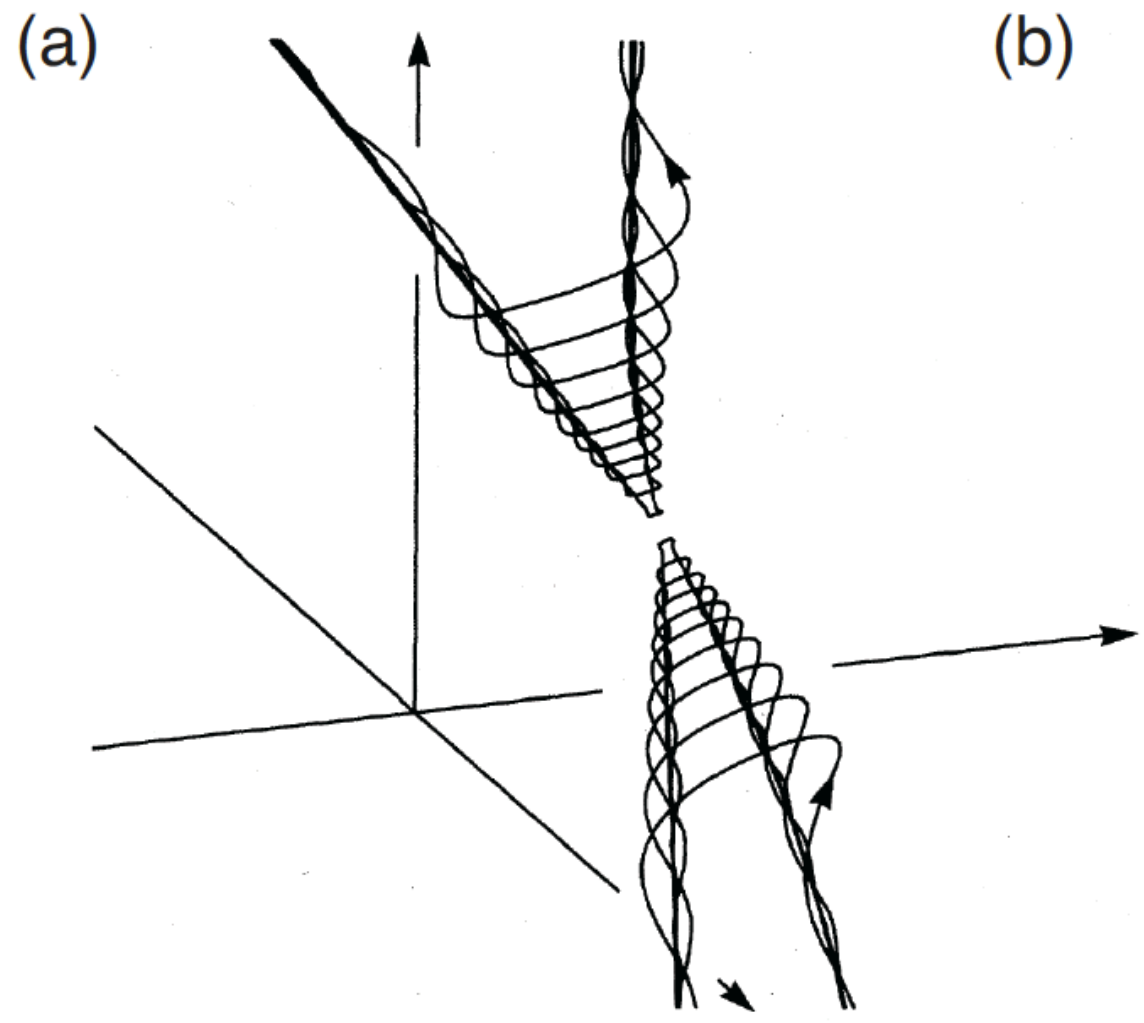
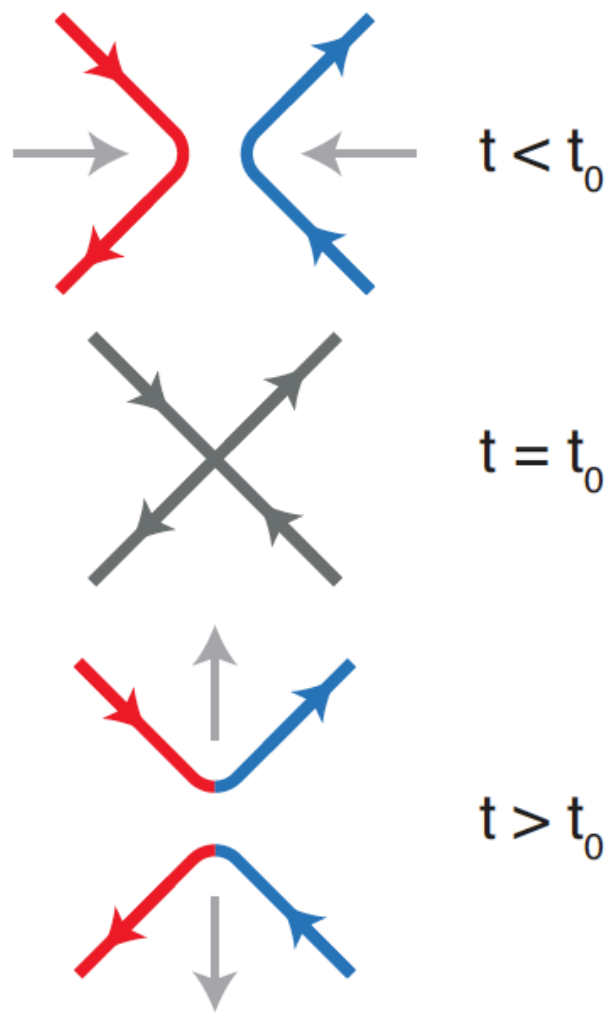
c may represent the affect of local strains

