

Superfluids and superconductors in confinement

Anton Vorontsov



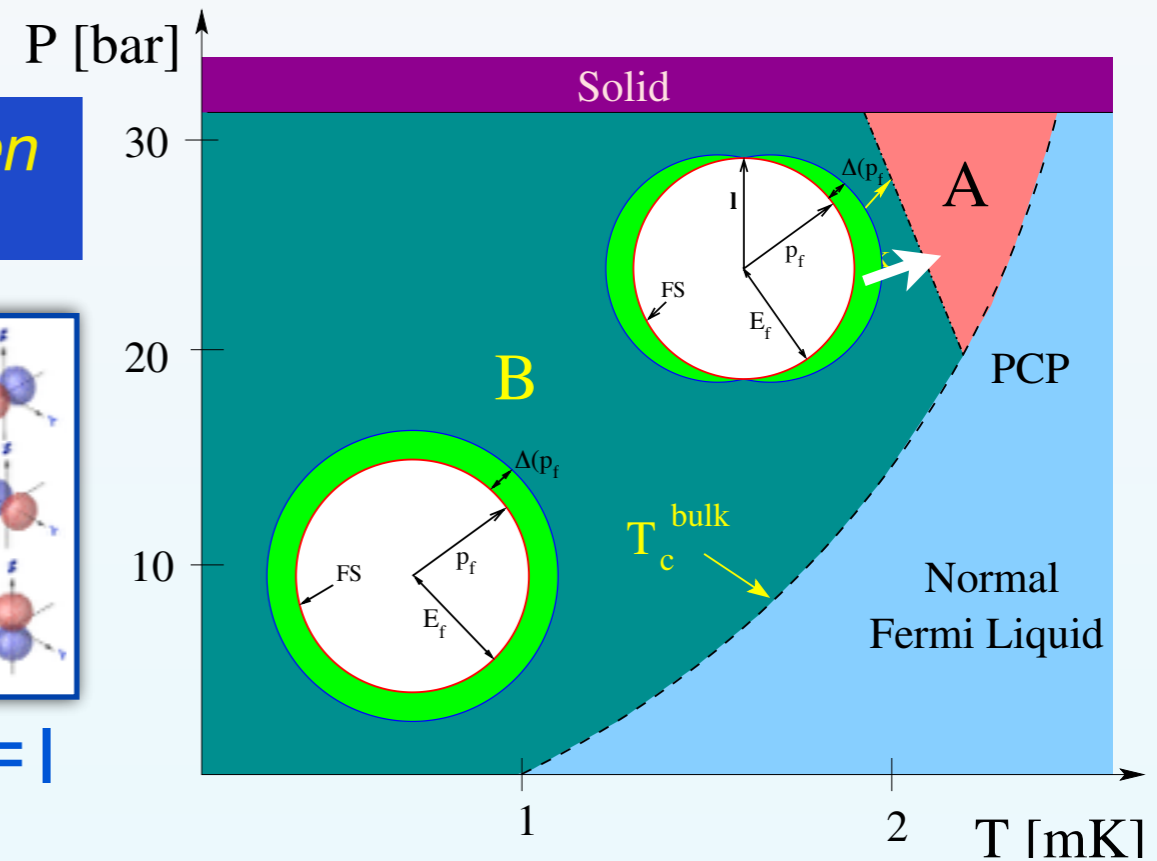
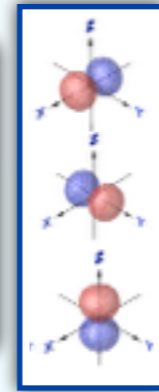
***DMR-0954342
CAREER***

Superfluid ^3He

► Multi-component (18) Order Parameter with Broken Spin- Orbital and Gauge Symmetries.

$$\left(\begin{array}{c} | \uparrow\uparrow \rangle \\ \frac{1}{\sqrt{2}} | \uparrow\downarrow + \downarrow\uparrow \rangle \\ | \downarrow\downarrow \rangle \end{array} \right) = \left(\begin{array}{ccc} A_{xx} & A_{xy} & A_{xz} \\ A_{yx} & A_{yy} & A_{yz} \\ A_{zx} & A_{zy} & A_{zz} \end{array} \right)$$

$S=1$ $L=1$



Normal State Symmetry:

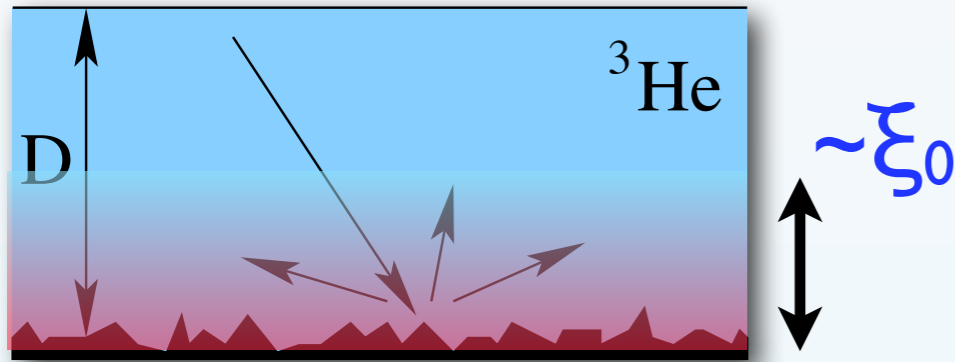
$$G_N = U(1) \times SO(3)_L \times P \times SO(3)_S \times \mathcal{T}$$

gauge orbital parity spin time reversal

One of the most sophisticated and successful Condensed Matter Systems:

- ◆ unconventional BCS pairing
- ◆ multiple condensed phases
- ◆ complex broken symmetries
- ◆ interactions: FL, dipole-dipole, ...
- ◆ topological properties

Surface states in ^3He



Normal State Film:

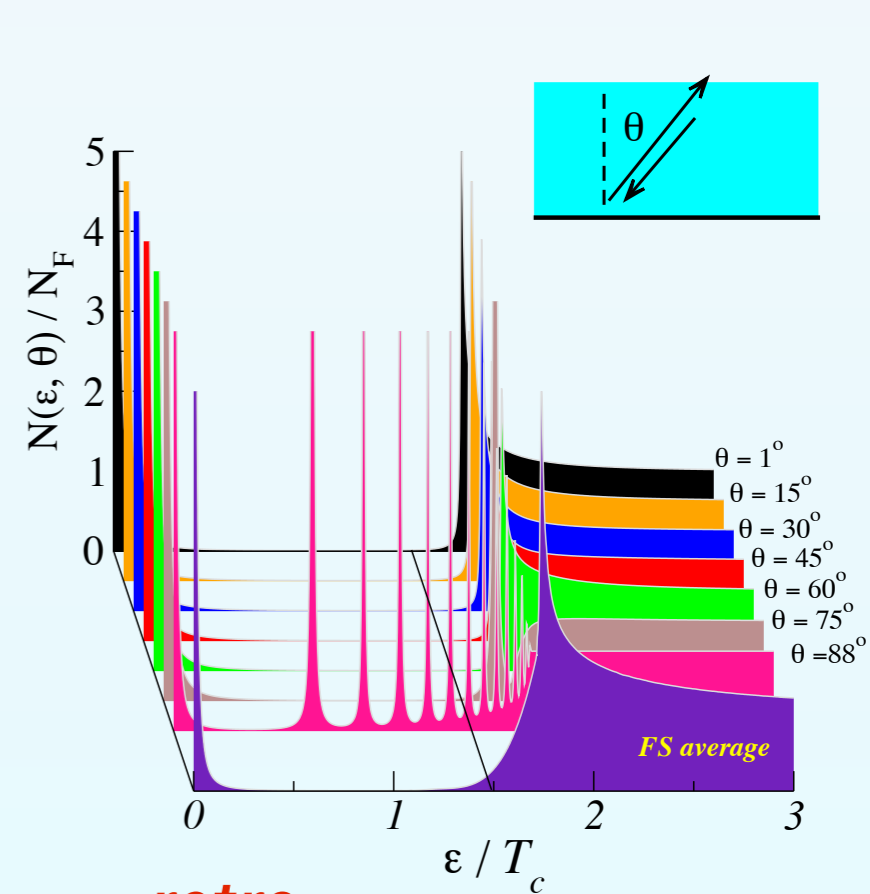
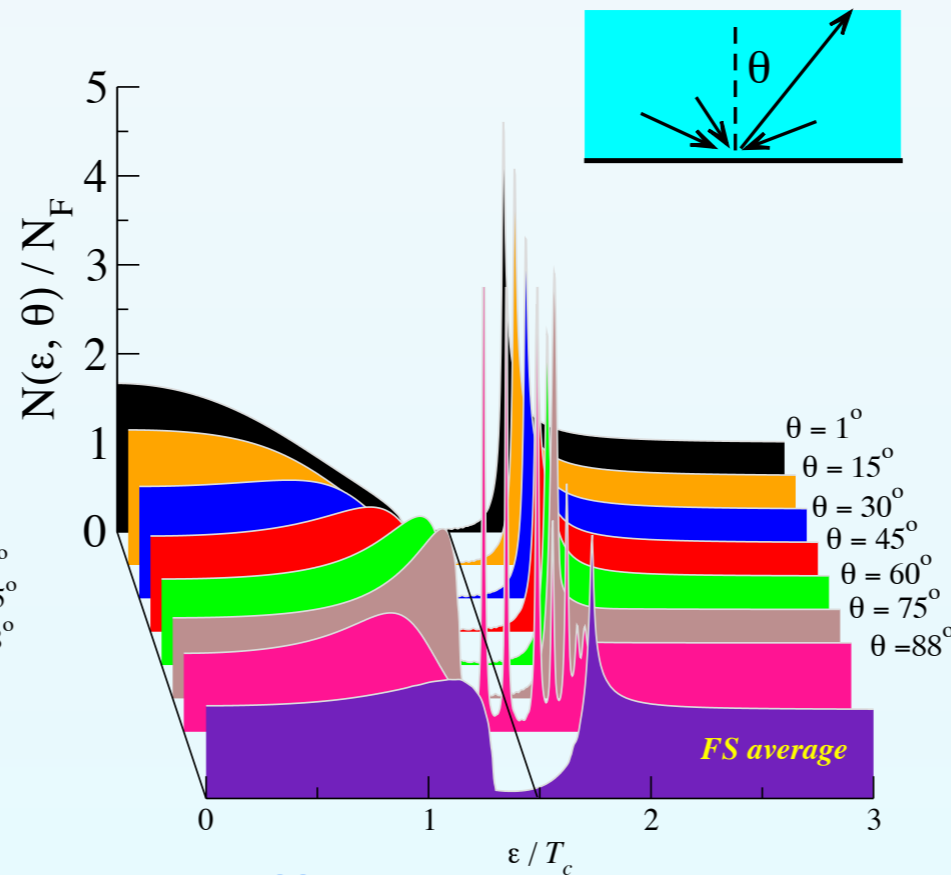
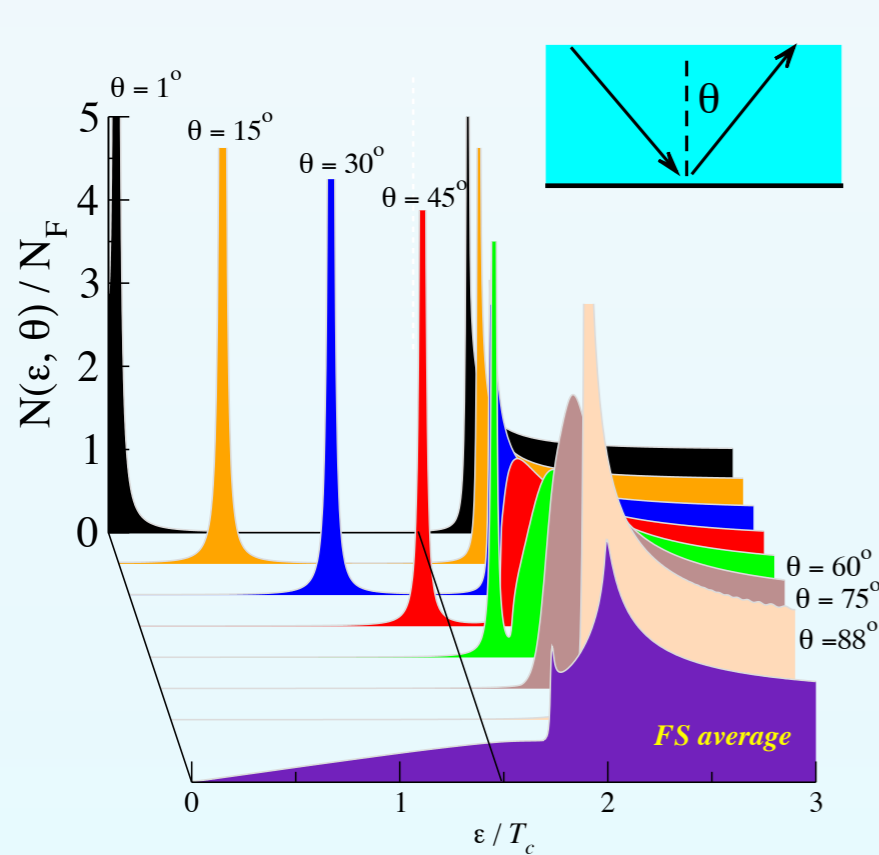
$$G_N = U(1) \times [U(1)_{Lz} \times \mathcal{R}_x \times \mathcal{R}_y] \times SO(3)_s \times \mathcal{T}$$