reconnection and ring collapse represented

NEARLY TIME REVERSIBLE!

M.S. Paoletti, M.E. Fisher, and D.P. Lathrop,
 "Reconnection dynamics for quantized vortices,"
 Physica D (2010)





Vortex Filament Models

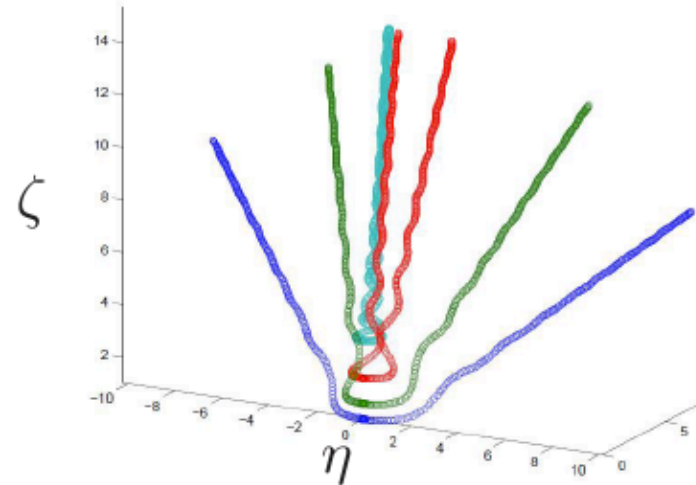
- Local Induction Approximation (LIA)

$$\frac{\partial \vec{s}(\sigma, t)}{\partial t} = \beta \frac{\partial \vec{s}(\sigma, t)}{\partial \sigma} \times \frac{\partial^2 \vec{s}(\sigma, t)}{\partial \sigma^2} + \alpha(T) \frac{\partial^2 \vec{s}(\sigma, t)}{\partial \sigma^2}$$

- LIA has one-parameter family of self-similar solutions in dimensionless similarity coordinates
- Adopt dimensionless similarity coordinates

$$\eta = (x - x_0) / \sqrt{\kappa(t - t_0)}$$
$$\zeta = (z - z_0) / \sqrt{\kappa(t - t_0)}$$

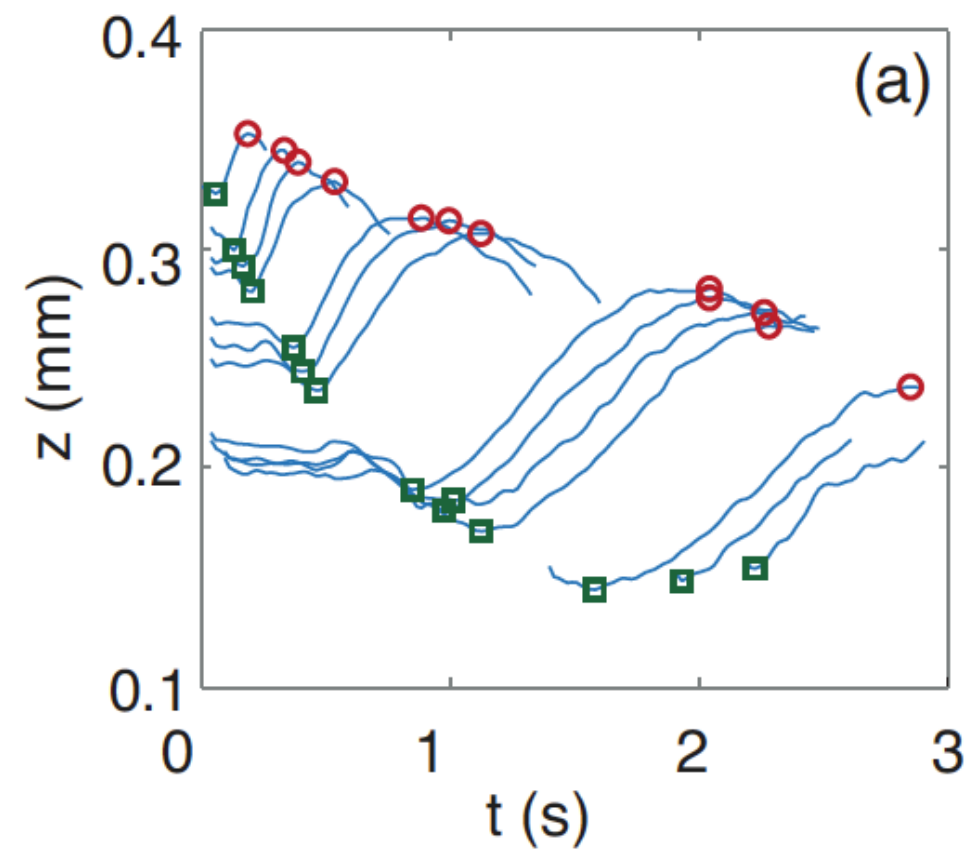
LIA Curves vs Vortex Angle



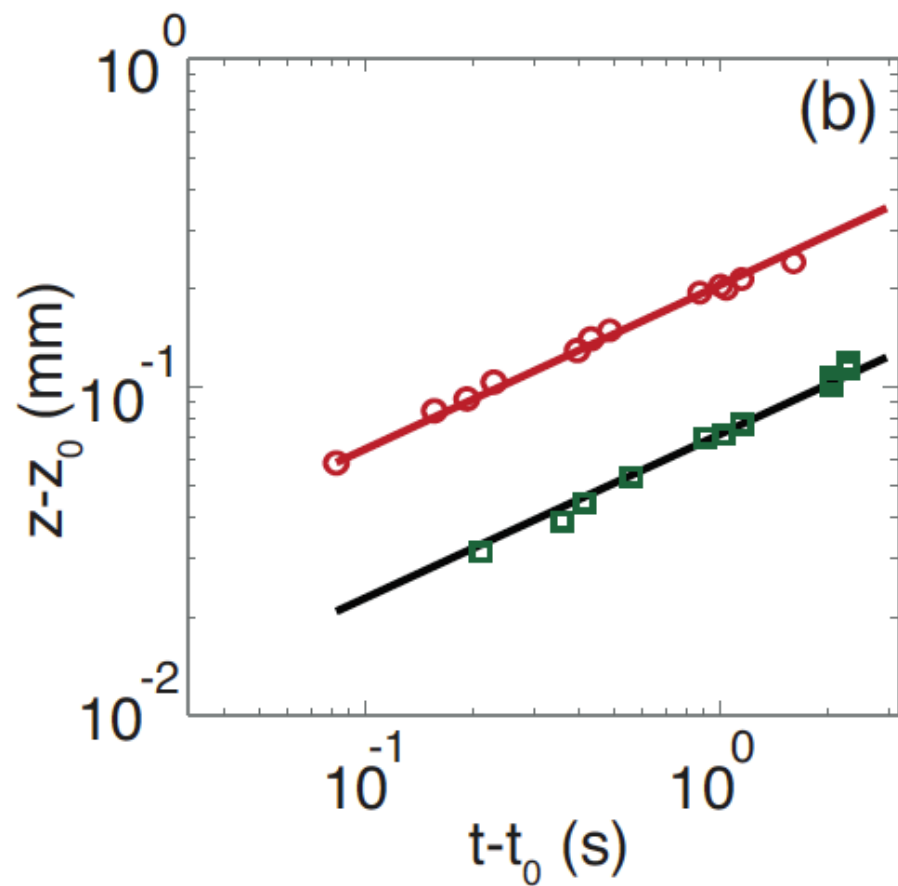
Eur. J. Mech. B - Fluids 19 (2000) 361-378

© 2000 Éditions scientifiques et médicales Elsevier SAS. All rights reserved
S0997-7546(00)00123-0/FLA