gauge

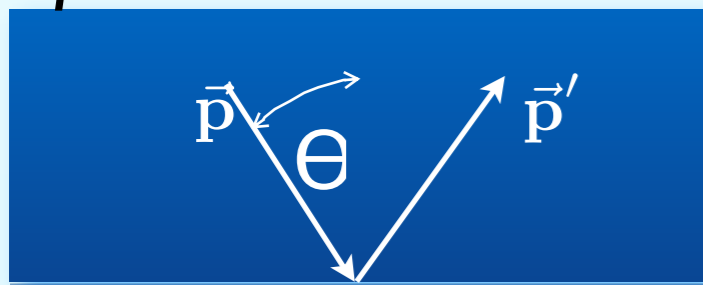
orbital rotations
and reflections (\mathcal{R})

spin

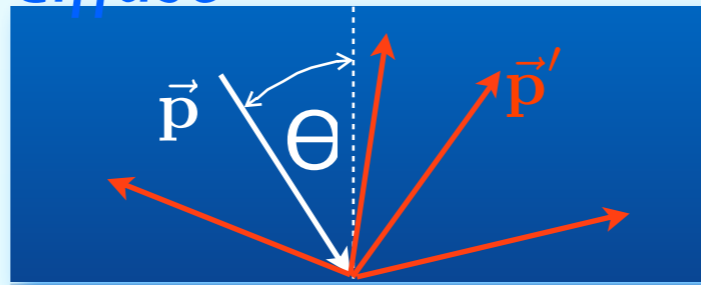
time
reversal



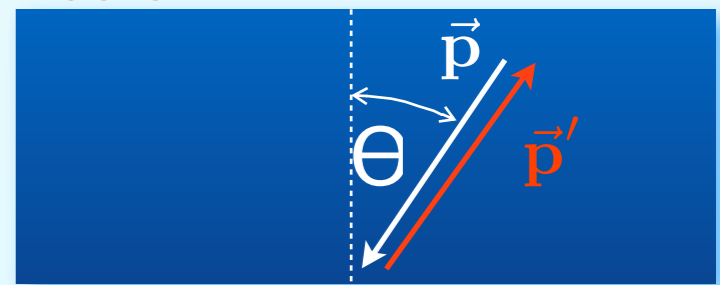
specular



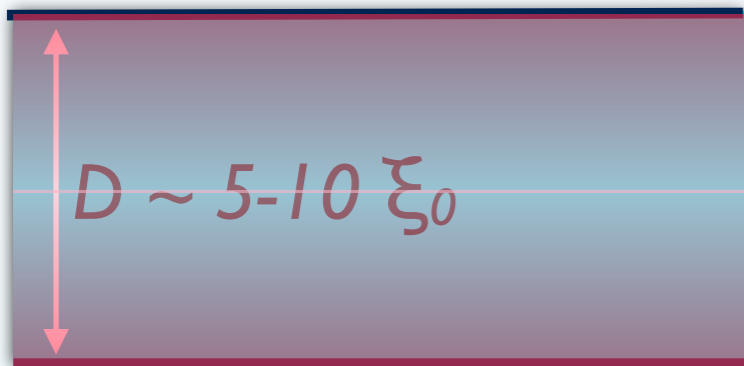
diffuse



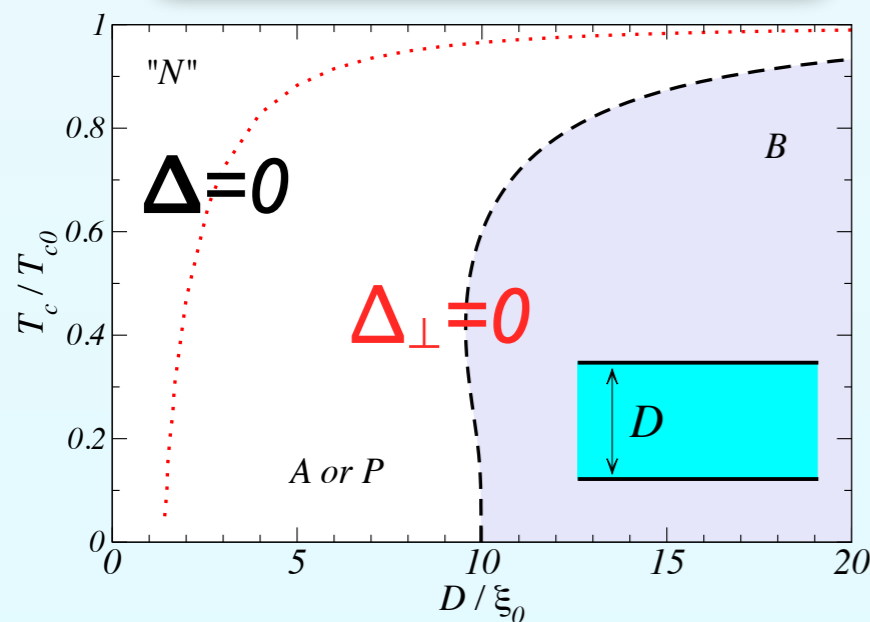
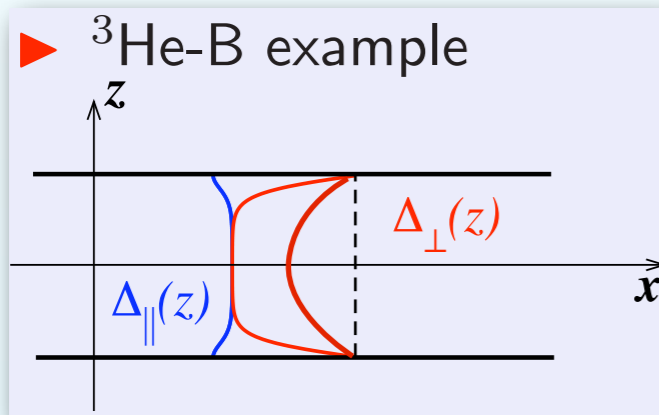
retro