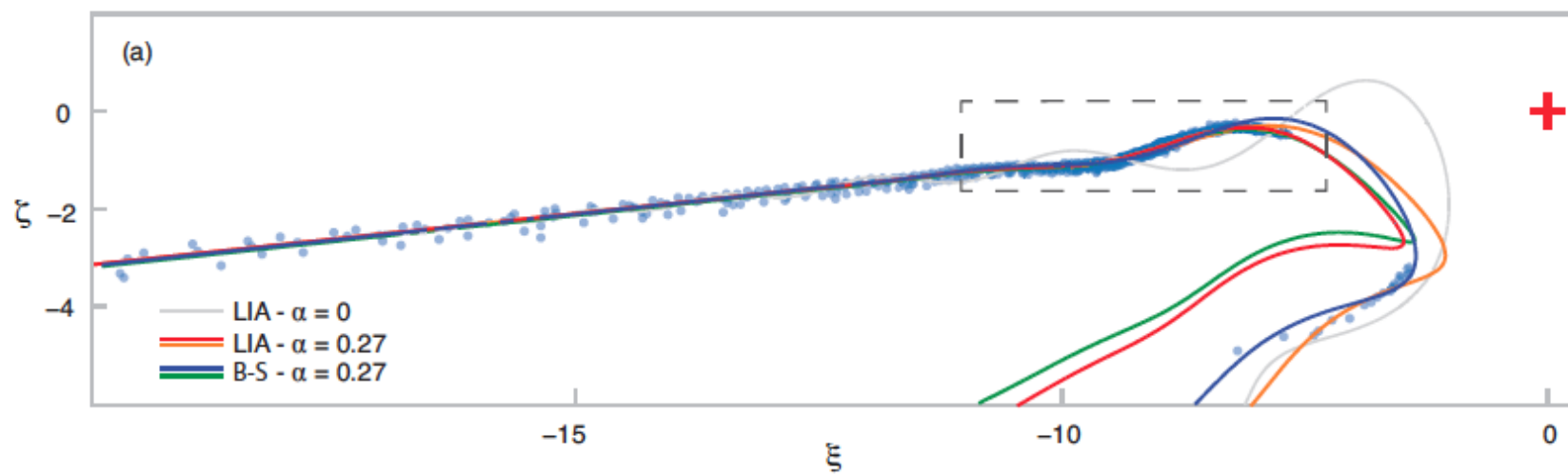
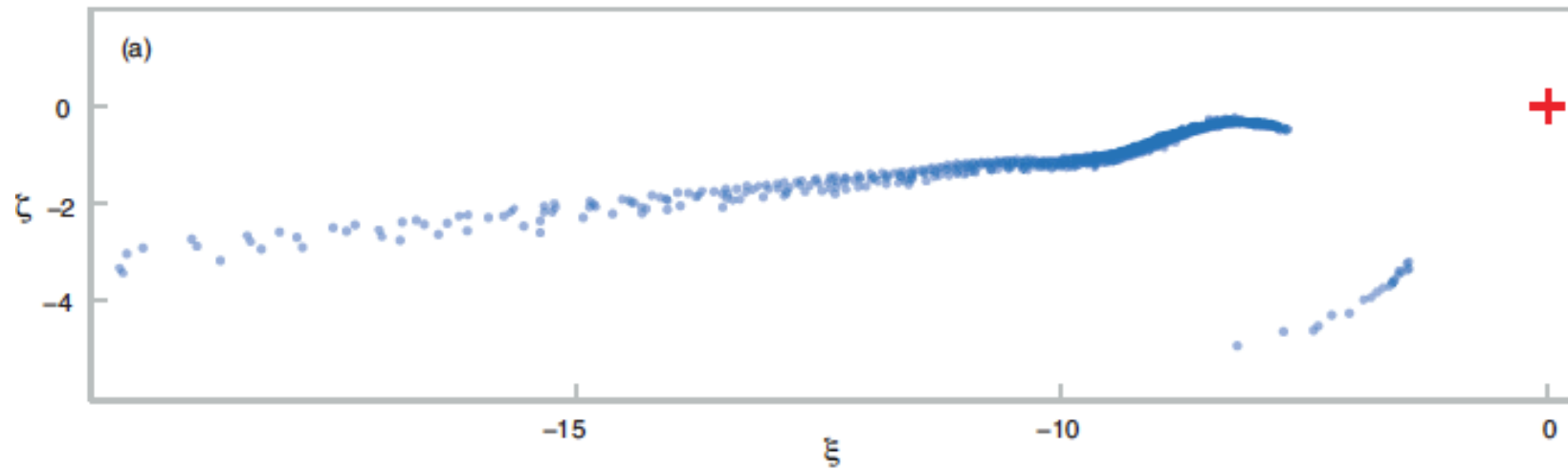
Evolution of quantum vortices following reconnection