Superfluid in confinement



$$\xi_0 = \frac{\hbar v_f}{2\pi T_c} \approx 20 - 80 \text{ nm}$$



▶ *surface states dominate the volume of the sample*

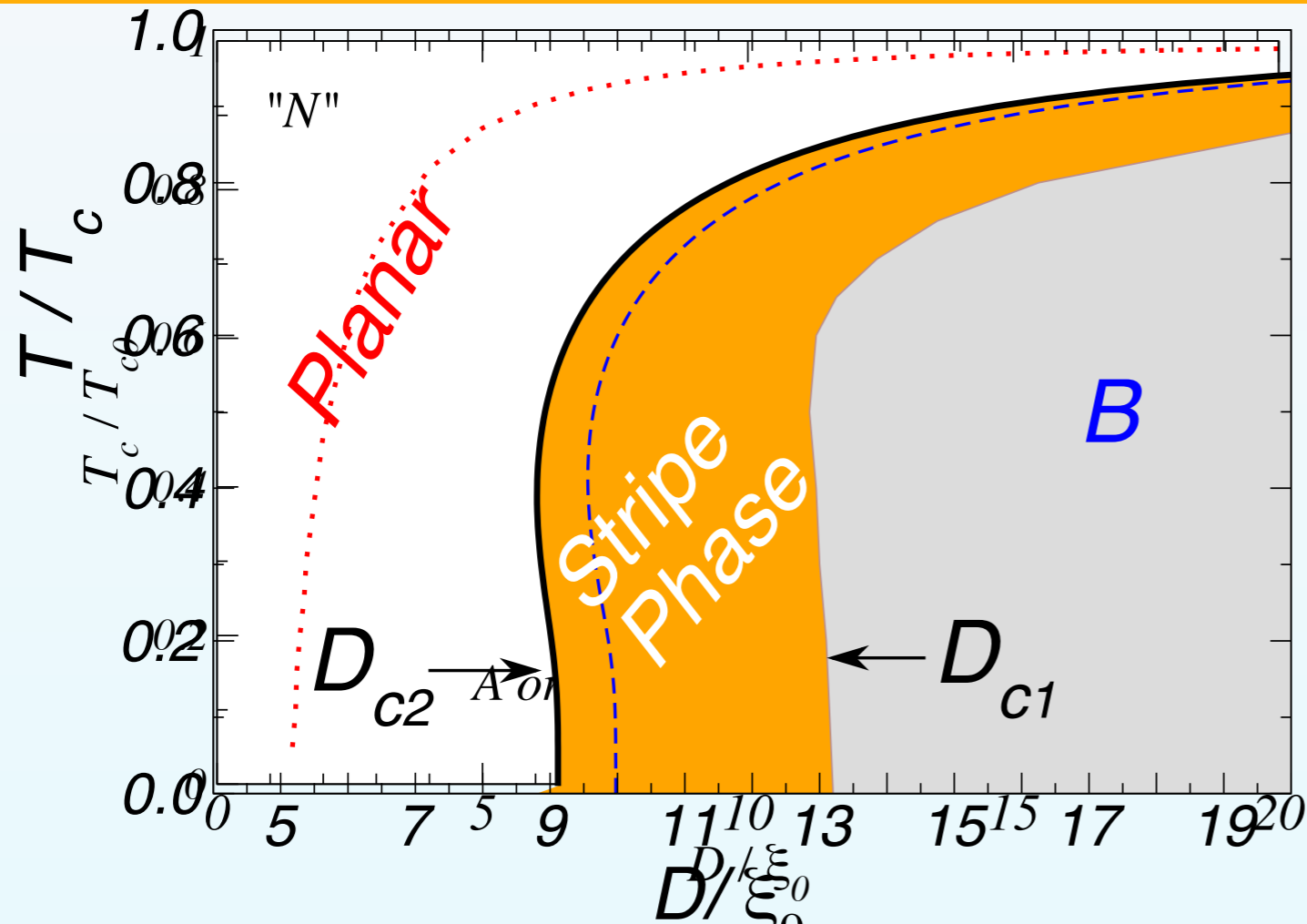
- ▶ *Surface states interactions, non-local physics (∇)*
- ▶ *Suppression of Order Parameter: 'non-bulk' quasiparticle spectrum, new energy landscape*
- ▶ *Confinement driven transitions B-A, A-Normal*
- ▶ *Completely new OP configurations, phases with new symmetry properties*

▶ **Control of Geometry & Spatial dimensions:**

- ▶ *Insight into pairing symmetries*
- ▶ *New phases*
- ▶ *New ways to access surface states: study and manipulation*
- ▶ *New technological devices*

Superfluid He-3 films

Confinement driven transition : *Stripe* phase



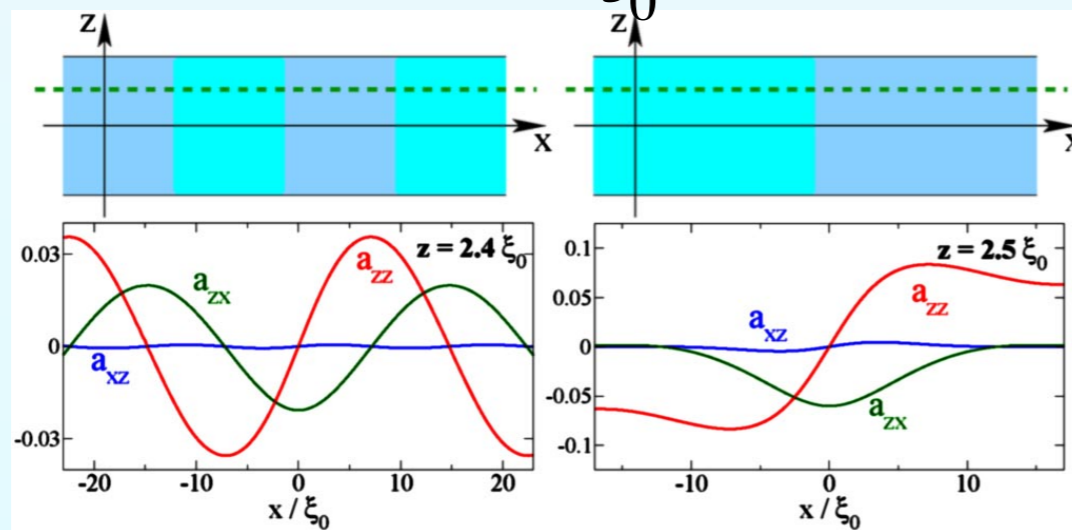
* Transition is driven by **re-structure of quasiparticle spectrum** due to OP component suppression

Hara, Nagai, Prog Theor.Phys 1986

* Spontaneously Broken Translation Symmetry in the x-y plane of the film

- Competition of gradient and condensation energies
- Multiple “domain wall” configurations stabilized by the boundary conditions

Salomaa, Volovik PRB 1988
Vorontsov, Sauls JLTTP 2005



Vorontsov, Sauls, PRL 2007

New phases in other geometries

► Chiral $^3\text{He-A}$ ribbon

Hao Wu, J. Sauls

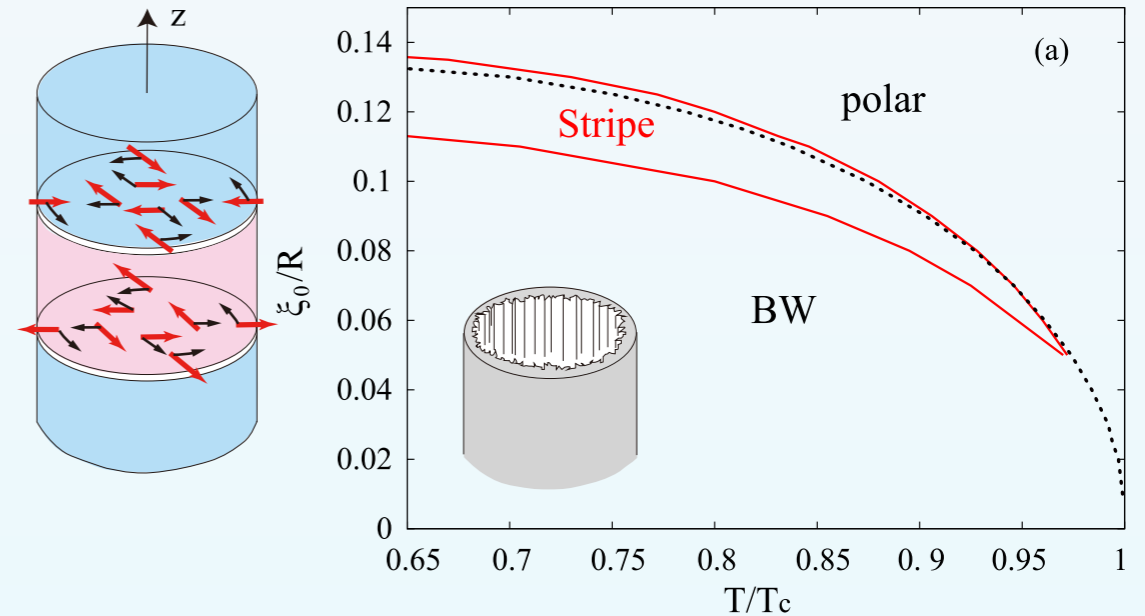
QFS'15 talk Aug 15, 9:40am

- ↳ Stripe order in multi-component OP
- ↳ Domain walls with non-trivial bound states and mass currents