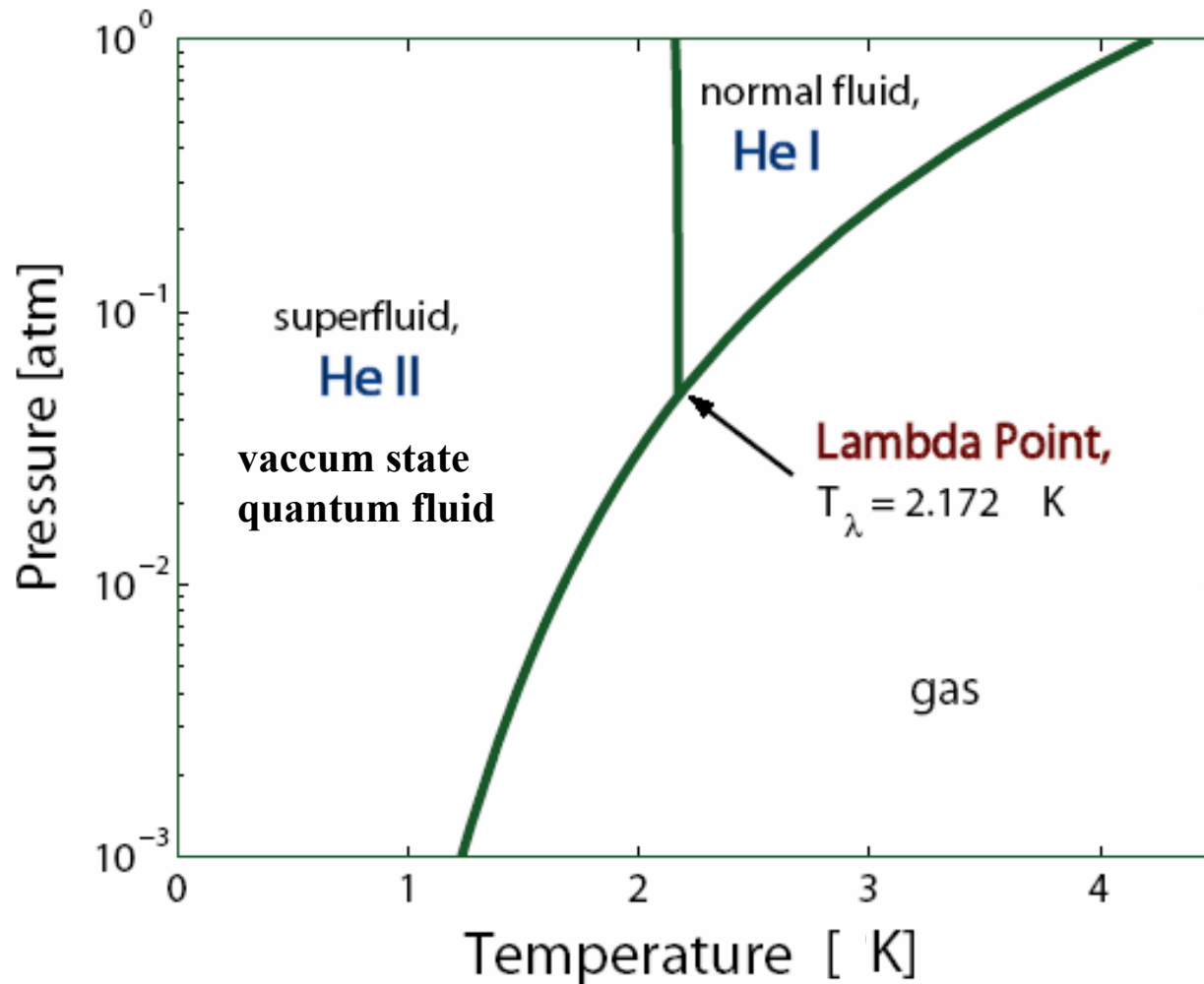
$$\xi = (x - x_0) / \sqrt{\kappa(t - t_0)}$$