► Cylindrical pores

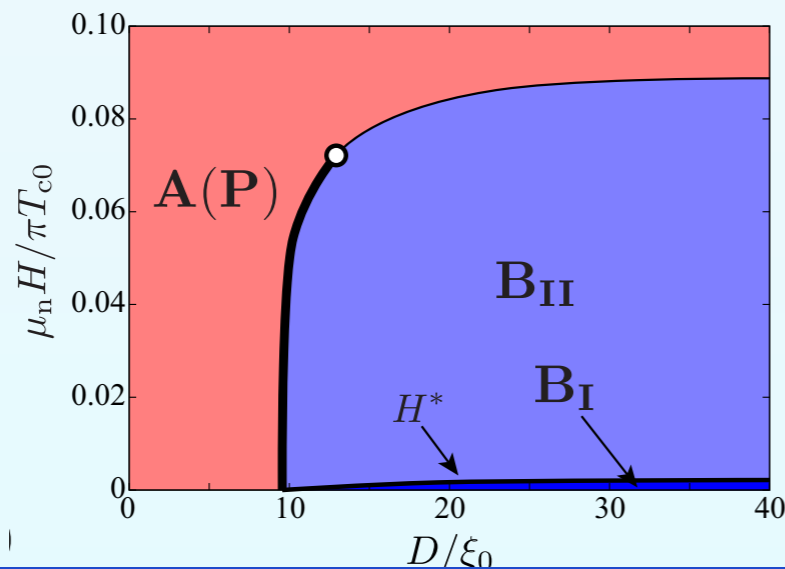
K. Aoyama, PRB 2014

QFS'15 talk Aug 14 9am



► Superfluid He-3 in magnetic field

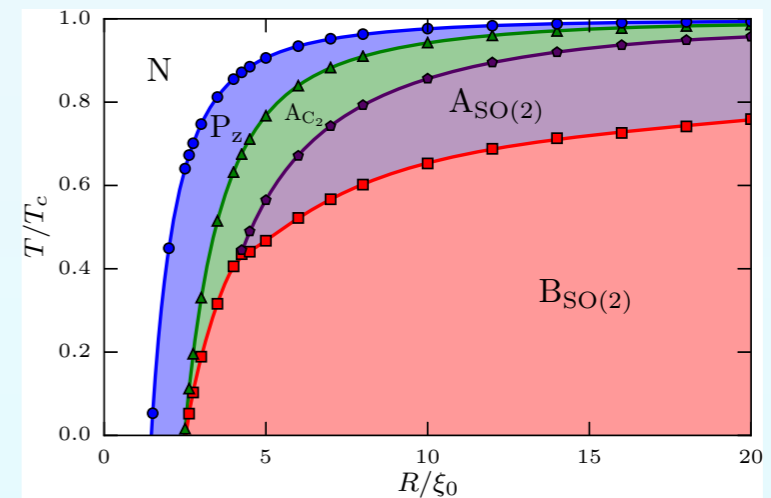
T. Mizushima



- ↳ Additional symmetries
- ↳ Protected topological phase in small B

J. Wiman, J. Sauls

QFS'15 posters

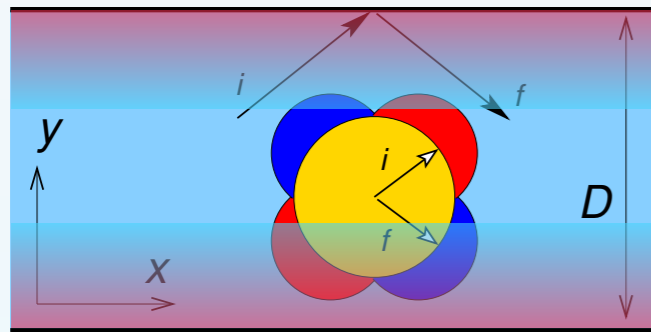


- ↳ Several new phases
- ↳ "Spiral" order

Spontaneous currents

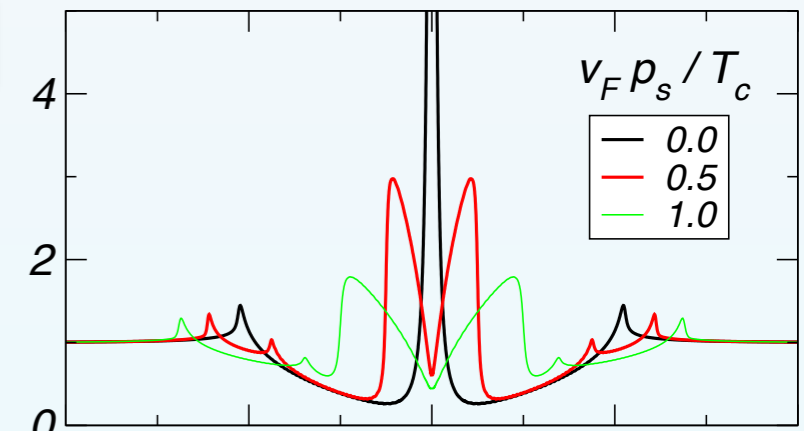
d-wave condensates

Energy gain due to shift of the bound states from zero energy $\epsilon \Rightarrow \epsilon - v_F p_s$

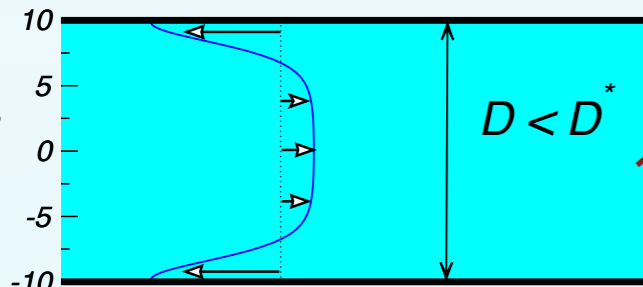


Zero-energy ABS

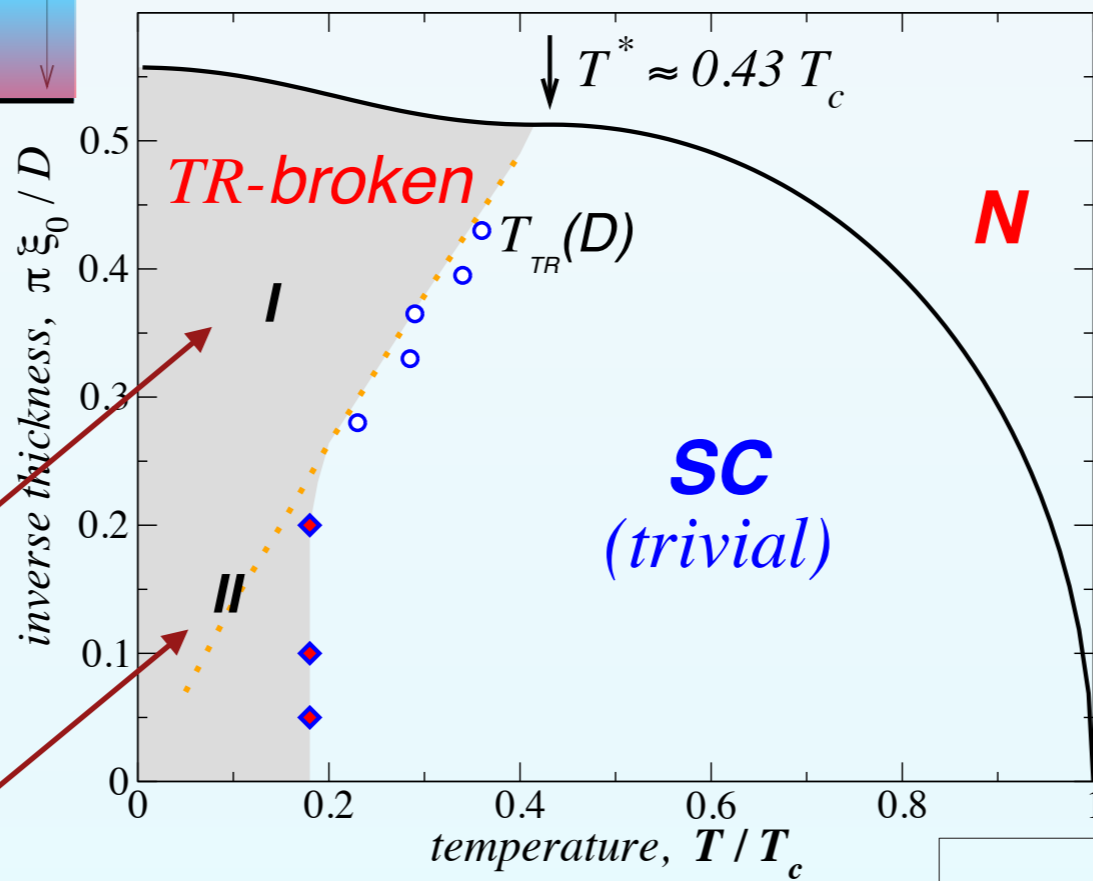
$$p_{sy} = \pi/D$$



Vorontsov, PRL 2009

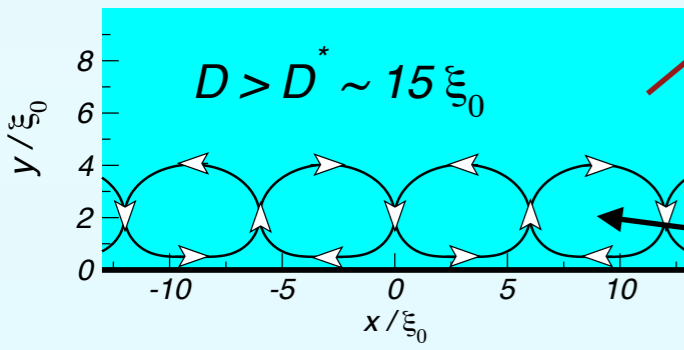


$D < D^*$



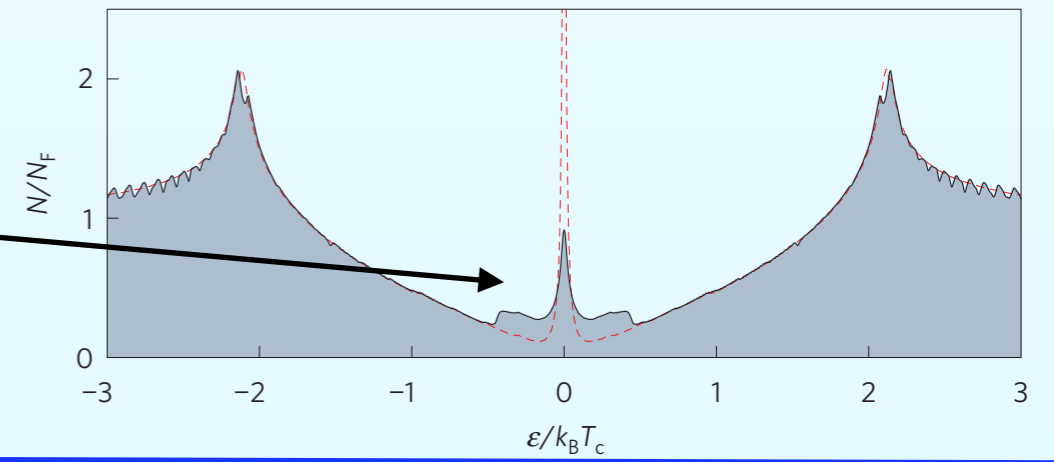
* Spontaneously Broken Time-Reversal symmetry

More complicated bound states structure



$D > D^* \sim 15 \xi_0$

non-local ABS interaction



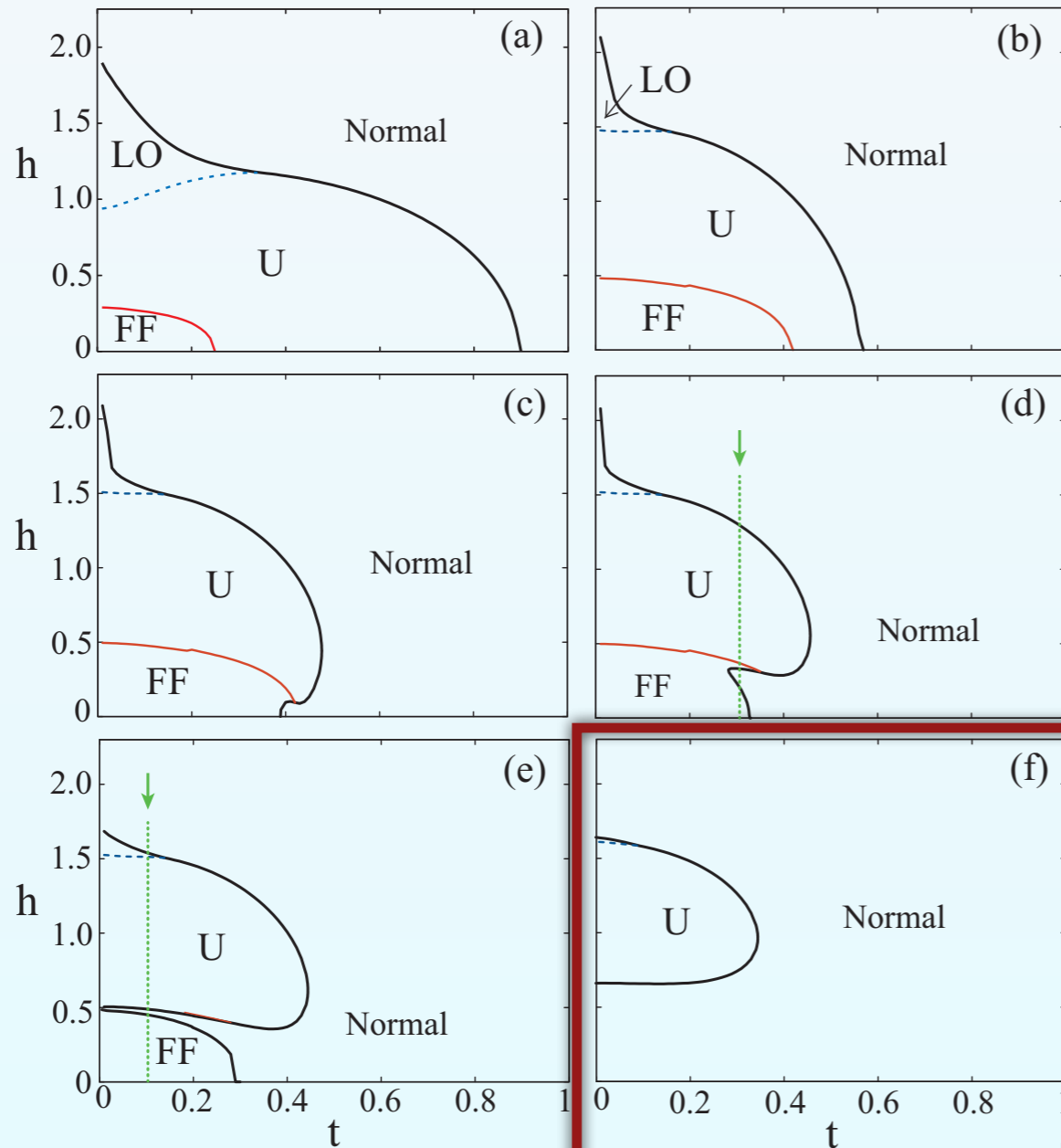
Hakansson et al, Nature Physics 2015

Re-entrant superconductivity

$D/\pi\xi_0=3.33$

M. Hachiya, PRB 2013

Magnetic field

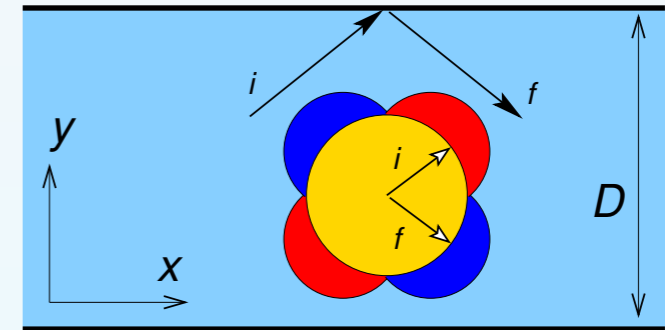


Temperature

$D/\pi\xi_0=1.79$

Confined geometry with Zeeman magnetic field:

$$\varepsilon \Rightarrow \varepsilon - v_{FF} p_s - \mu_B H$$



$\longrightarrow H$

Zeeman magnetic field:
Fulde-Ferrell-Larkin-Ovchinnikov state

- \hookrightarrow Real OP modulations, Currents, 'Uniform' phases
- \hookrightarrow Re-entrant superconductivity
- \hookrightarrow Induced by magnetic-field

Grand Challenge 1

New phases are everywhere!

- *WHERE* are they?

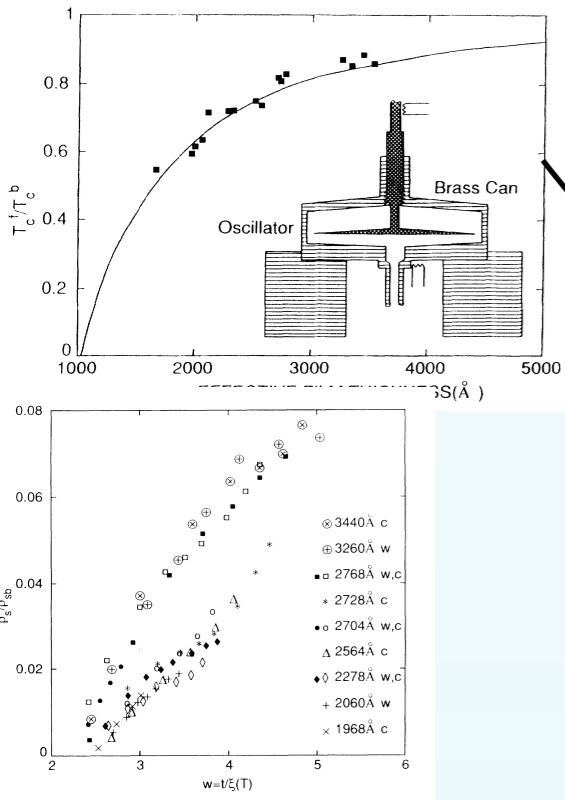
Prediction of signatures of bound states (surfaces and domain walls) and of new phases :

magnetic properties
connection to Majorana and Weyl quasiparticles
transport & non-equilibrium properties
condensate dynamics

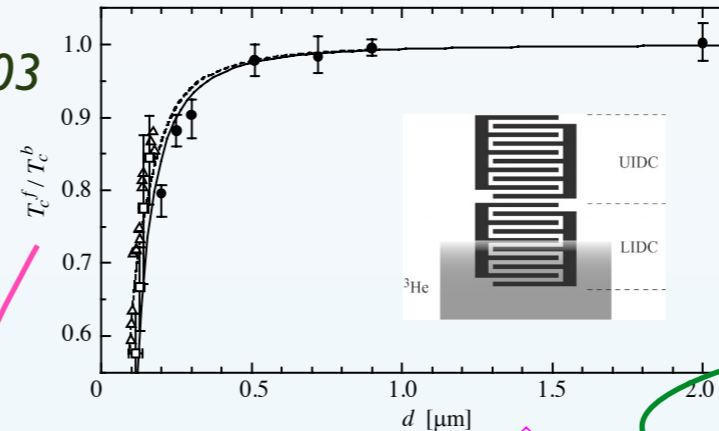
Experimental challenges and development of new techniques: *low T, small volume, high B, surface physics*