$$\zeta = (z - z_0) / \sqrt{\kappa(t - t_0)}$$



Background: Superfluid Helium



Two-Fluid Model

- Order parameter for superfluid helium is a complex field,

$$\Psi(\mathbf{x}) = Ae^{i\phi}$$

A is amplitude,

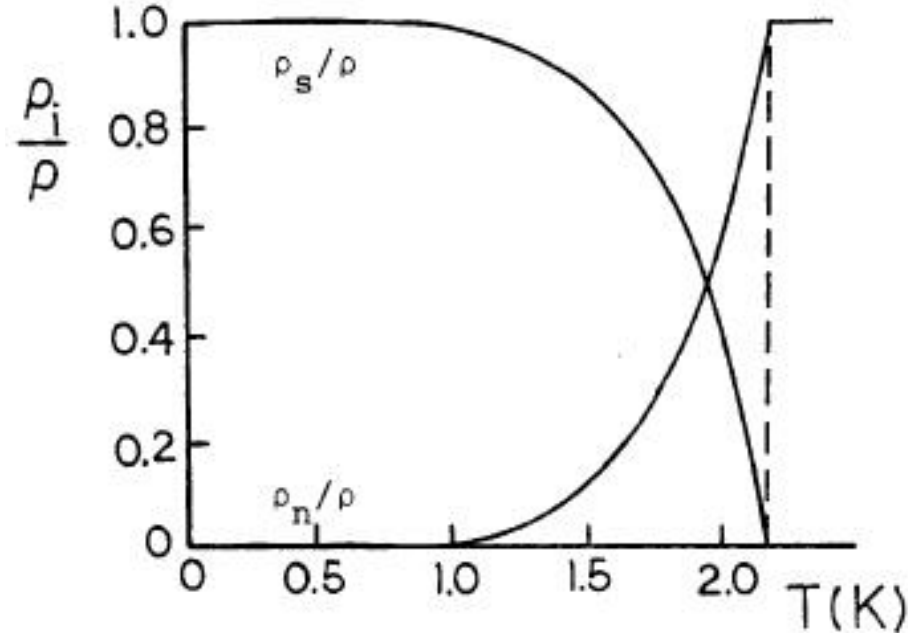
and ϕ is the phase

- Superfluid velocity given by

$$v_s = \kappa \nabla \phi \quad \kappa = \frac{h}{m}$$

h = Planck's constant

m = mass of helium atom



Circulation Quantization

Superfluid order parameter described by a complex field

$$\Psi = \sqrt{\rho(r)} e^{i\phi(r)}$$

Superfluid velocity field is the gradient of the wave function's phase

$$\vec{v}_s \propto \nabla\phi$$

Superfluid is an irrotational fluid in the bulk, but permits circulation around line-like phase defects called **quantized vortices**



$$\zeta \sim 1 \text{ \AA}$$

$$\omega = \nabla \times \vec{v}_s = \nabla \times (\nabla\phi(r)) = 0$$

Vorticity Vanishes

$$\Gamma = \oint_C \vec{v} \cdot d\vec{l} = \oint_C \kappa \nabla\phi(r) \cdot d\vec{l} = \kappa\Delta\phi = (2\pi n)\kappa \quad \text{Circulation Quantized}$$

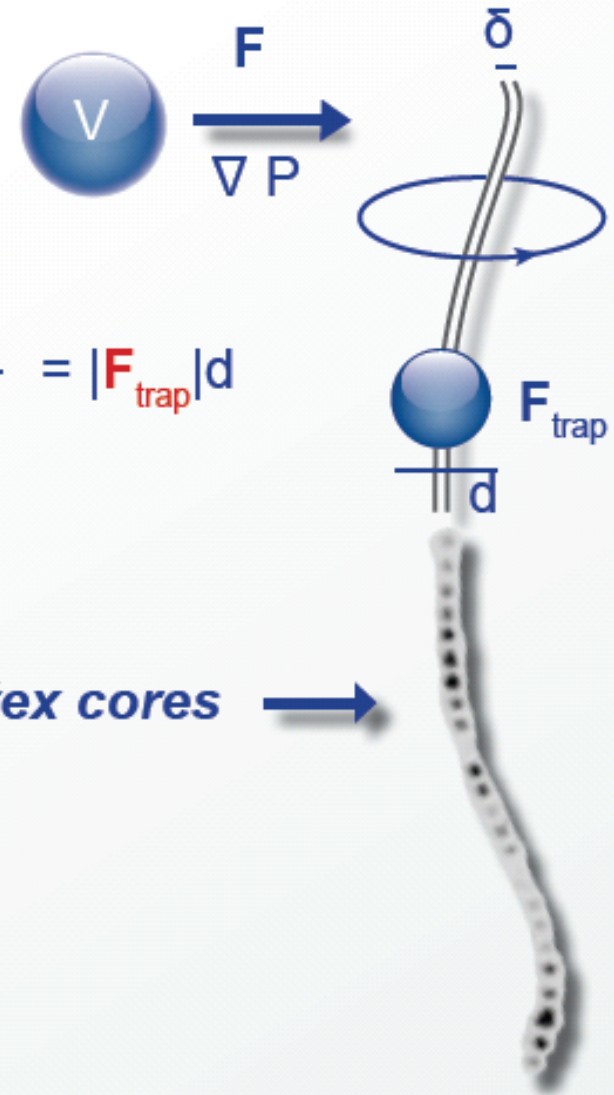
$$\kappa = h/m_{He} \approx 9.97 \cdot 10^{-8} \text{ m}^2/\text{s}$$

$$n = 0, 1, 2 \dots$$

Visualization of vortices - particle trapping

$$P = -\frac{\rho_s K^2}{8\pi^2 r^2}$$

$$\mathbf{F} = \oint_{\partial\Omega} P \hat{n} dA$$



Decrease of energy $\Delta\varepsilon = \frac{\rho_s K^2}{4\pi} d \ln \frac{d}{2\delta} = |\mathbf{F}_{\text{trap}}| d$

$$\frac{\mathbf{F}_{\text{trap}}}{V} \propto \frac{\ln d}{d^3}$$

Particles get trapped on vortex cores →

Ions in liquid He $\ominus 16 \text{ \AA}$ $\oplus 6 \text{ \AA}$

Parks and Donnelly (1966), Williams and Packard (1974)