³He thin films: experiments

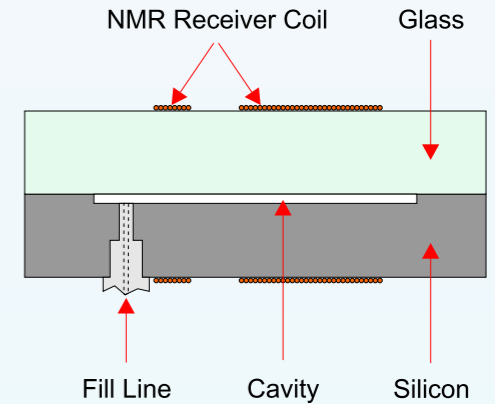
Xu, Crooker 1990



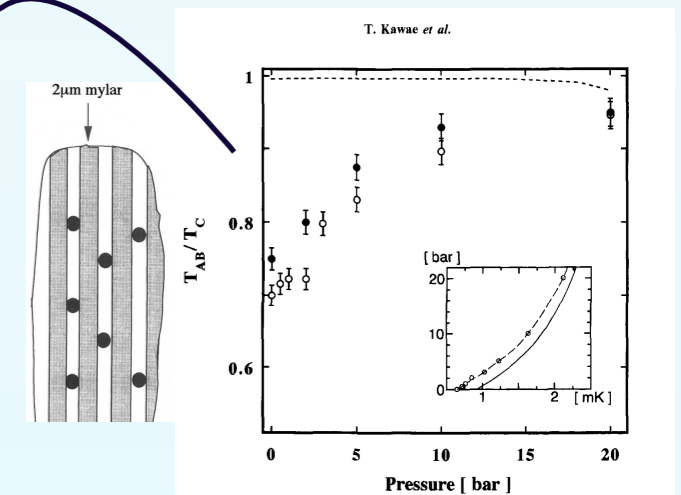
Saitoh et al 2003



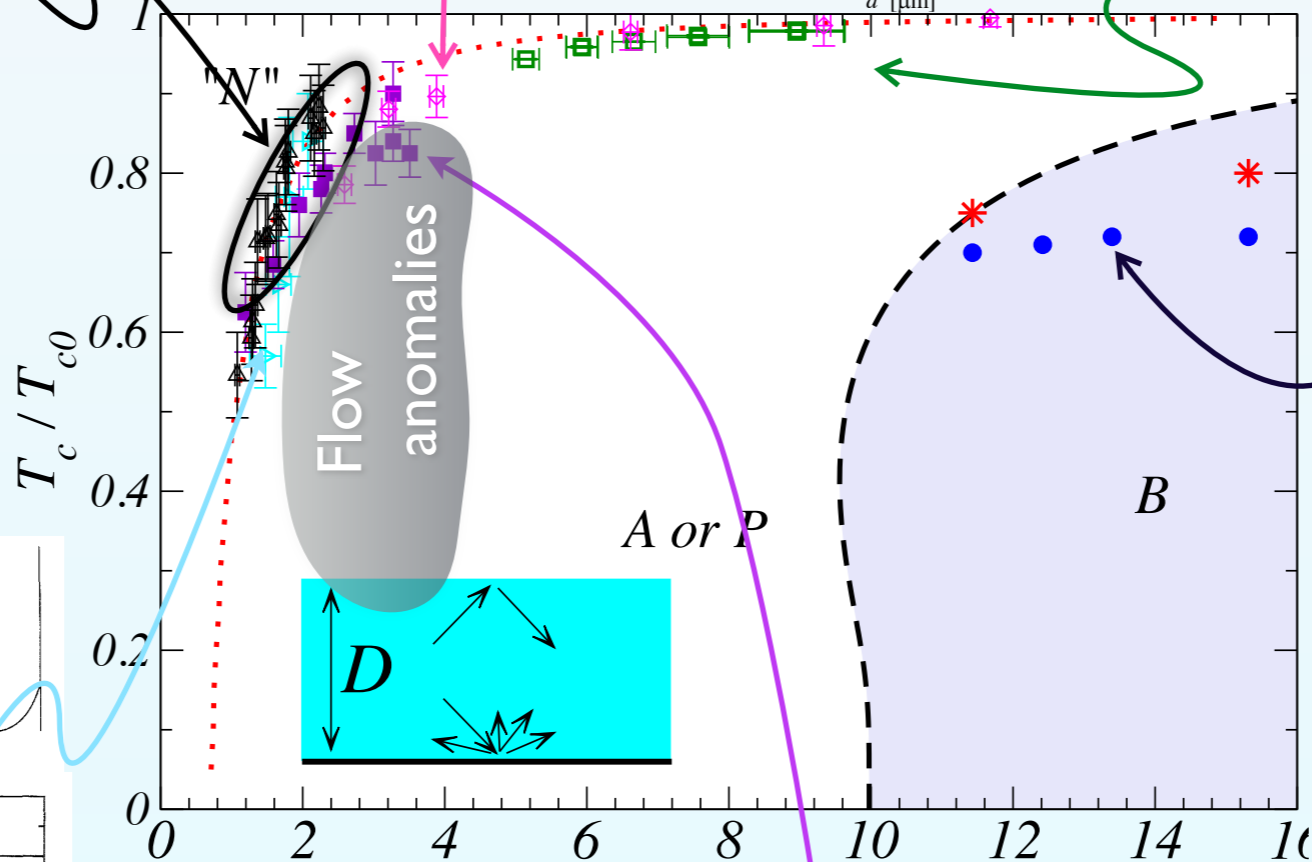
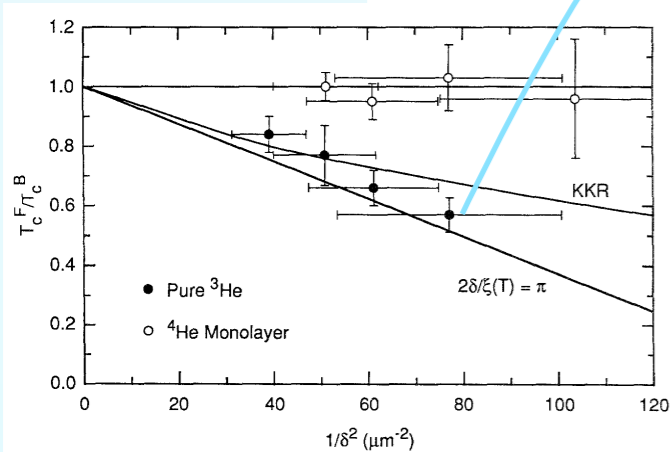
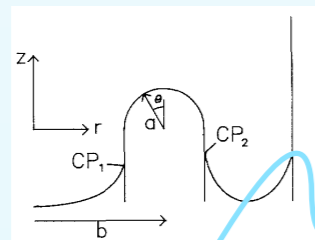
RHUL NMR 2010-2012



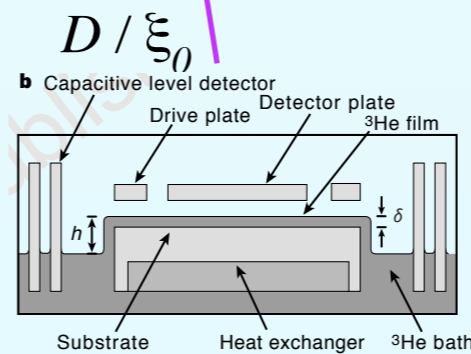
Kawae et al NMR 1998



Steel et al 1994



Schechter et al 1998 3rd sound



Flow anomalies: below $\sim 4\xi_0$
 - Davis 1988
 - Steel 1994
 - Schechter 1998

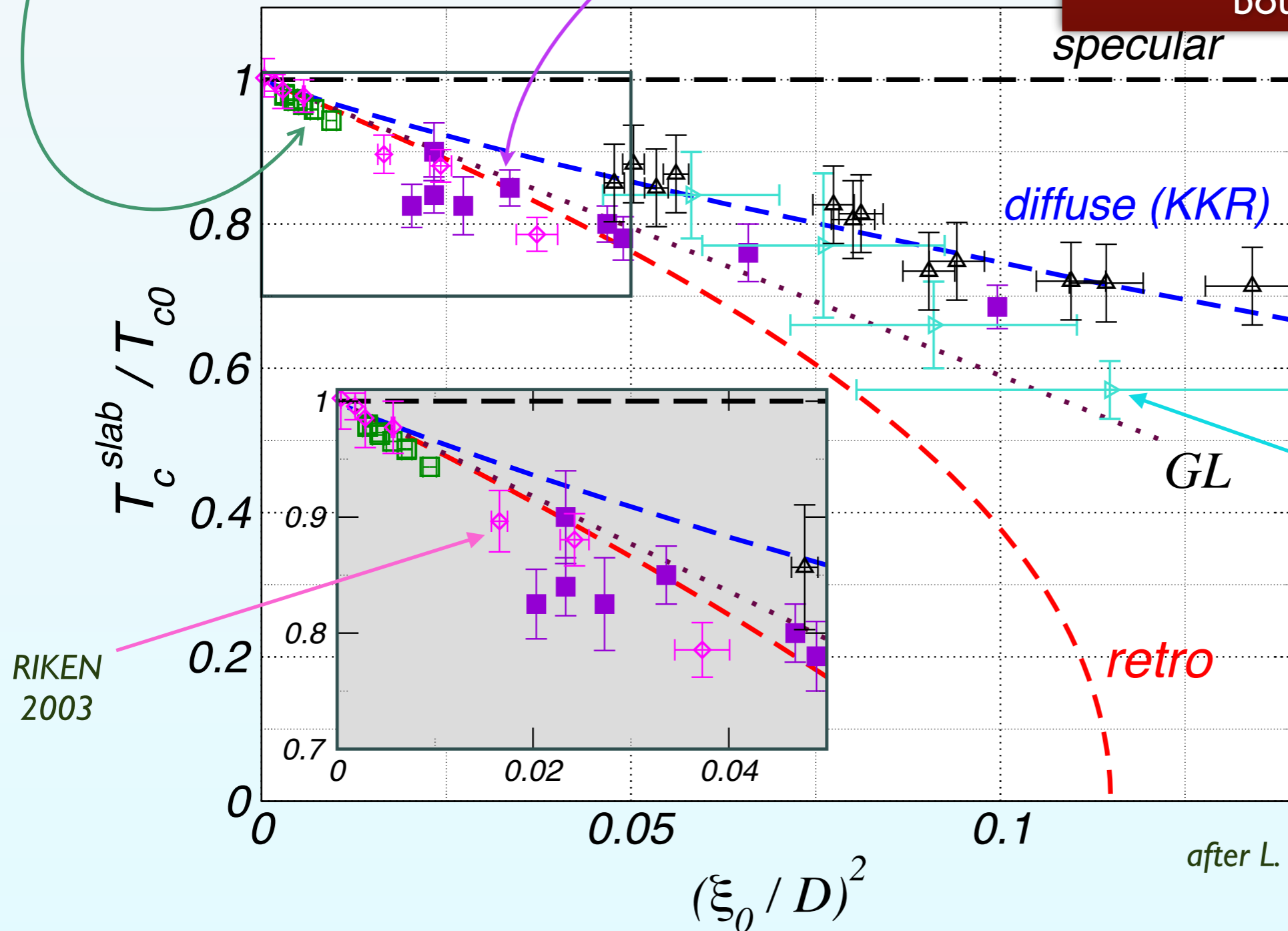
T_c suppression

RHUL NMR
Levitin et al
2010-2012

Berkeley, 3rd sound
Schechter et al
1998

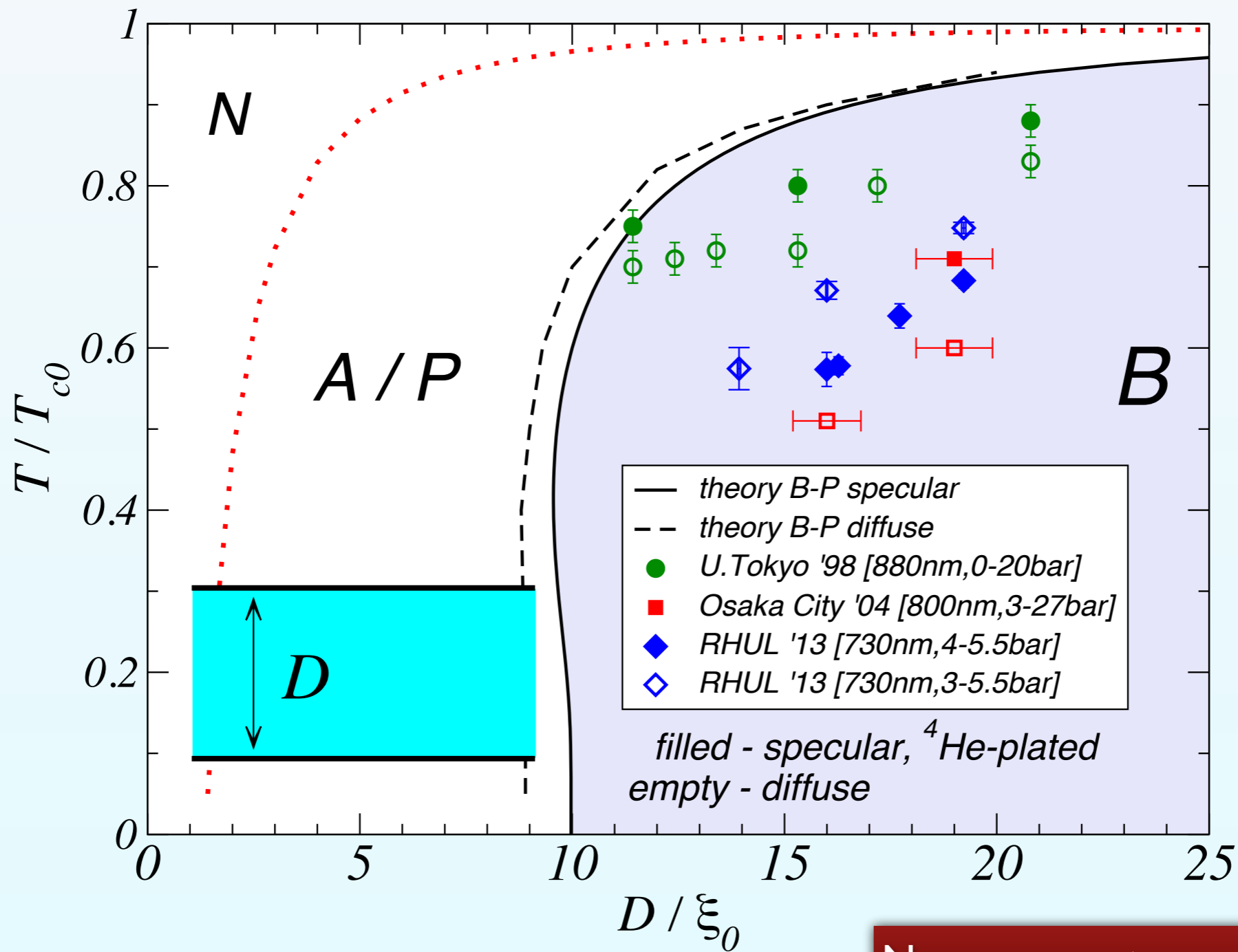
Recent experiments:
Stronger suppression of Superfluidity
than allowed by most pairbreaking
boundary condition