Solid hydrogen particles $> 1 \mu\text{m}$

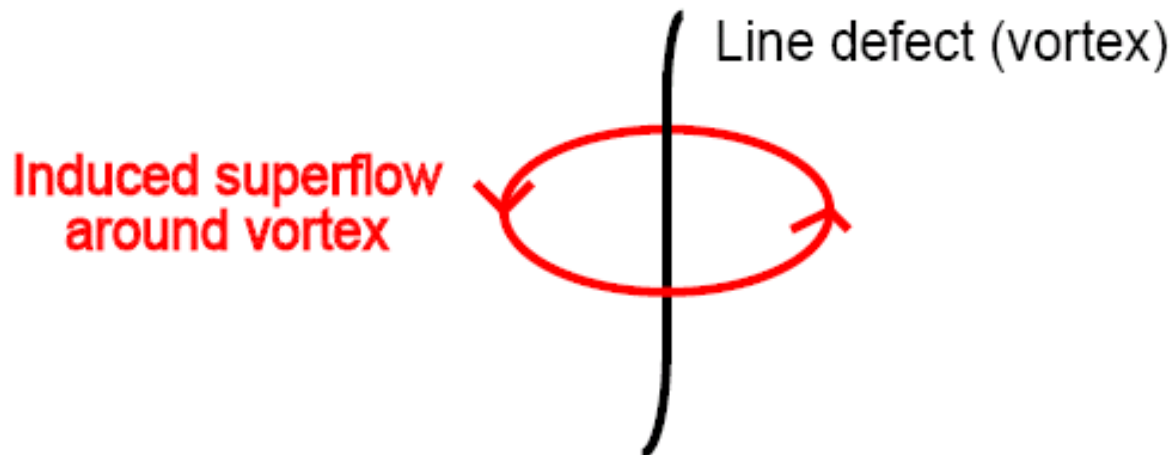
Bewley, Lathrop, Sreenivasan, Nature 441 588 (2006)

Quantized Vortices

- Lowest energy state: $n=1$, so ϕ wraps 2π around a defect
- Induces a superflow around the line:

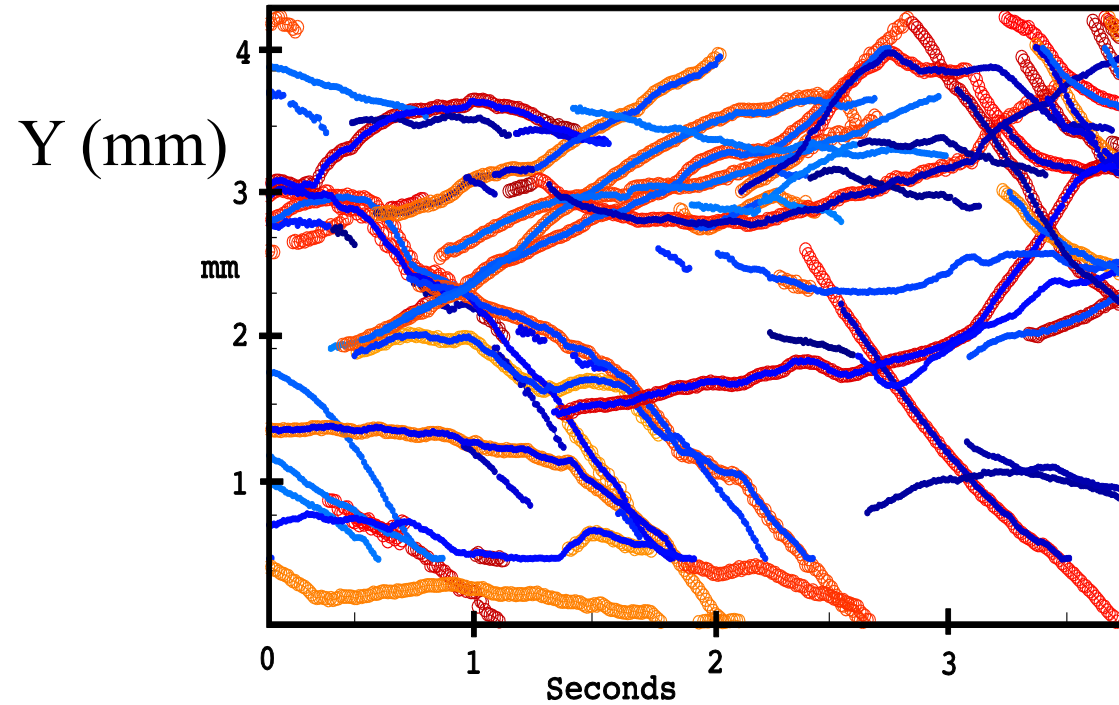
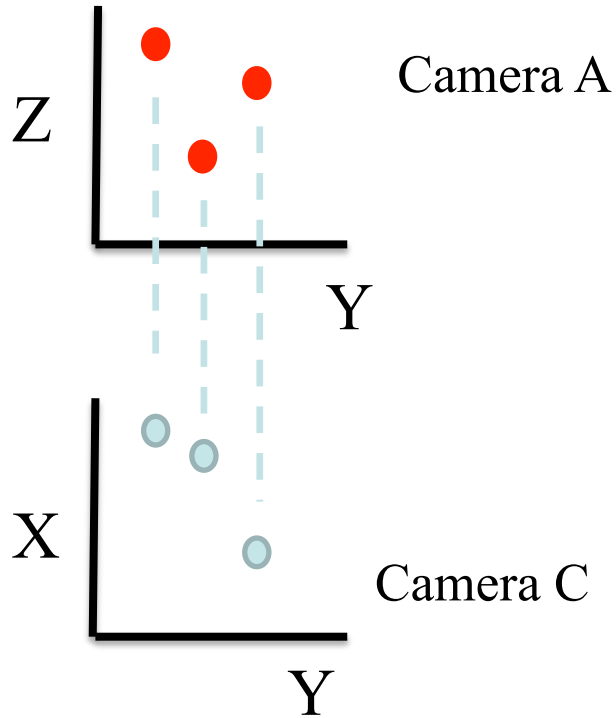
$$\mathbf{v}_\Phi = \frac{\mathbf{K}}{r}$$