Berkley 1998
RIKEN 2003
RHUL 2012



after L. Levitin et al, Science 2013

A-B transition: experiments

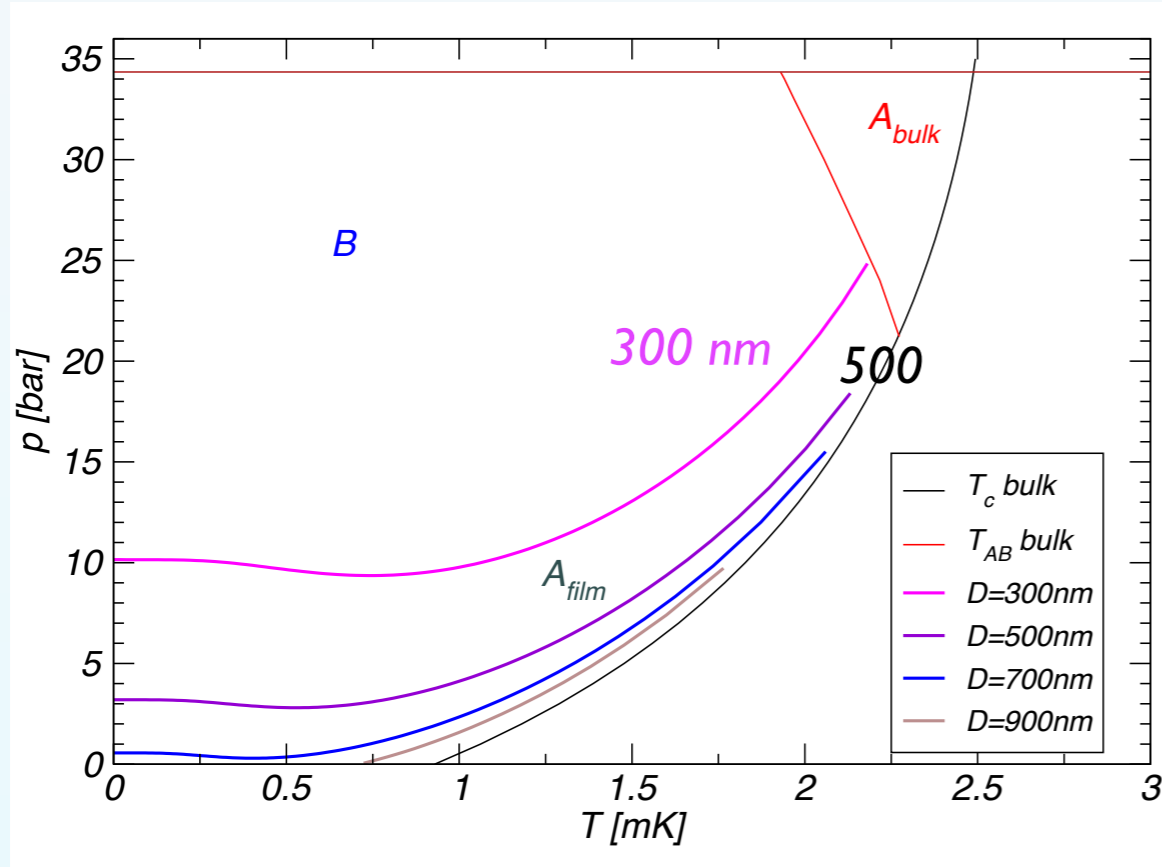


No agreement among measurements

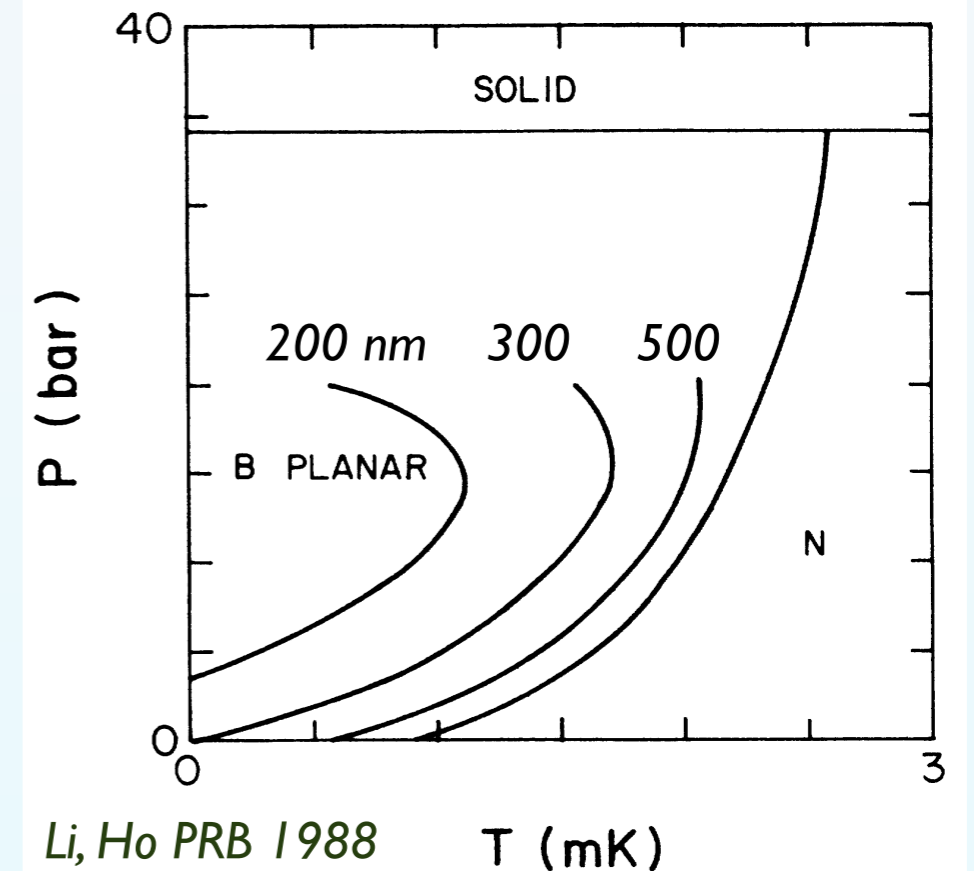
A-B transition: theory

Quasiclassical weak coupling

No agreement in theory



Ginzburg-Landau theory



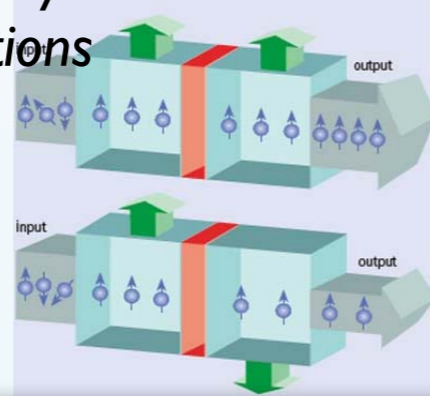
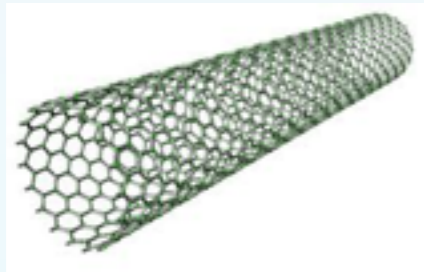
Grand Challenge 2

- Need for development of numerical approaches to model complex systems
- Joint effort of several groups

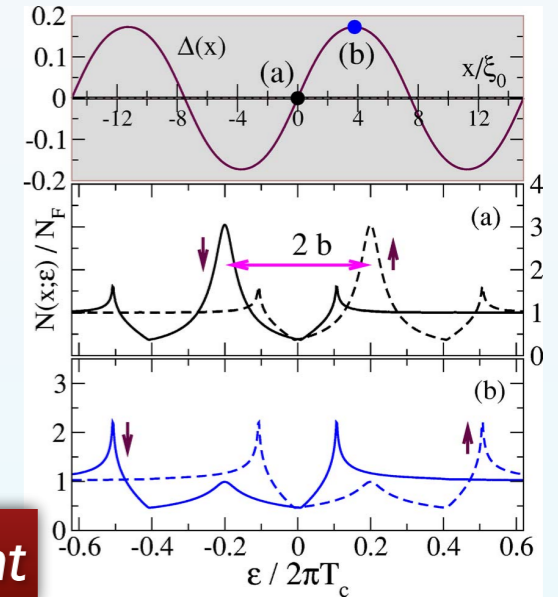
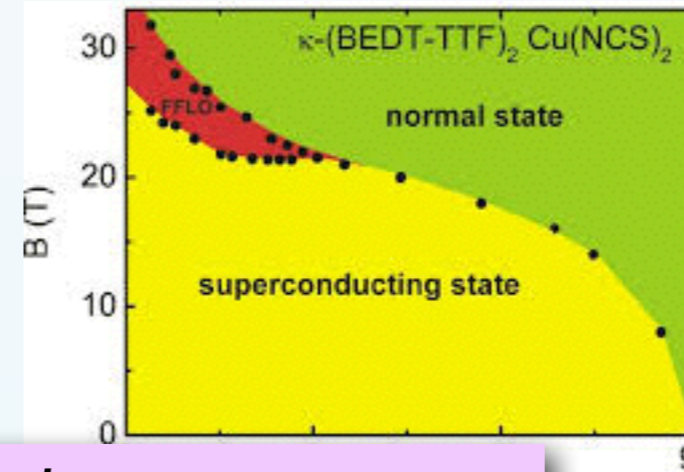
Broader connections

Nano-world:

- enhanced role of surface atomic layer
- strongly modified DOS + interactions
- quantum discrete levels
- coherence effects

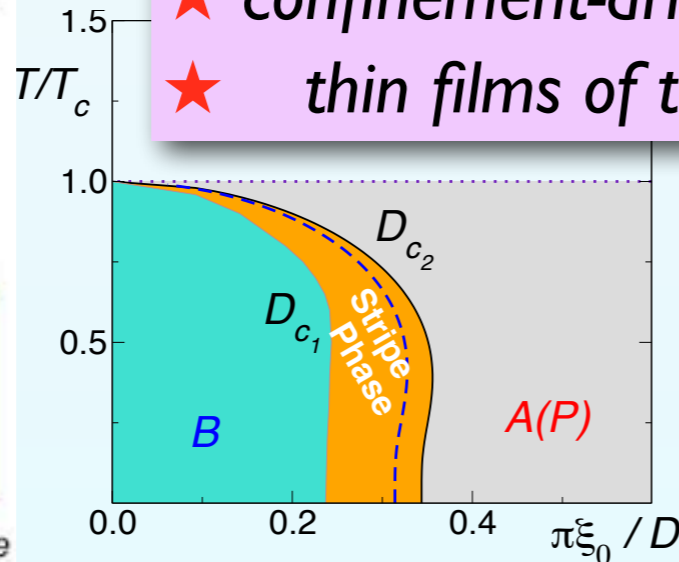
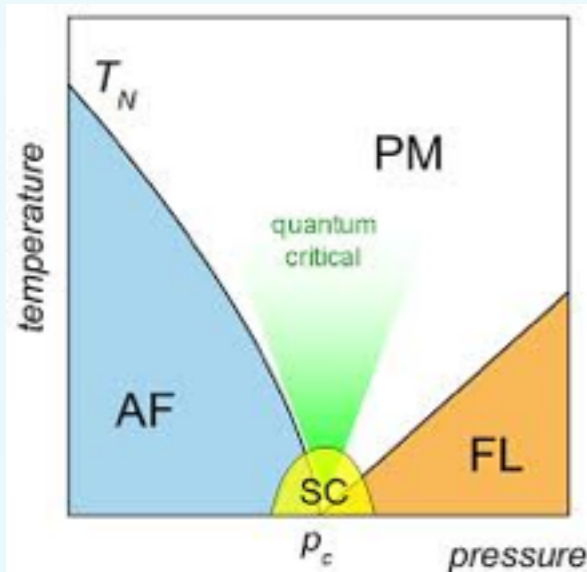


Mayaffre et al 2015, QFS'15 talk Aug 11, 11am

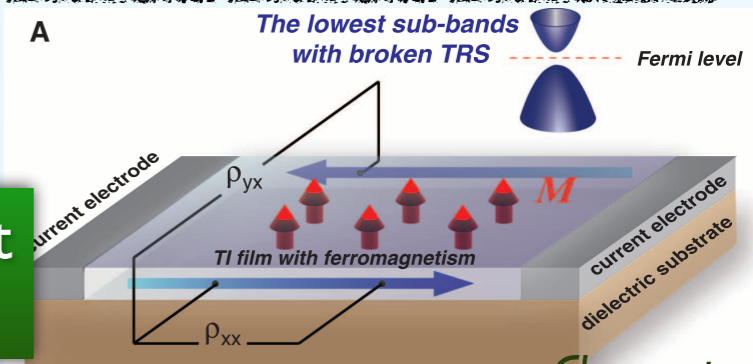


- ★ physics in restricted geometry
- ★ non-uniform states: FFLO
- ★ confinement-driven transitions: QPT
- ★ thin films of topological insulators

1964-present



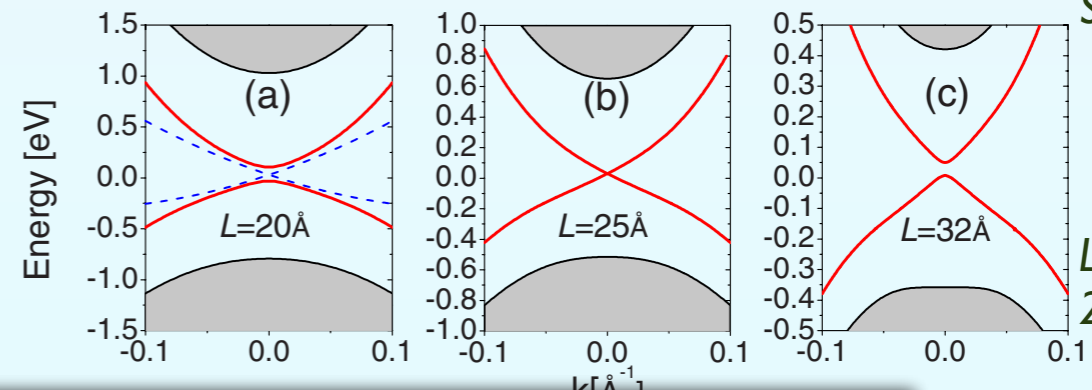
Anomalous Hall Effect in Magnetic TI



Chang et al, Science 2013

Quantum Critical Point:

- change of ground state by external parameter
- appearance of new phases near QCP



Lu et al, PRB 2010

Interaction of Dirac states in thin films

Vision for theory of restricted geometries

- ▶ *Superfluid He-3 is a model of unconventional pairing*
 - ➔ *1.1 9 x 2 order parameter components*
 - ➔ *1.2 symmetry and topology playground*
- ▶ **Grand Challenge:** *understanding surface states in confined geometry*
 - ➔ *2.1 properties of bound states*
 - ➔ *2.2 interactions with fields*
 - ➔ *2.3 connection to topological properties*
- ▶ **Grand Challenge:** *find agreement between theory and experiment (thin films)*
 - ➔ *3.1 numerical modeling - combined effort*
 - ➔ *3.2 connection to experiment*
- ▶ *Impact on various fields*
 - ➔ *4.1 States in confinement including FFLO*
 - ➔ *4.2 QPT and topological materials*

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