s is distance from defect

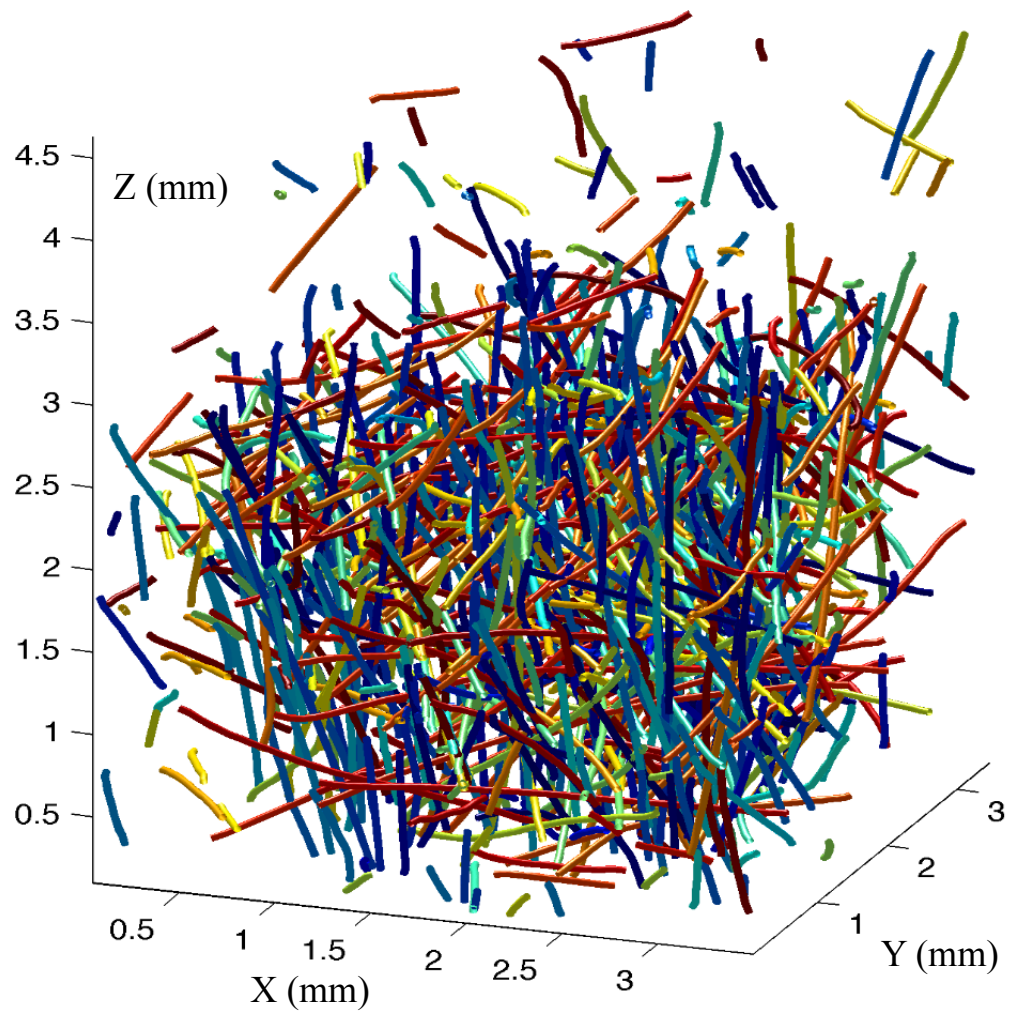


3D Stereomatching

3D trajectory reconstruction requires identifying particles mutually between two cameras



- 'Shared' coordinate between two cameras
- Normalized distance between tracks used to stereomatch



Single Particle Tracks in 3D

Rendering code by
Nick Ouellette